

Homework 4

Unless otherwise specified, assume room temperature ($T = 300$ K).

- 1) Purpose: Understanding p - n junction band diagrams.
Consider a p - n junction with $N_A = 5 \times 10^{14} \text{ cm}^{-3}$ and $N_D = 10^{18} \text{ cm}^{-3}$. Draw the band diagram of this device under the following conditions. Solve for and label all energy levels where applicable (intrinsic Fermi levels, Fermi levels and quasi-Fermi levels) and the potential barrier in each diagram.
 - a. At equilibrium (applied voltage $V_A = 0$ V).
 - b. At $V_A = 0.5$ V.
 - c. At $V_A = -1.0$ V.

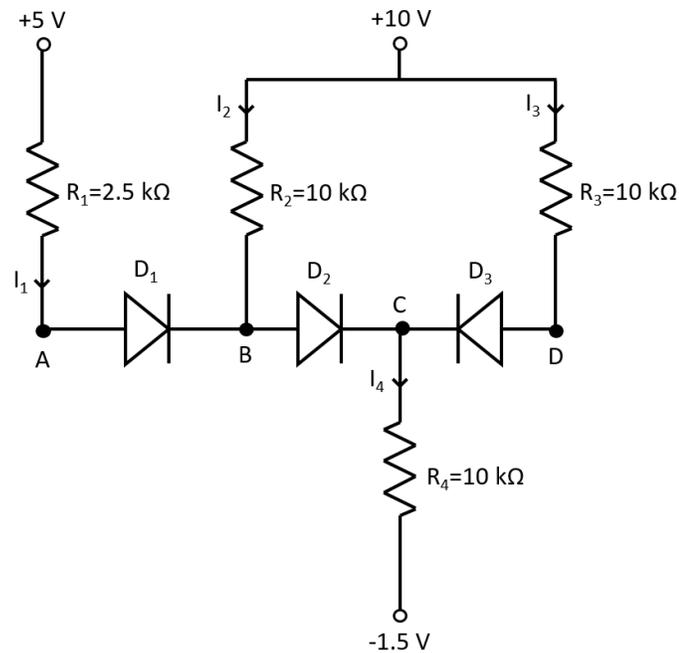
- 2) Purpose: Understanding p - n junction electrostatics.
Consider a silicon p - n junction with $N_A = 5 \times 10^{17} \text{ cm}^{-3}$ and $N_D = 10^{15} \text{ cm}^{-3}$. The relative permittivity of silicon is 11.8, and the permittivity of free space is $8.85 \times 10^{-14} \text{ F/cm}$.
 - a. Determine the magnitude of the depletion width on the p -side of the metallurgical junction (x_p), the depletion width on the n -side of the metallurgical junction (x_n), and the entire depletion width (W).
 - b. Determine the maximum electric field in the depletion width, as well as the electric field at $x = -x_p/2$.
 - c. Determine the built-in potential (V_{bi}), as well as the potential at $x = x_n/2$.

- 3) Purpose: Understanding junction capacitance.
Consider the p - n junction described in Question 2 above. Assume the cross-sectional area of the diode is $2 \times 10^{-5} \text{ cm}^2$.
 - a. Determine the equilibrium junction capacitance (C_{J0}).
 - b. The diode is to be used in an LC circuit with a 10-nH inductor. If the desired oscillation frequency of the circuit is $f = 5$ GHz, at what voltage should the diode be biased?

Hint: The applied bias will be negative.

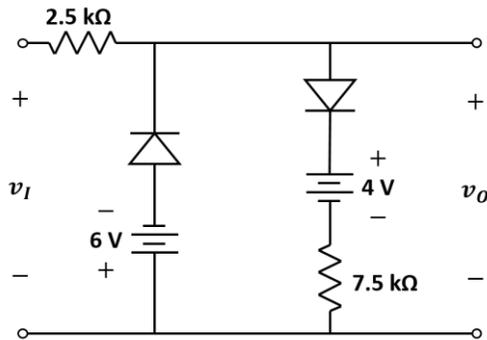
- 4) Purpose: Understanding p - n junction carrier concentrations.
Consider a silicon p - n junction with $N_A = 10^{16} \text{ cm}^{-3}$ and $N_D = 10^{18} \text{ cm}^{-3}$. Let the mobility of electrons (μ_n) be $1300 \text{ cm}^2/\text{V-s}$ and the mobility of holes (μ_p) be $400 \text{ cm}^2/\text{V-s}$. Let the minority carrier lifetime electrons and holes (τ_n and τ_p , respectively) both be 10^{-6} s. There is an applied voltage of 0.6 V.
 - a. Solve for the excess electron concentrations on the p -side of the junction at $130 \mu\text{m}$, $580 \mu\text{m}$, and $1160 \mu\text{m}$ away from the depletion width edge (i.e. moving further into the p -side of the device).
 - b. Solve for the excess hole concentration on the n -side of the junction at $70 \mu\text{m}$ and $1000 \mu\text{m}$ away from the depletion width edge.

- 5) Purpose: Understanding $p-n$ junction $I-V$ characteristics.
 Consider the same diode described in Question 3. What is the reverse saturation current (I_0) of the diode? What is the current in the diode when the applied voltage (V_A) is 0.6 V?
- 6) Purpose: Understanding how diodes behave in circuits.
 Find the Q-points for the three diodes in the circuit below. Use the constant voltage drop model for the diodes, with $V_{on} = 0.7$ V.
Hint: See Example 3.8 in Jaeger & Blalock.



7) Purpose: Using diodes to shape signal waveform.

Calculate output voltage, v_o , for the following circuit. Show the graphical representation of v_o for $-20\text{ V} \leq v_i \leq +20\text{ V}$, assuming ideal diodes. Show all work for full credit.



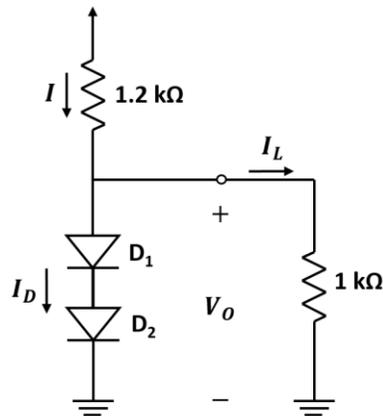
8) Purpose: Implementing diodes in practical circuits.

A particular design of a voltage regulator circuit is shown in the next page. Diodes D_1 and D_2 each has a voltage drop of 0.65 V at 1.4 mA.

(a) What regulator voltage output, V_O , when a 1 k Ω resistance is not connected (no load condition)?

(b) What is V_O when a 1 k Ω resistance is added as load?

Hint: Use diode exponential model and iterative process to solve V_O .



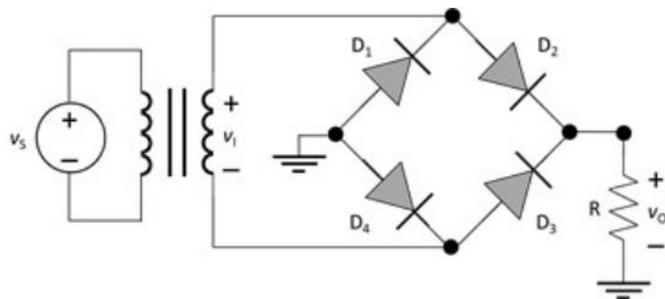
9) Purpose: Investigating the full-wave bridge rectifier.

Consider the following full wave rectifier circuit. The supply voltage from wall-point is stepped down using a transformer and connected to the input of the full wave rectifier.

Here, the input voltage (v_I) to the rectifier is a *sine-wave* with amplitude of 10 V.

Assume that diodes can be represented by the constant-voltage-drop model with $V_D = 0.6$ V.

(a) Show the current path for the positive and negative half-cycle of v_I . Also, sketch and clearly label the transfer characteristic (v_O vs. v_I) and the time response (same plot showing v_O vs. t and v_I vs. t) of the circuit shown.



(b) The output resistance, R is now replaced with a Zener diode, Z . Assume that the Zener voltage is 6.5 V and that r_z is negligibly small. How does the transfer characteristic and time response change? Generate both plots for the modified circuit.

