



ECE 4813

Semiconductor Device and Material Characterization

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As with all of these lecture slides, I am indebted to Dr. Dieter Schroder from Arizona State University for his generous contributions and freely given resources. Most of (>80%) the figures/slides in this lecture came from Dieter. Some of these figures are copyrighted and can be found within the class text, *Semiconductor Device and Materials Characterization*. **Every serious microelectronics student should have a copy of this book!**



Optical Characterization

Optical Microscopy

Ellipsometry

Transmission

Reflection

Photoluminescence

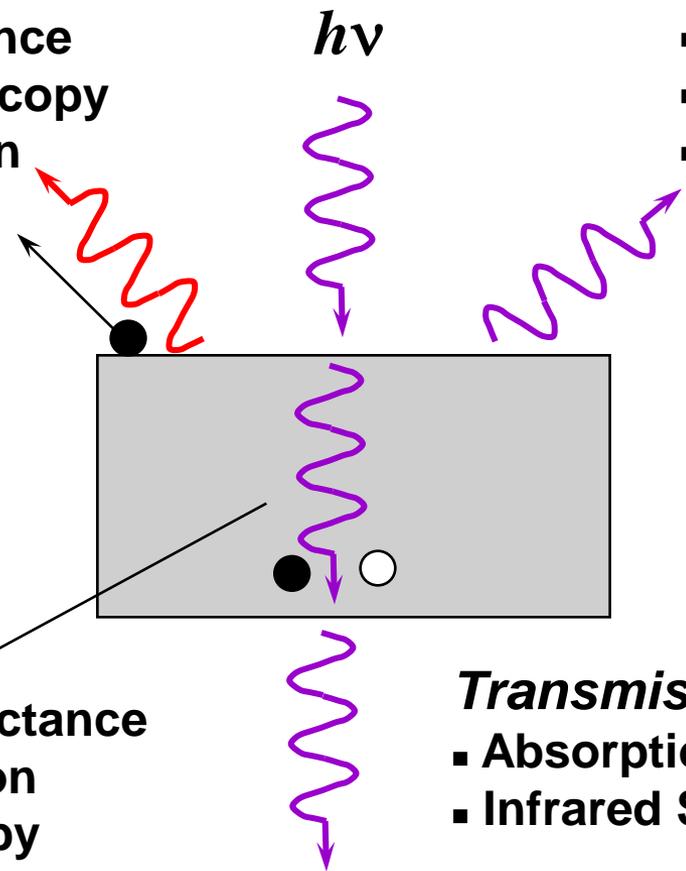
Optical Excitation

Emission

- Photoluminescence
- Raman Spectroscopy
- UV Photoelectron Spectroscopy

Reflection

- Optical Microscopy
- Ellipsometry
- Reflection Spectroscopy



Absorption

- Photoconductance
- Photoelectron Spectroscopy

Transmission

- Absorption Coefficient
- Infrared Spectroscopy



Optical Characterization

- **Photometric Measurements**
 - **Amplitude of reflected or transmitted light**
 - **⇒ Optical constants, absorption coefficients**

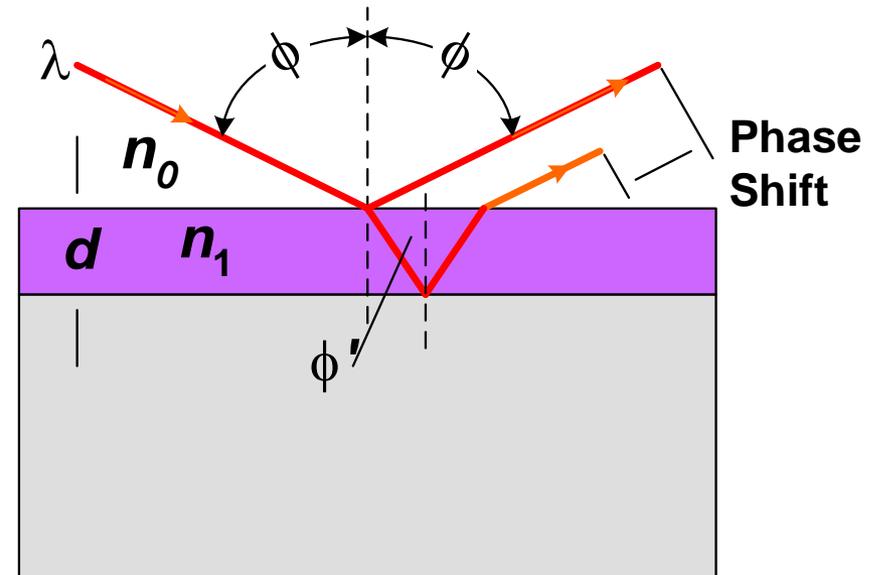
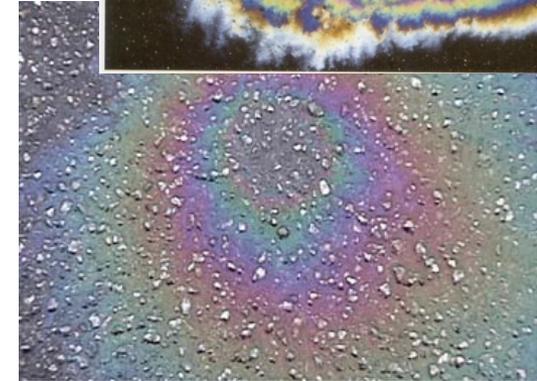


Optical Characterization

- **Interference Measurements**
 - **Phase of reflected or transmitted light**
 - \Rightarrow **Film thickness, surface structure**
 - **Two emerging light beams are phase shifted**
 - \Rightarrow **Constructive and destructive interference**

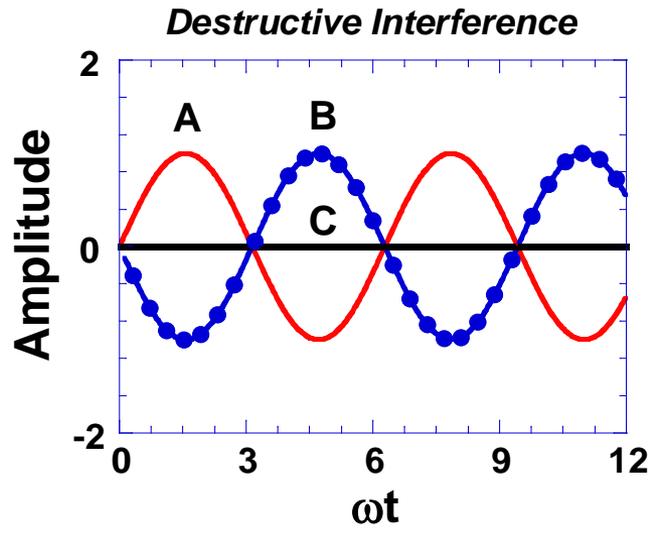
$$n_1 \sin \phi' = n_0 \sin \phi$$

$$d = \frac{\lambda}{2\sqrt{n_1^2 - n_0^2 \sin^2 \phi}}$$

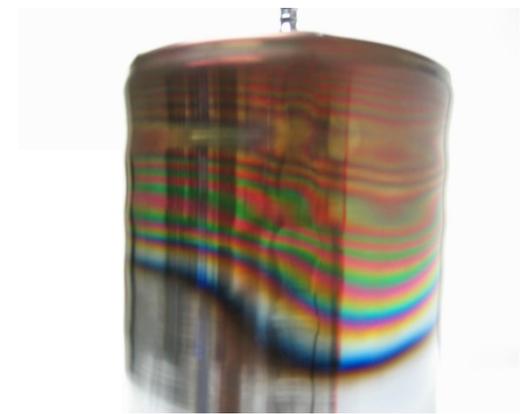
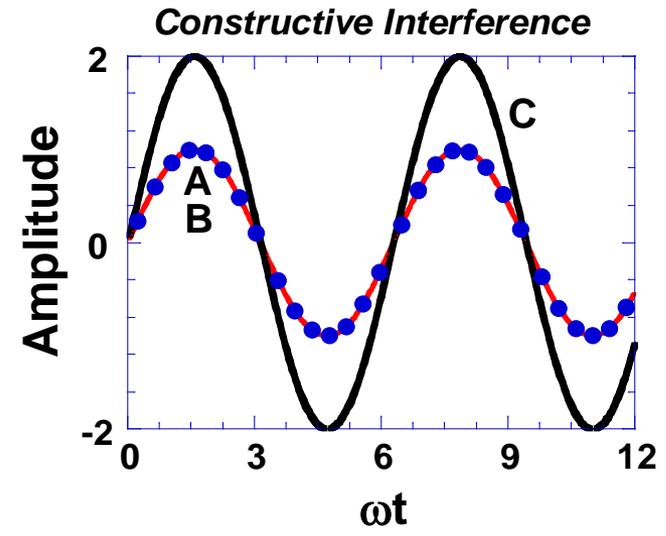




Interference



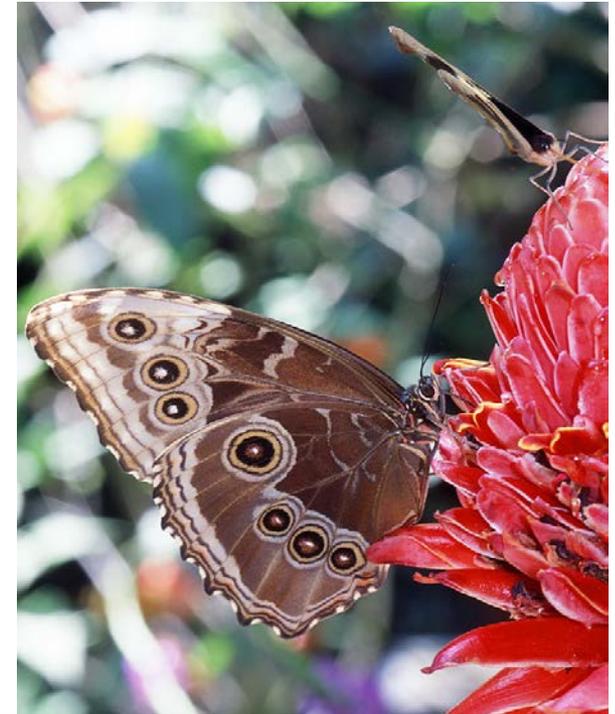
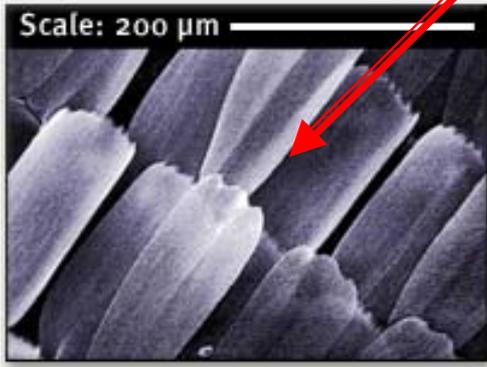
Eye



Oxide thickness variations

Interference

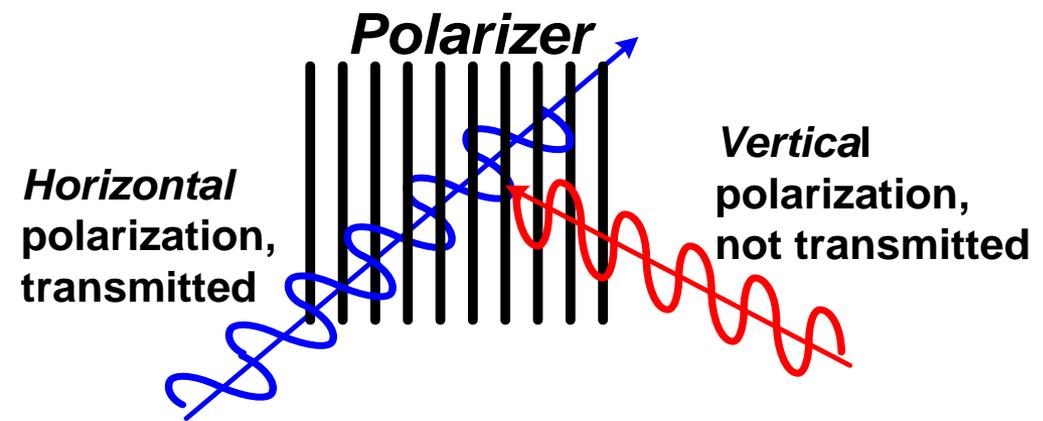
- *Blue Morpho* butterfly gets its bright blue color from interference effects
- Interference due to microscopic ridges on the wings



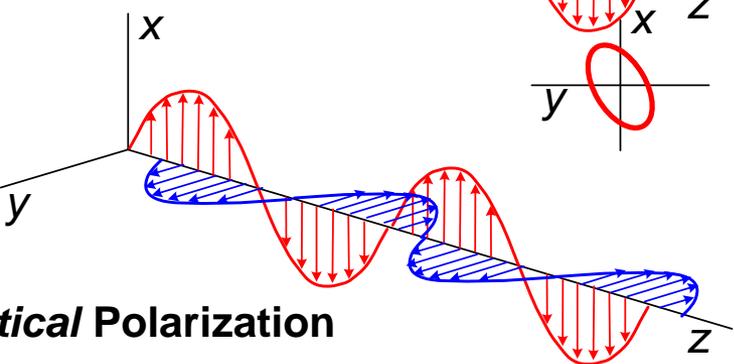
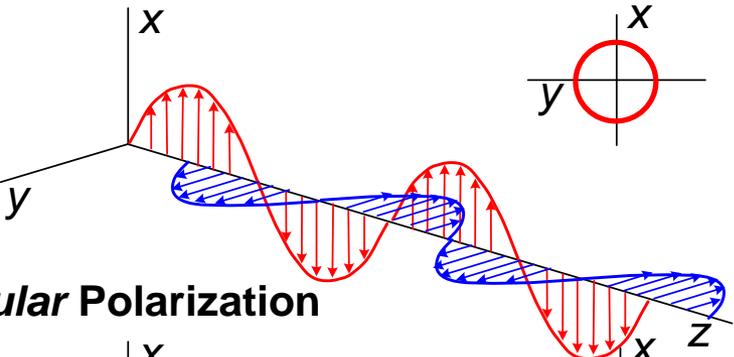
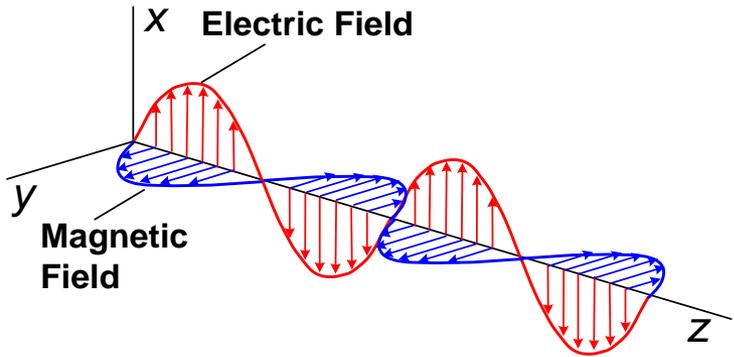


Optical Characterization

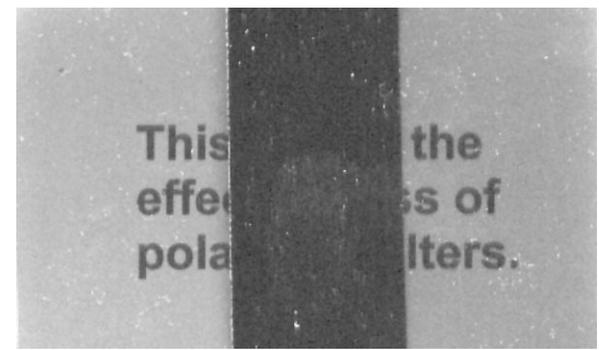
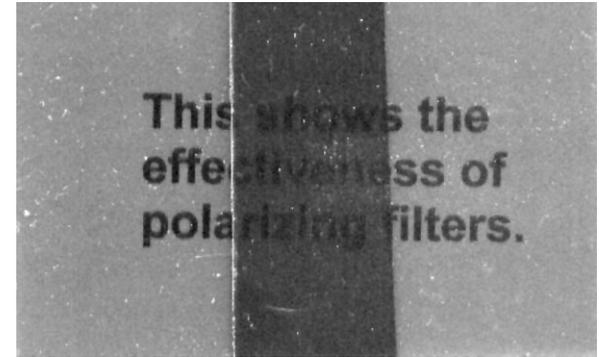
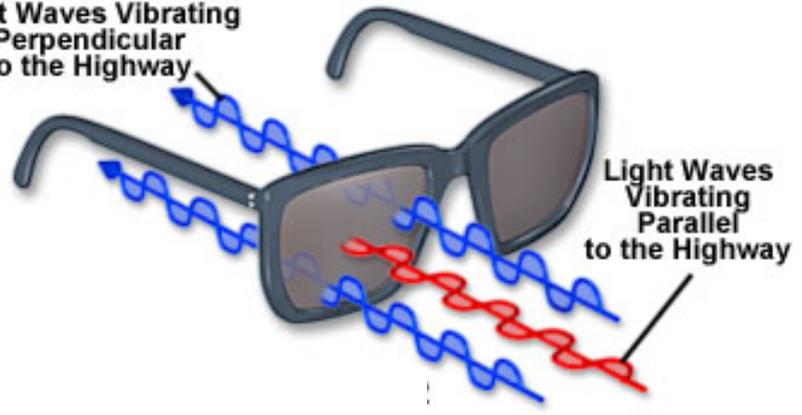
- ***Polarization* Measurements**
 - Ellipticity of reflected light
 - ⇒ Optical constants, film thickness, surface structure
- **Polarizer polarizes the light into particular orientation**
- **H-sheet; most popular linear polarizer**
 - Polyvinyl alcohol (plastic sheet) is heated and stretched
 - Sheet is dipped into iodine solution
 - Iodine impregnates the plastic, attaches to long-chain molecules, forms “wire” grid



Polarized Light



Light Waves Vibrating Perpendicular to the Highway





Polarizing Filter Effect

- Colored light from thin-film iridescence in butterflies is often polarized
- Left wings: unmodified
- Right wings: generated by taking two photographs through a polarizing filter rotated by 90° between exposures, and then producing the difference of the two images
- One shows a pattern of polarized and depolarized regions, the other does not
- Wing color important in male attraction to females

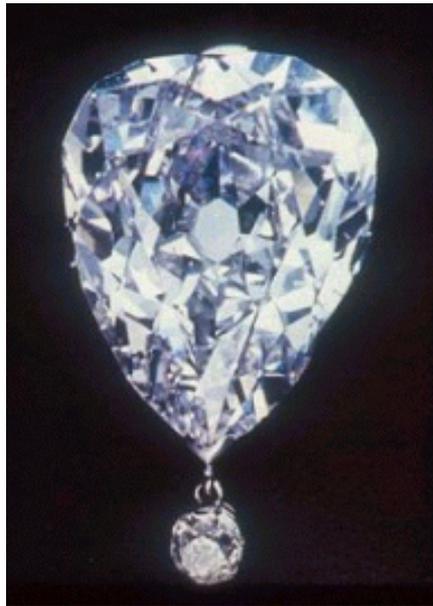


A. Sweeney et al. *Nature* **423**, 31 (2003)



Diamonds

- What's so special about diamonds?



**Star of South
Africa Diamond
83.5 Carats**

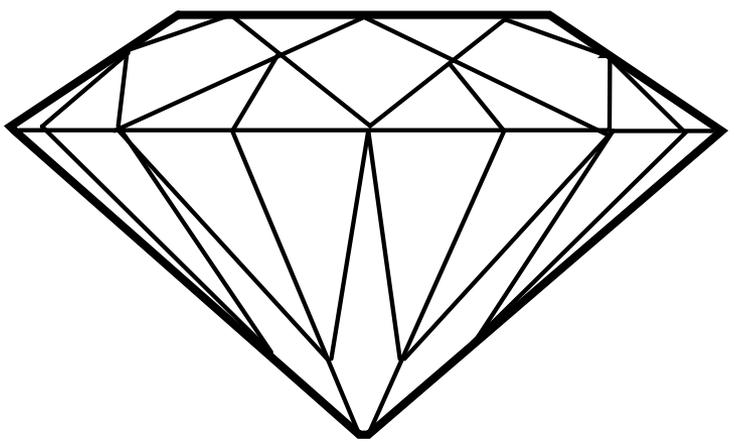


**Taylor Diamond
69 Carats**

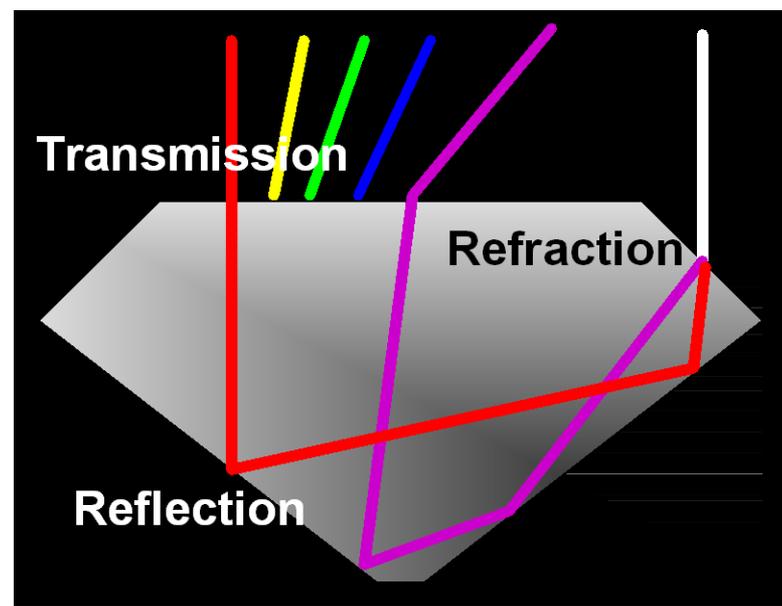


Transmission, Reflection, Refraction

- A diamond is polished into a particular shape for maximum light refraction/reflection/transmission

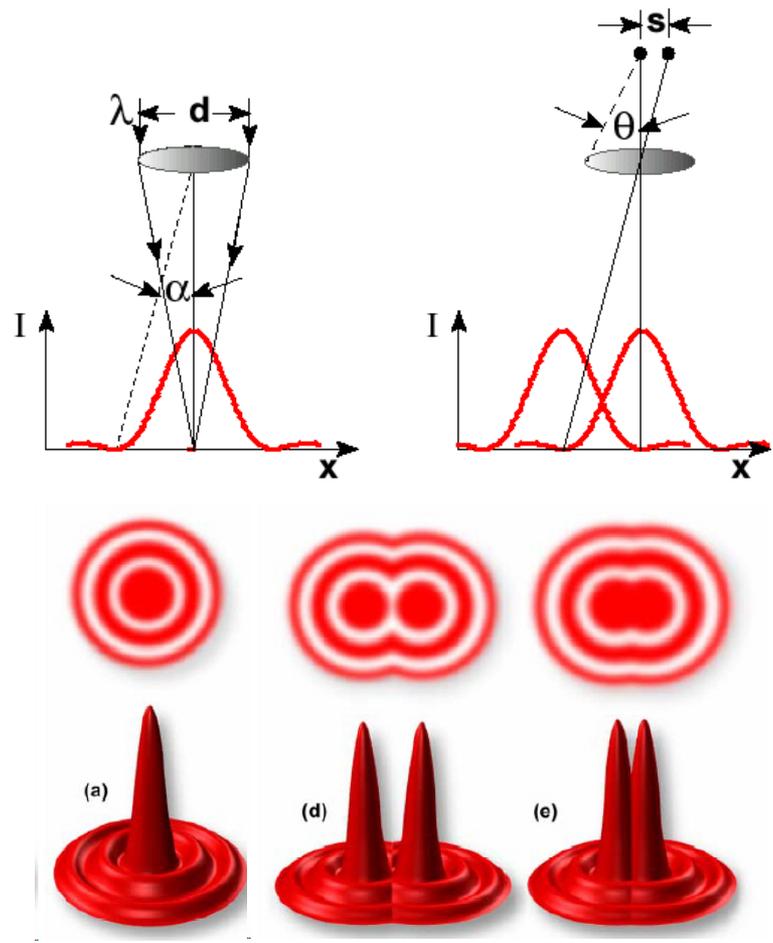


58 Facets



Optical Microscopy

- Light cannot be focused to an infinitesimally small spot due to the wave nature of light

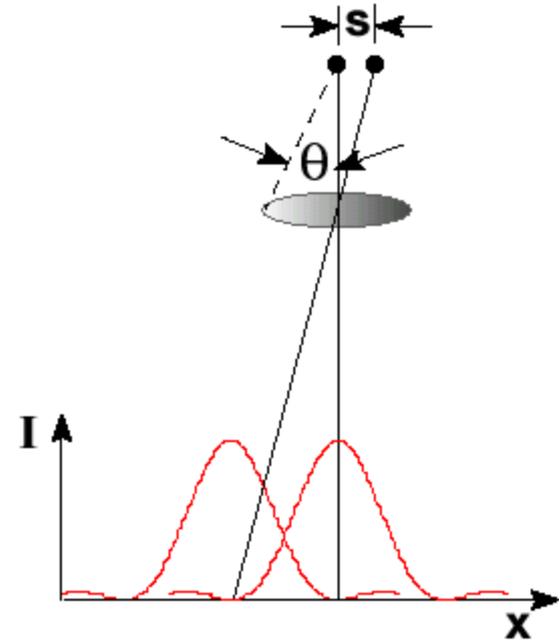


Optical Microscopy

- There is no lower limit to the size of an *isolated* object that can be detected
- The minimum separation, s , of two point objects occurs when the first maximum of the diffraction pattern of one object falls on the first minimum of the second object

$$s = \frac{0.61\lambda}{n \sin \theta} = \frac{0.61\lambda}{NA}$$

- λ = free space wavelength,
 n = refractive index of immersion medium, θ = half the angle subtended by the lens at the object,
 NA = numerical aperture

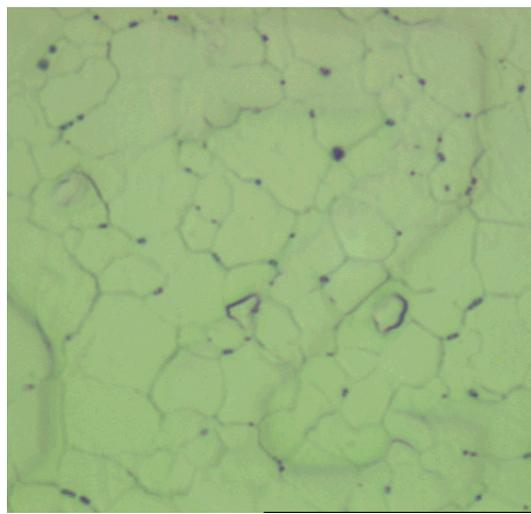


**Best resolution about $0.25 \mu m$
for $\lambda \approx 0.4 \mu m$, $NA \approx 1$**

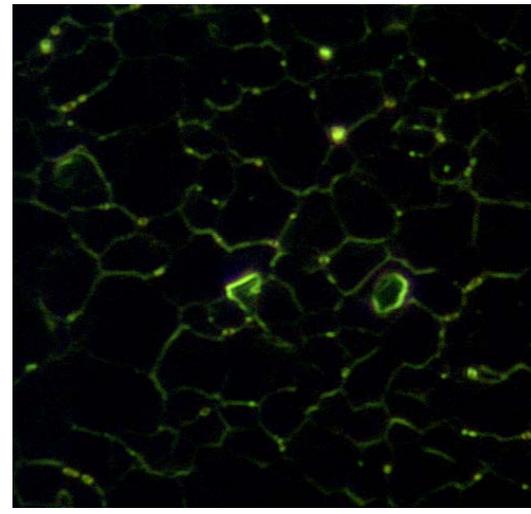


Optical Microscopy

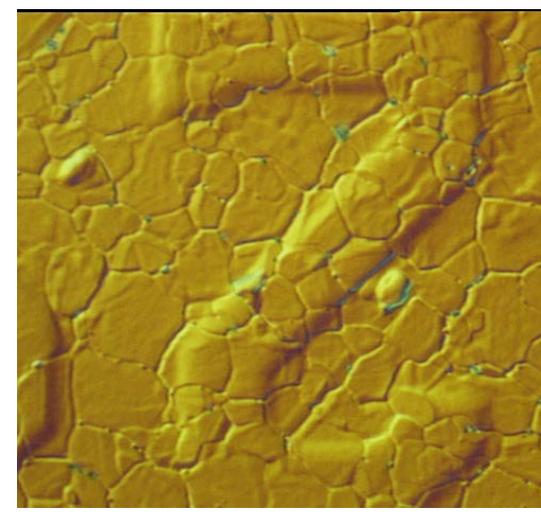
- Different approaches to optical microscopy bring out different features



Bright Field



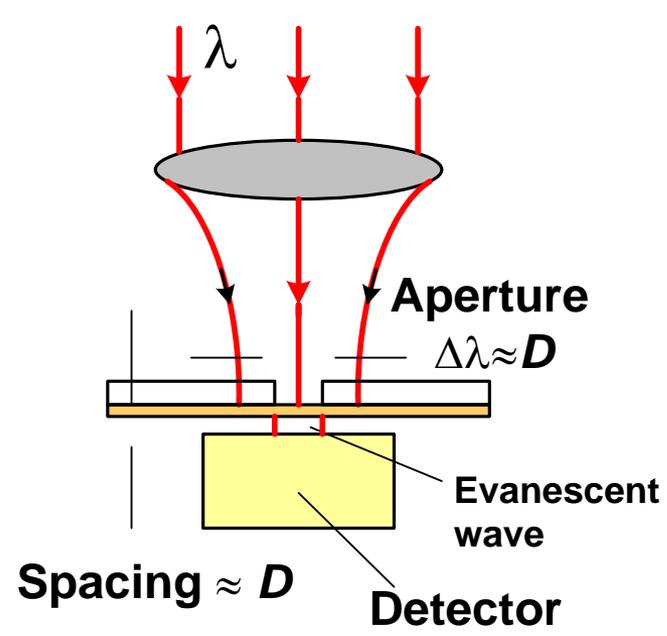
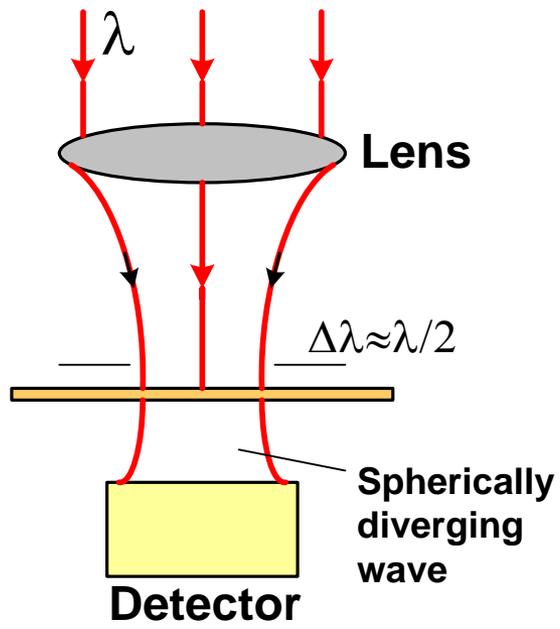
Dark Field



Interference Contrast

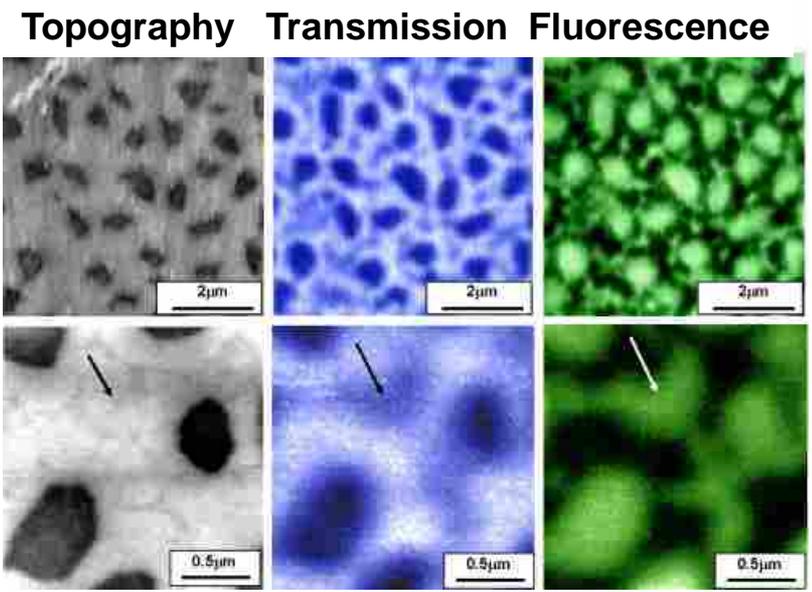
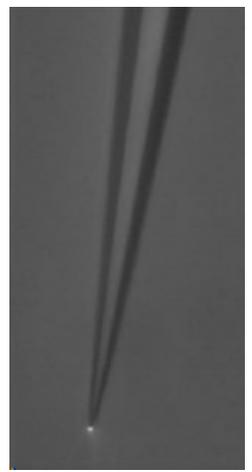
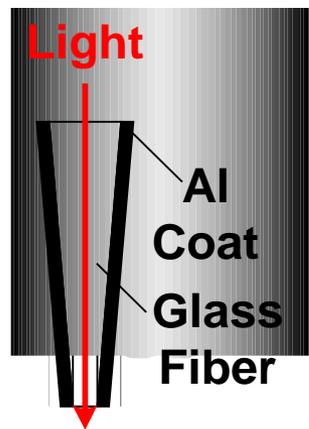
Near Field Optical Microscopy

- Conventional microscopy
 - ◆ Images the *far field*, where Raleigh limit prevails
- Near field microscopy
 - ◆ Images the *near field*, where solution determined by aperture, not wavelength
 - ◆ Detector must be very close to sample



Near Field Optical Microscopy

- The light is confined to a small aperture
 - ◆ Drawn or etched glass fiber



Polymer Sample

Physics.nist.gov/Divisions/Div844/facilities/nsom/nsom.html



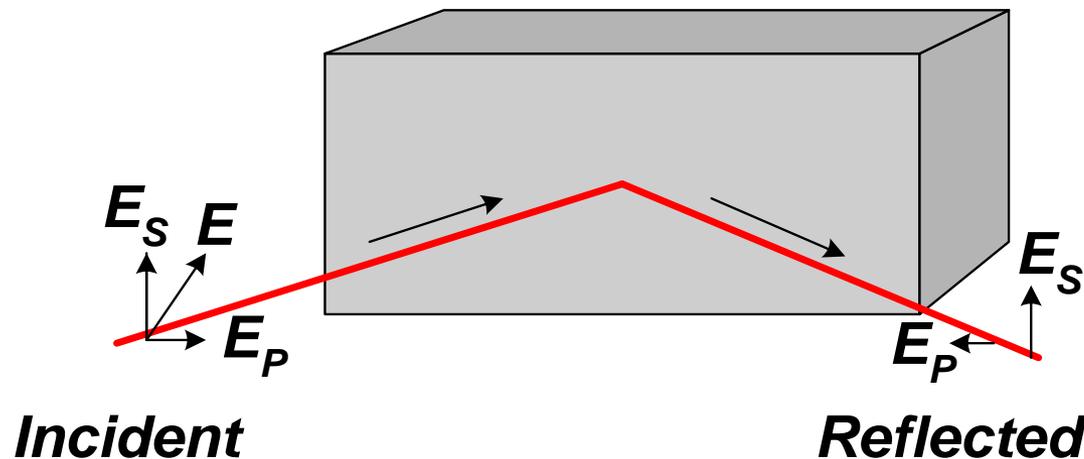
Ellipsometry

Definition

- Measurement of the state of polarization of a polarized light wave

General Scheme

- A polarized light wave probe interacts with an "optical system", this interaction changes the state of polarization, measurement of the initial and final states is performed this yields information about the optical constants of the "system"

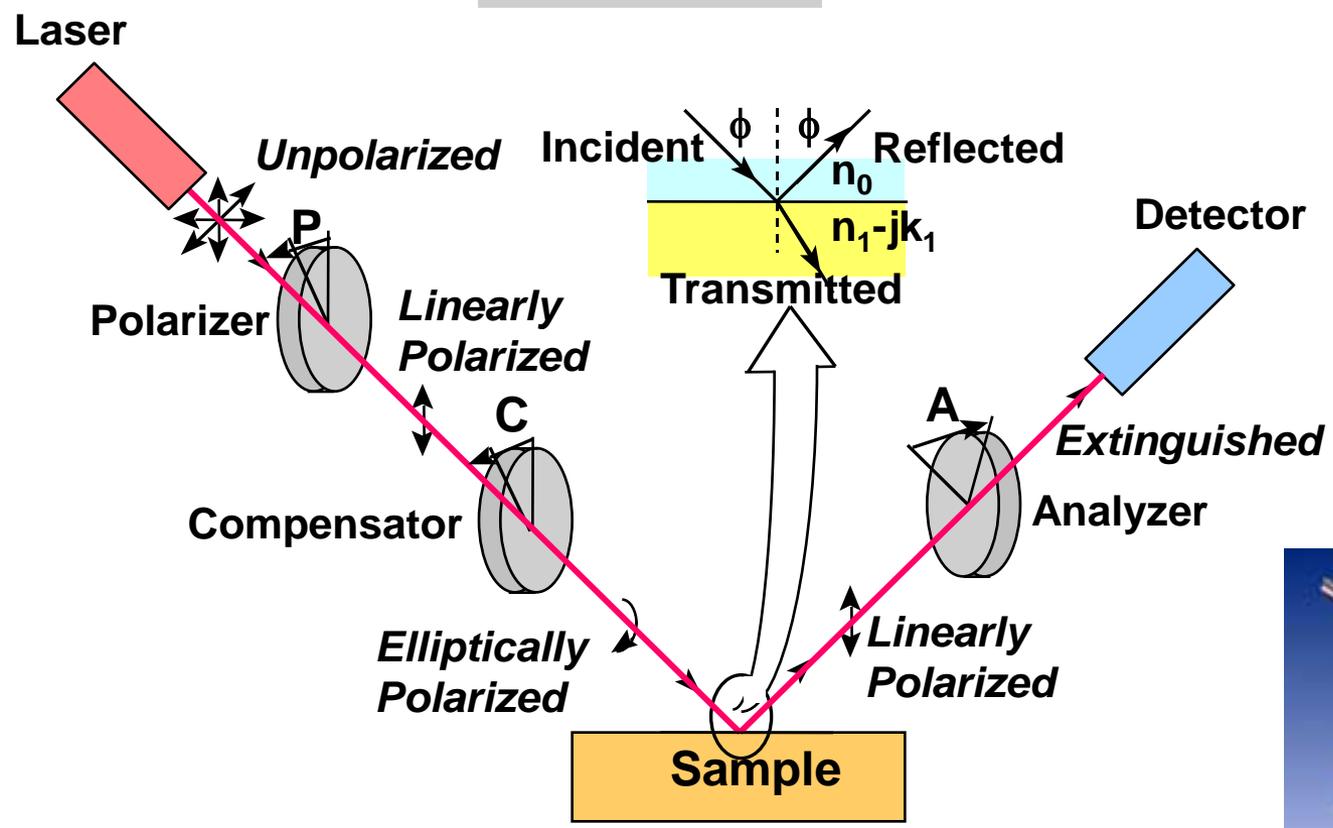


Null Ellipsometer

- ◆ Angles P, C, and A lead to ellipsometry quantities ρ , Ψ and Δ

$$\rho = \tan \Psi e^{j\Delta}$$

The ellipsometry equation!





Ellipsometry

- **Nondestructive technique**
- **Film thickness measurement; can measure film thicknesses down to 1 nm**
- **Refractive index determination; can measure refractive index of thin films of unknown thickness**
- **Azimuth angles can be measured with great accuracy**
- **Measures a ratio of two values**
 - ◆ **Highly accurate and reproducible (even in low light levels)**
 - ◆ **No reference sample necessary**
 - ◆ **Not as susceptible to scatter, lamp or purge fluctuations**
- **Surface uniformity assessment**
- **Composition determinations**
- **Can be used for *in situ* analysis**



Ellipsometer

- **Null ellipsometry**

- ◆ Polarizer-Compensator-Sample-Analyzer
- ◆ Polarizer and Compensator Angles adjusted for linear polarization upon reflection
- ◆ Analyzer is adjusted to extinguish reflected light

- **Rotating Analyzer Ellipsometry**

- ◆ Analyzer rotates

$$I(\theta) = I_0 [1 + a_2 \cos 2\theta + b_2 \sin 2\theta]$$

$$\Psi = \frac{1}{2} \cos^{-1}(-a_2); \quad \Delta = \cos^{-1} \left(\frac{b_2}{\sqrt{1 - a_2^2}} \right)$$

- **Spectroscopic Ellipsometry**

- Uses *several wavelengths*
- Can also use *several angles*



Ellipsometry

- Measure change of polarization state of light reflected from a surface

$$R_p = \frac{E_p(\text{reflected})}{E_p(\text{incident})}; \quad R_s = \frac{E_s(\text{reflected})}{E_s(\text{incident})}$$

$$\rho = \frac{R_p}{R_s} = \tan \Psi e^{i\Delta}$$

- For an air-solid with an absorbing substrate

$$n_1^2 - k_1^2 = n_0^2 \sin^2 \phi \left[1 + \frac{\tan^2 \phi [\cos^2 2\Psi - \sin^2 2\Psi \sin^2 \Delta]}{[1 + \sin 2\Psi \cos \Delta]^2} \right]$$

$$2n_1 k_1 = \frac{n_0^2 \sin^2 \phi \tan^2 \phi \sin 4\Psi \sin \Delta}{[1 + \sin 2\Psi \cos \Delta]^2}$$



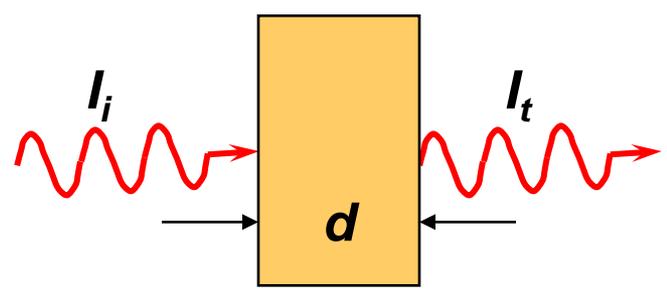
Transmission / Absorption

Definition

- Absorption - the loss of a photon from an incident flux by the process of exciting an electron from a lower- to a higher-energy state

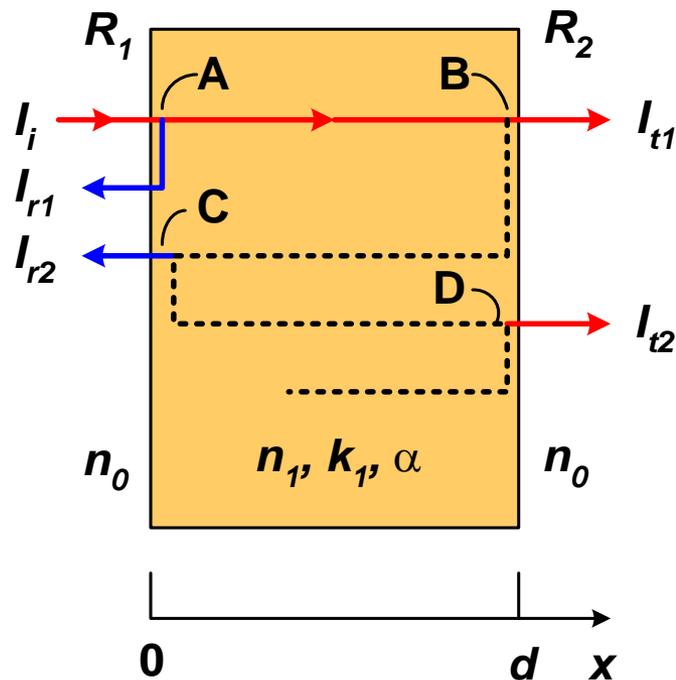
General Scheme

- Light is incident on a thin sample part of the light is reflected and the remainder is absorbed or transmitted; a measurement is made of the transmitted intensity
- The experiment can be carried out as a function of temperature, externally applied fields, sample thickness, etc.



Transmission

- Optical transmission measurements
 - Sample thickness
 - Absorption coefficient
 - Impurities in semiconductors (oxygen and carbon in Si)



$$T = \frac{I_t}{I_i} = \frac{(1 - R_1)(1 - R_2)e^{-\alpha d}}{1 + R_1 R_2 e^{-2\alpha d} - 2\sqrt{R_1 R_2} e^{-\alpha d} \cos \phi}$$

For $R_1 = R_2$:

$$T = \frac{(1 - R)^2 e^{-\alpha d}}{1 + R^2 e^{-2\alpha d} - 2R e^{-\alpha d} \cos \phi}$$

$$R = \frac{(n_0 - n_1)^2 + k_1^2}{(n_0 + n_1)^2 + k_1^2} \quad \phi = \frac{4\pi n_1 d}{\lambda}$$



Transmission

$$T = \frac{(1-R)^2 e^{-\alpha d}}{1 + R^2 e^{-2\alpha d} - 2R e^{-\alpha d} \cos \phi}$$

$$T = \frac{1}{2\pi} \int_{-\pi}^{\pi} \frac{(1-R)^2 e^{-\alpha d}}{1 + R^2 e^{-2\alpha d} - 2R e^{-\alpha d} \cos \phi} d\phi$$

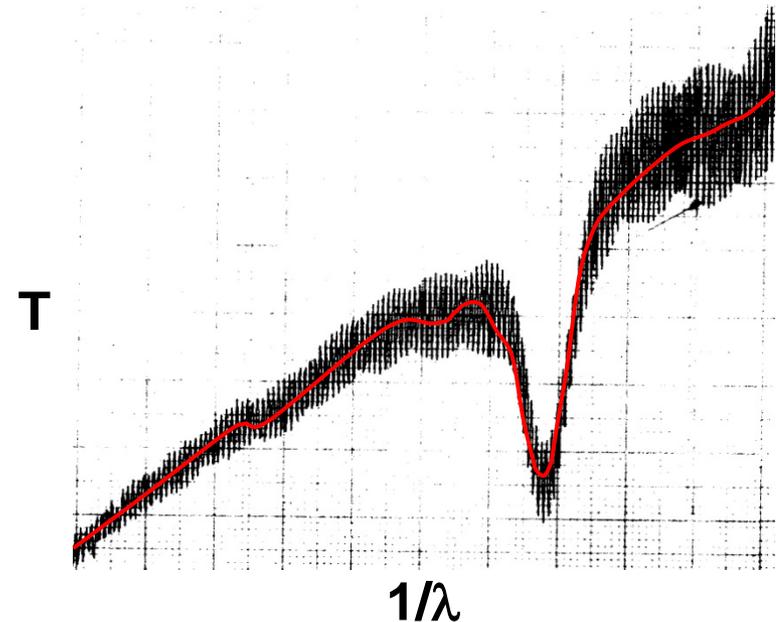
- If detector has insufficient resolution

$$T = \frac{(1-R)^2 e^{-\alpha d}}{1 - R^2 e^{-2\alpha d}}$$

- If $\alpha = 0$

$$T = \frac{(1-R)^2}{1 + R^2 - 2R \cos \phi}$$

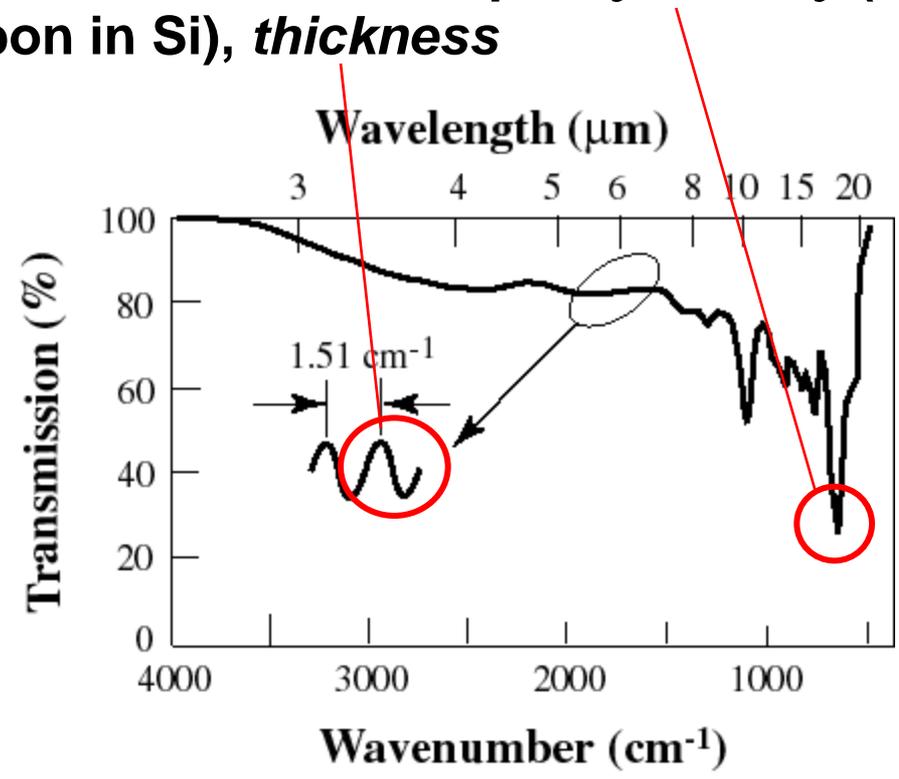
$$T = \frac{(1-R)^2}{1 - R^2} = \frac{1-R}{1+R}$$





Transmission

- Gives *absorption coefficient, impurity density (e.g., oxygen, carbon in Si), thickness*



$$\alpha = \frac{1}{d} \ln \left(\frac{(1-R)^2 + \sqrt{(1-R)^4 + 4T^2R^2}}{2T} \right); \quad d = \frac{1}{2n_1 \Delta(1/\lambda)}$$



Thickness

- Oscillations are determined by

$$\cos 4\pi nd / \lambda;$$

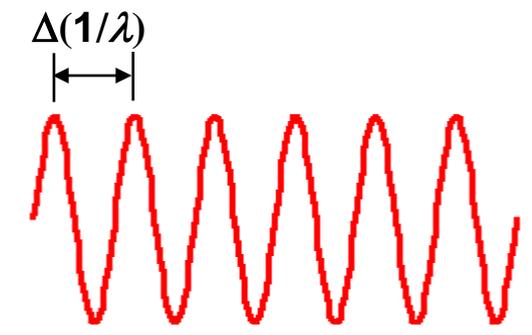
- Has maxima at

$$d = \frac{m\lambda_0}{2n}; d = \frac{(m+1)\lambda_1}{2n} \dots \dots \dots d = \frac{(m+i)\lambda_i}{2n}$$

$$\Rightarrow m = \frac{i\lambda_i}{\lambda_0 - \lambda_i}$$

$$d = \frac{1\lambda_0\lambda_i}{2n(\lambda_0 - \lambda_i)} = \frac{i}{2n(1/\lambda_i - 1/\lambda_0)}$$

$$\text{For } i = 1: d = \frac{1}{2n(1/\lambda_1 - 1/\lambda_0)} = \frac{1}{2n\Delta(1/\lambda)}$$

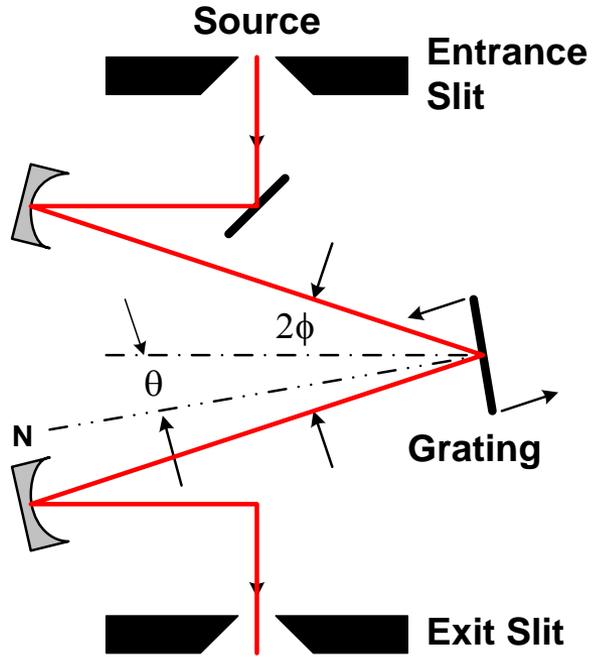


$1/\lambda$: **Wave number**

Instrumentation

- Two types of instruments are used

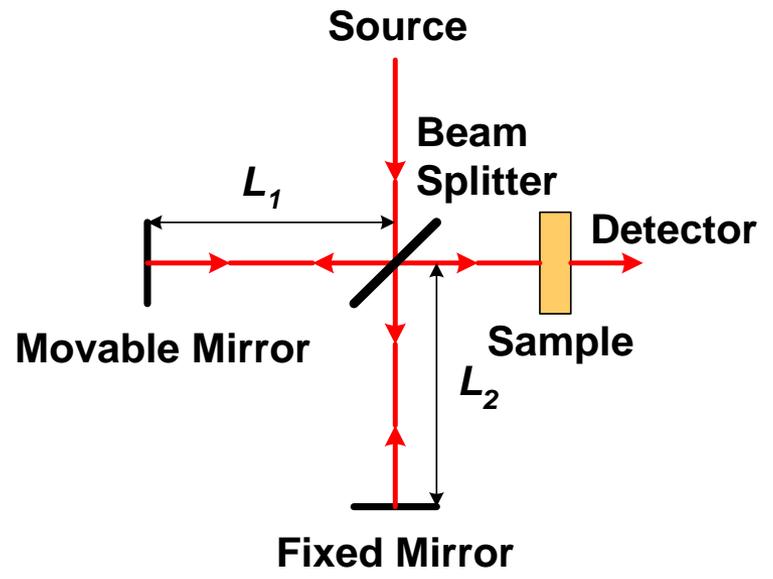
Monochromator



$$m\lambda = 2d \sin(\theta)\cos(\phi)$$

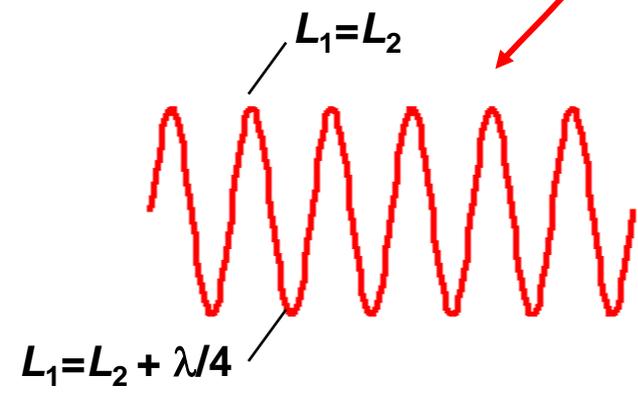
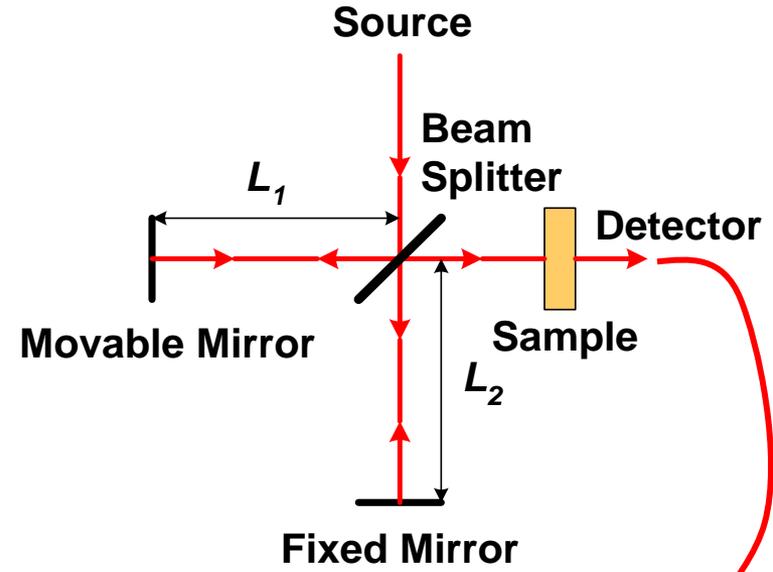
$m = 1, 2, 3 \dots$
 $d = \text{line spacing of grating}$

Interferometer



Interferometer

- Let source be $\cos 2\pi f x$
 - ◆ f : frequency of light
 - ◆ x : movable mirror location
- $L_1 = L_2$
 - ◆ Constructive interference
 - ◆ Maximum detector output
- $L_1 = L_2 + \lambda/4$
 - ◆ Destructive interference
 - ◆ Zero detector output





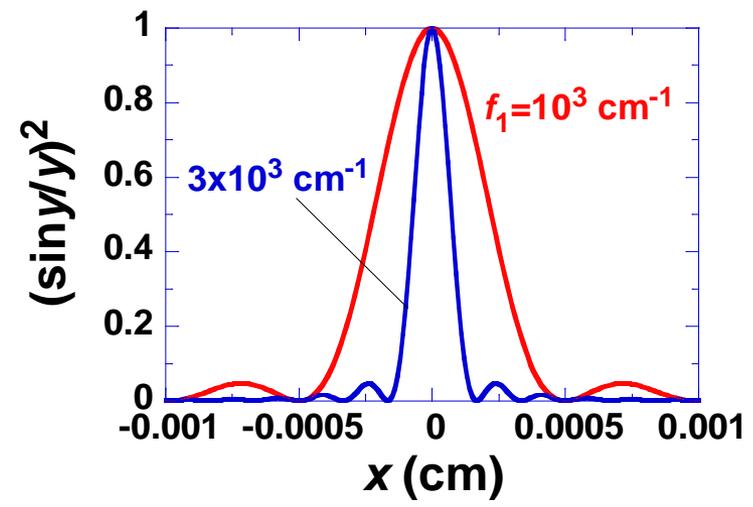
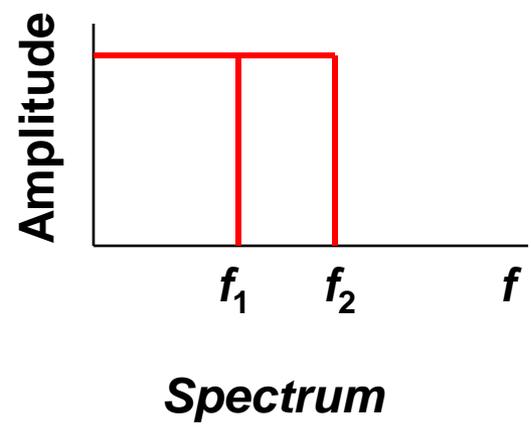
Fourier Transform Infrared Spectroscopy

- Fourier transform infrared spectroscopy (FTIR)

$$I(x) = B(f)[1 + \cos 2\pi xf] \quad I(x) = \int_0^f B(f)[1 + \cos 2\pi xf] df$$

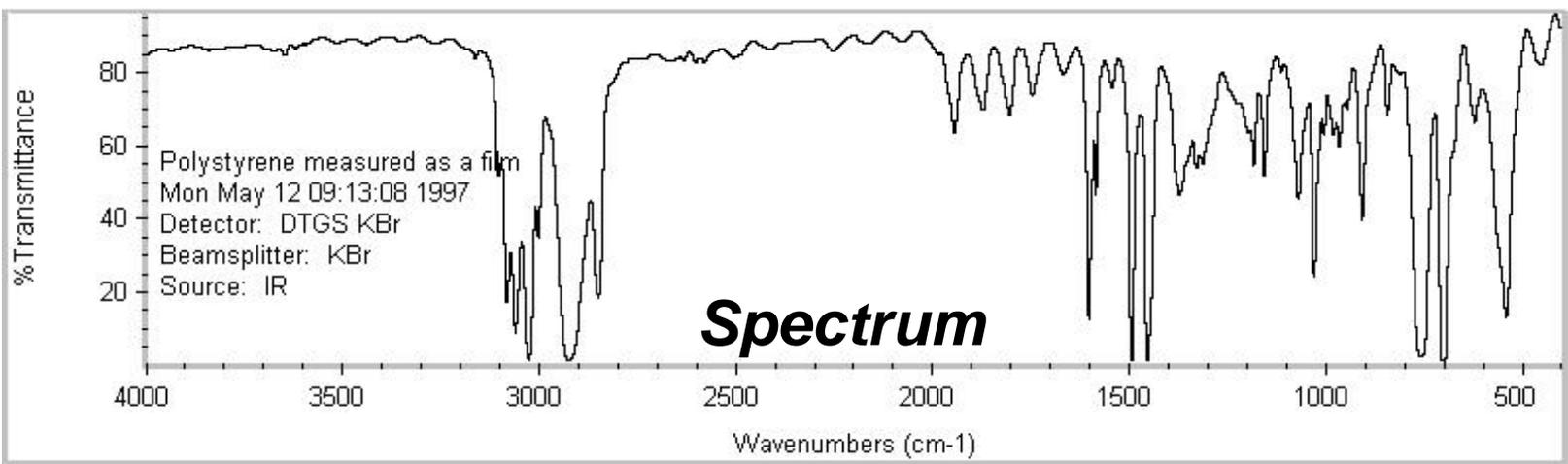
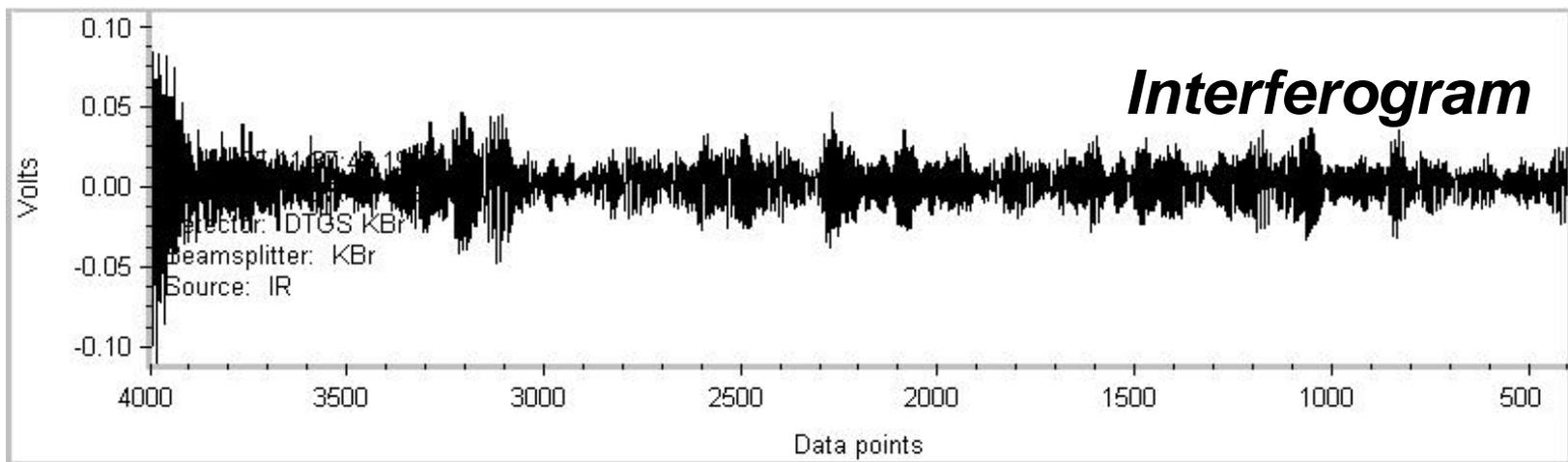
$$I(x) = \int_0^{f_1} A \cos 2\pi xf df = Af_1 \frac{\sin 2\pi xf_1}{2\pi xf_1}$$

$$B(f) = \int_{-\infty}^{\infty} I(x) \cos 2\pi xf dx$$



Interferogram

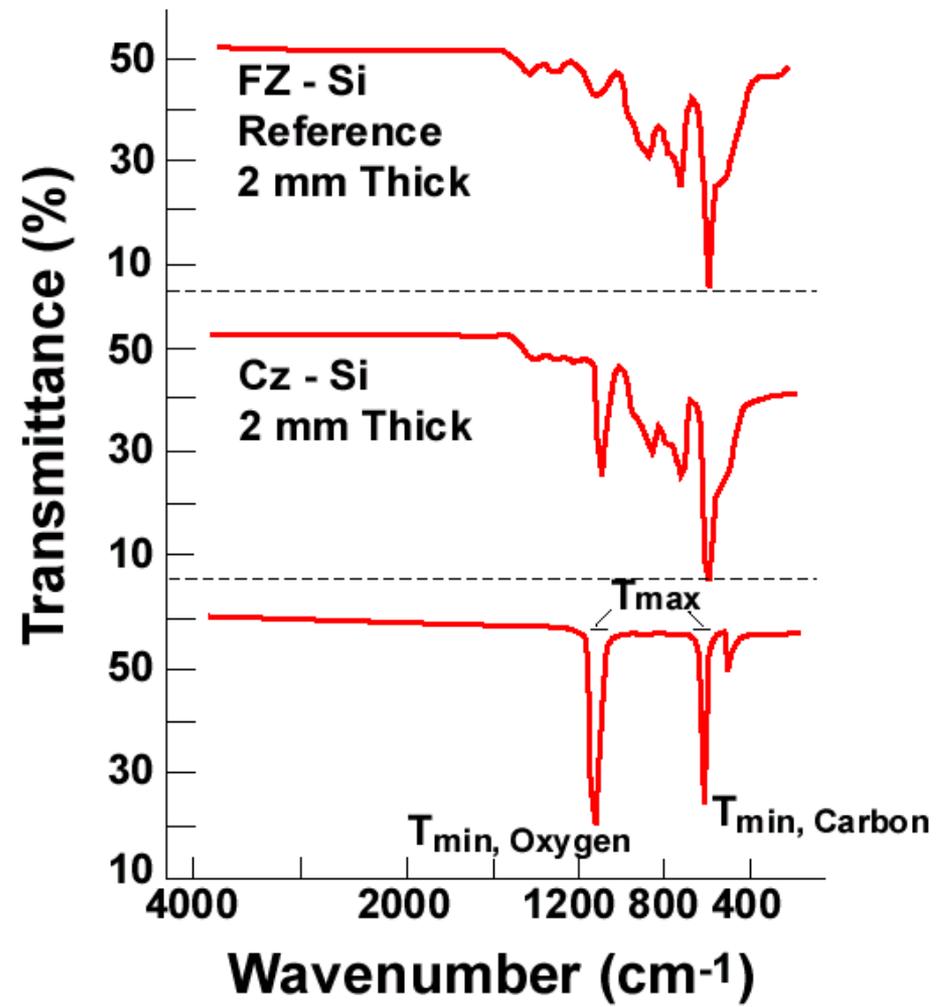
Interferogram - Spectrum





FTIR Applications

- Determine oxygen and carbon density by transmission dip



Reflection

- Reflection measurements

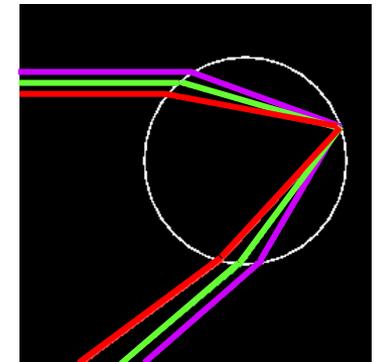
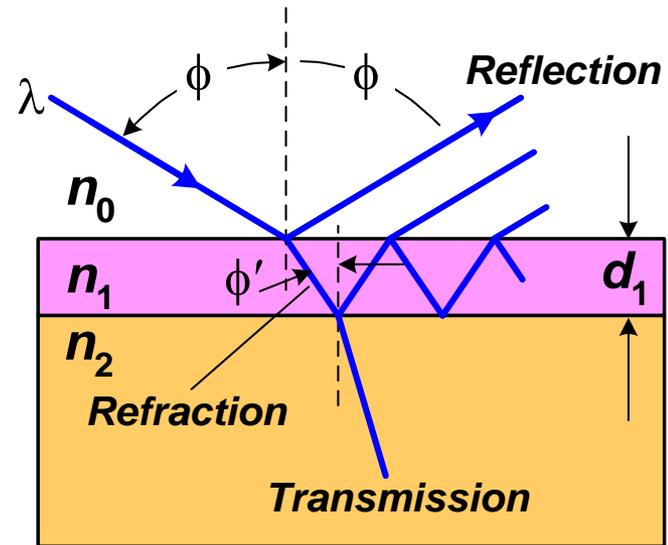
- Film thickness
- Reflectivity

$$R = \frac{r_1^2 e^{\alpha d_1} + r_2^2 e^{-\alpha d_1} + 2r_1 r_2 \cos \phi_1}{e^{\alpha d_1} + r_1^2 r_2^2 e^{-\alpha d_1} + 2r_1 r_2 \cos \phi_1}$$

$$r_1 = \frac{n_0 - n_1}{n_0 + n_1}; r_2 = \frac{n_1 - n_2}{n_1 + n_2}$$

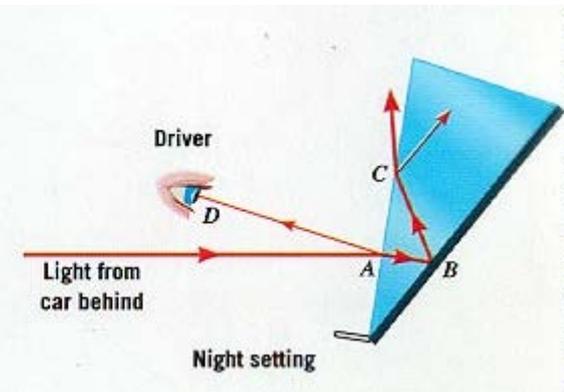
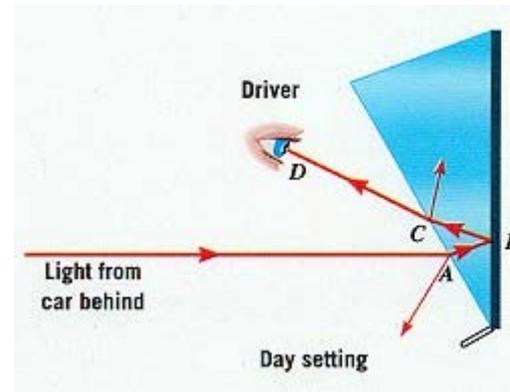
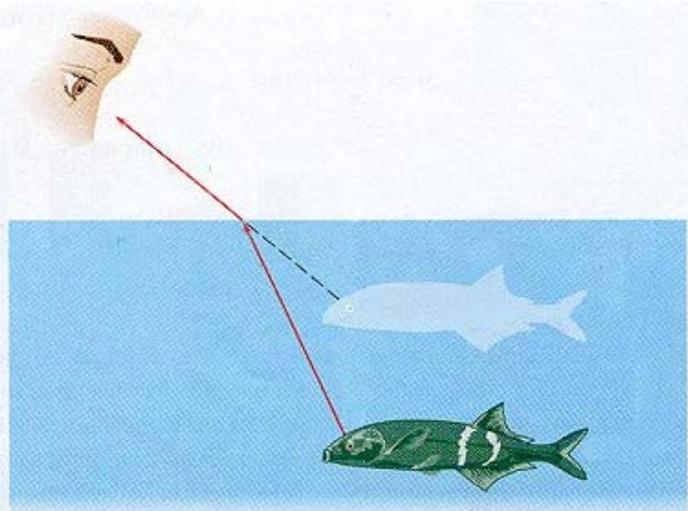
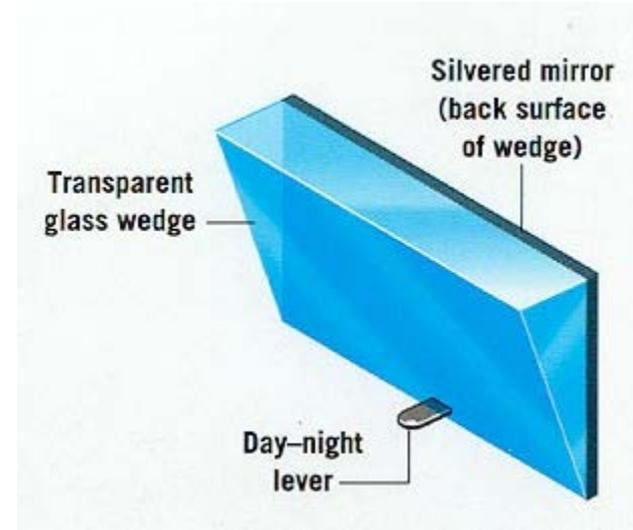
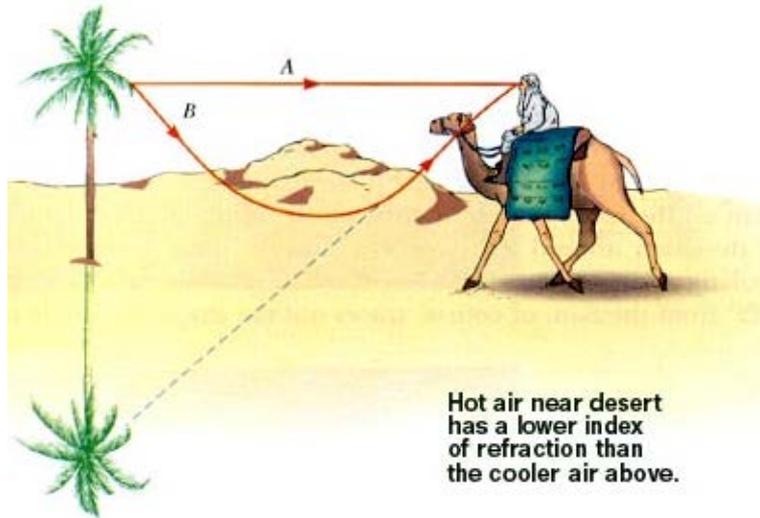
$$\phi_1 = \frac{4\pi n_1 d_1 \cos \phi'}{\lambda}$$

$$\phi' = \sin^{-1} \left[\frac{n_0 \sin \phi}{n_1} \right]$$



Reflection Examples

Rearview Mirror

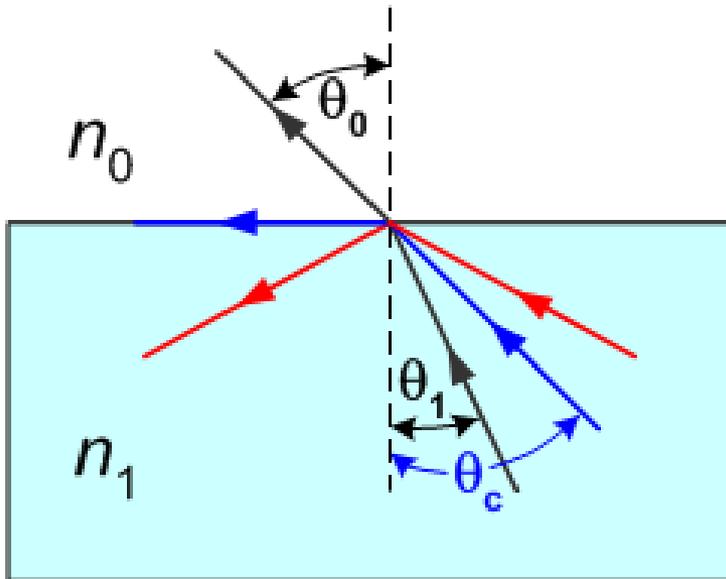


<http://sol.sci.uop.edu/~jfalward/refraction/refraction.html>



Total Internal Reflection

- Snell's law: $n_0 \sin \theta_0 = n_1 \sin \theta_1$
- For $\theta_1 = \theta_c = \sin^{-1}(n_0/n_1)$ (critical angle) $\Rightarrow \theta_0 = 90^\circ$
 - ◆ Total internal reflection





Reflection

- R versus λ yields plots with *unequal* wavelength spacings
- R versus $1/\lambda$ (wavenumber) gives *equal* spacings

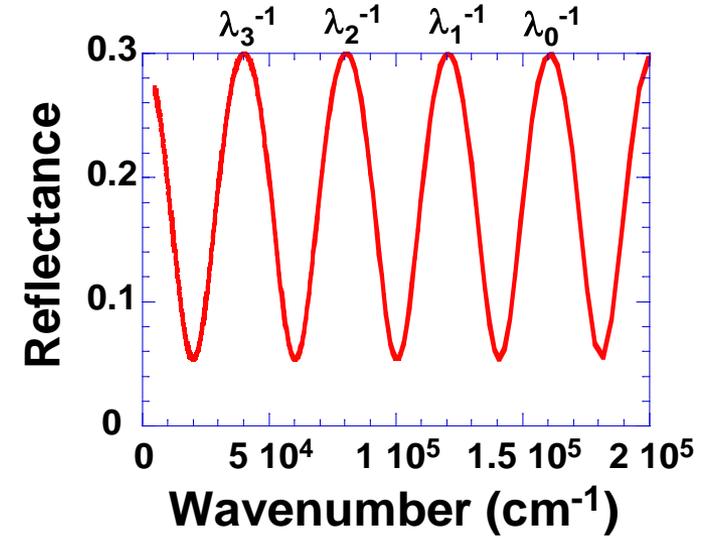
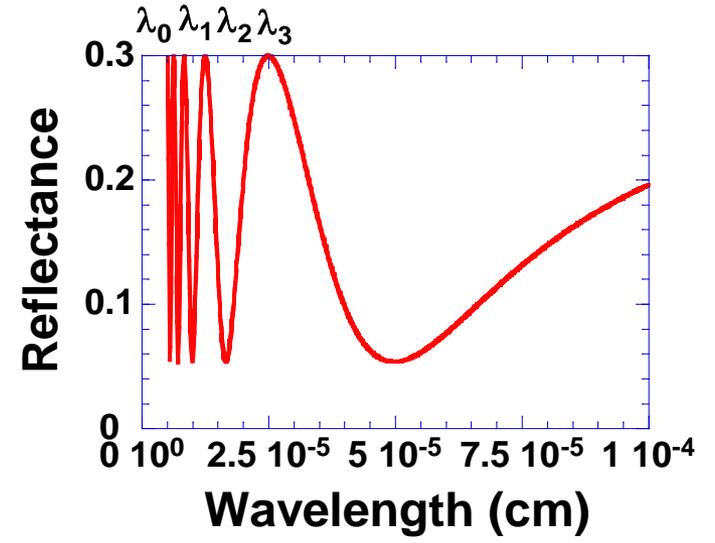
$$\lambda(\text{max}) = \frac{2n_1 d_1 \cos \phi'}{m}$$

$$m = 1, 2, 3 \dots$$

$$d_1 = \frac{i \lambda_0 \lambda_i}{2n_1 (\lambda_i - \lambda_0) \cos \phi'}$$

$$= \frac{i}{2n_1 (1/\lambda_0 - 1/\lambda_i) \cos \phi'}$$

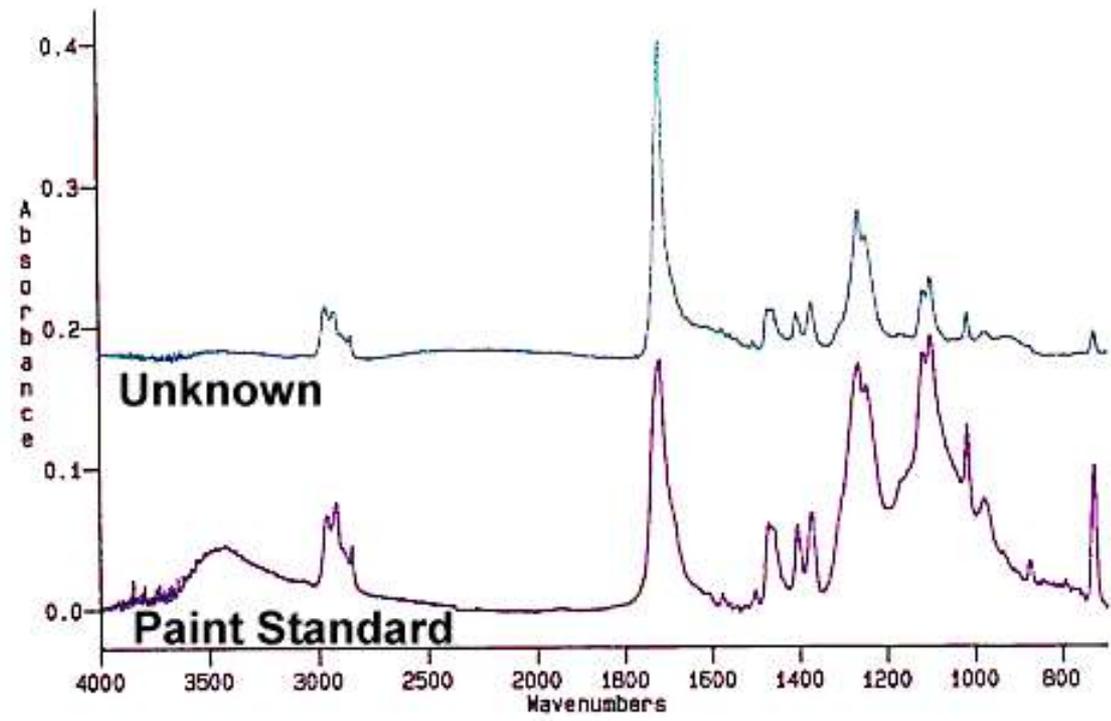
i : number of complete cycles from λ_0 to λ_i





Reflection FTIR Applications

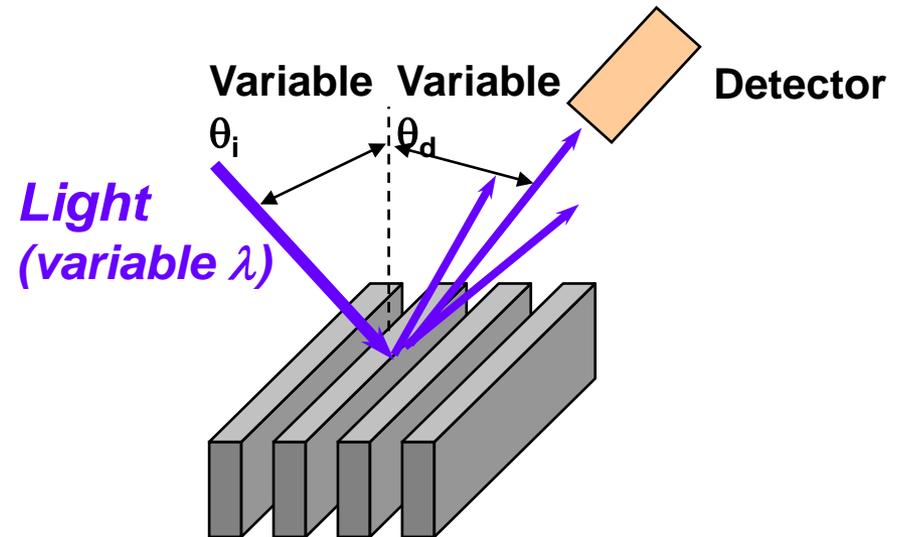
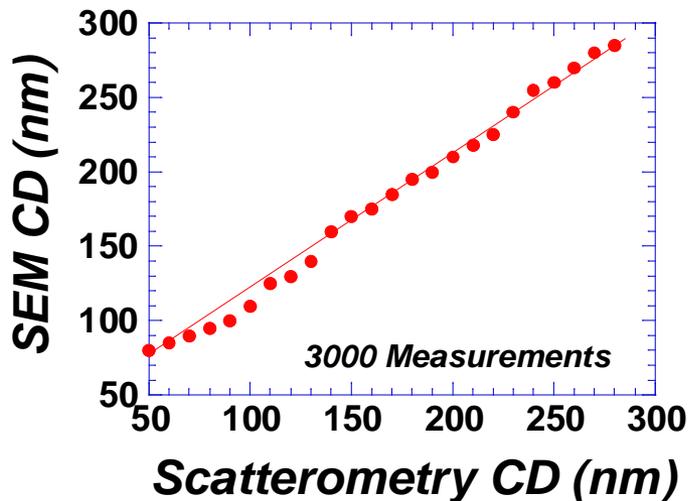
- FTIR is used in many solid state and chemical applications



www.mee-inc.com/ftir.html#analytical

Line Width

- Scatterometry uses scattered or diffracted light
- From diffracted signature can determine
 - ◆ Line height
 - ◆ Line width
 - ◆ Corner rounding
 - ◆ Sidewall slope/angle
- **Special test structure**



C.J. Raymond in *Handbook of Si Semiconductor Metrology* (A.C. Diebold, ed.) Marcel Dekker, 2001.



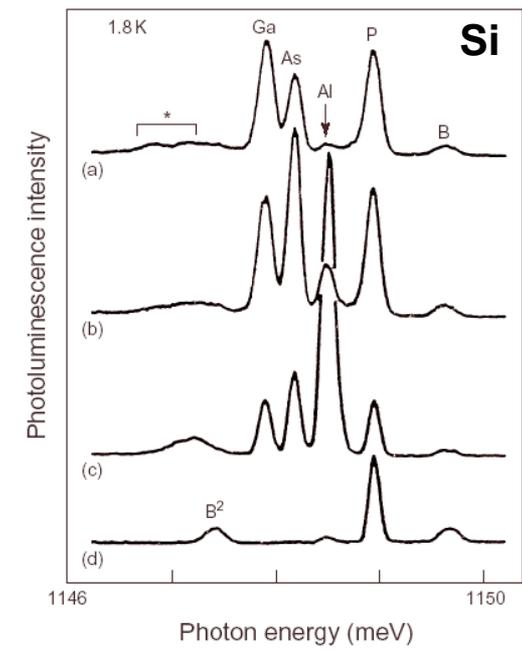
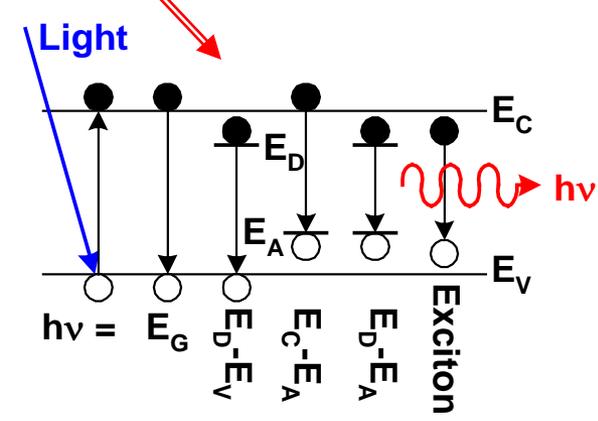
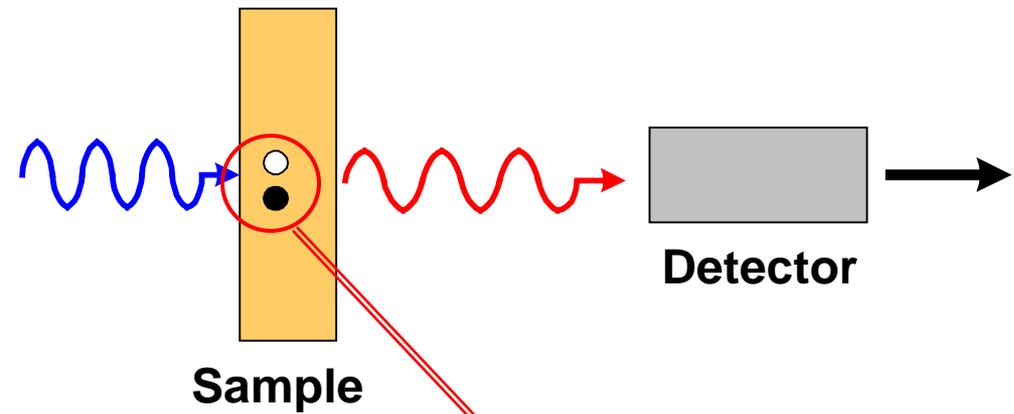
Luminescence

Luminescence is the emission of light due to:

- **Incandescence: energy supplied by heat**
- **Photoluminescence: energy supplied by light**
- **Fluorescence: energy supplied by ultraviolet light**
- **Chemiluminescence: energy supplied by chemical reactions**
- **Bioluminescence: energy supplied by chemical reactions in living beings**
- **Electroluminescence: energy supplied by electric current/voltage**
- **Cathodoluminescence: energy supplied by electron beams.**
- **Radioluminescence: energy supplied by nuclear radiation**
- **Phosphorescence: delayed luminescence or "afterglow"**
- **Triboluminescence: energy supplied by mechanical action**
- **Thermoluminescence: energy supplied by heat**

Photoluminescence

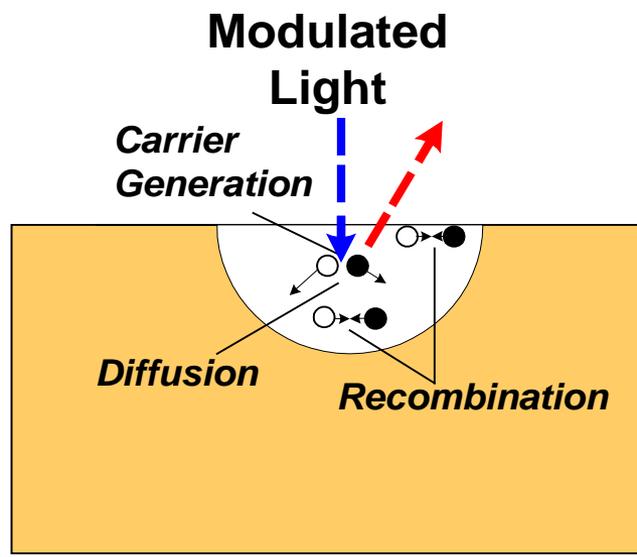
- Incident laser creates electron-hole pairs (ehp)
- When the ehp recombine, they emit light



How Does PL Work And How Can It Be Used?

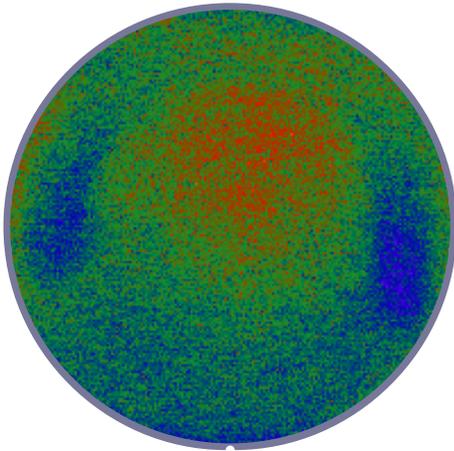
- Carrier generation depth
 - Wavelength \Rightarrow **depth information**
- Recombination
 - Shockley-Read-Hall (impurities) \Rightarrow **impurity information**
 - Auger (high carrier densities) \Rightarrow **doping density information**
 - Surface (surface states, impurities) \Rightarrow **surface information**
 - Radiative (light emission) \Rightarrow **detection mechanism**

This is what we want!



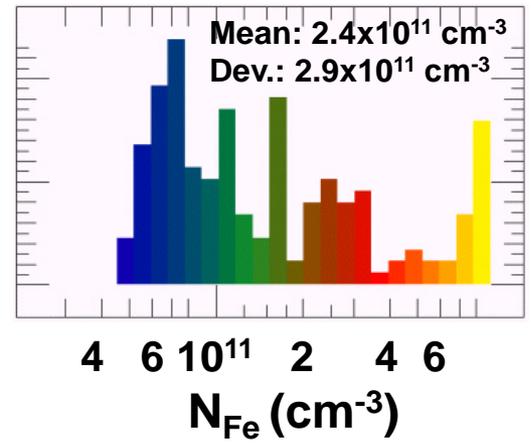
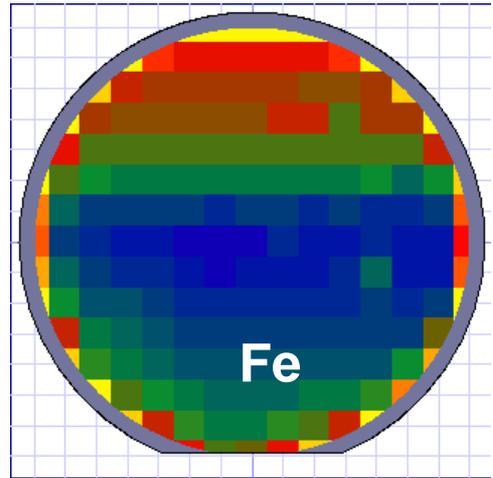
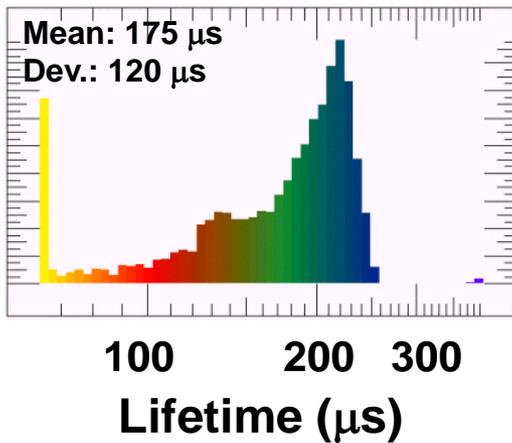
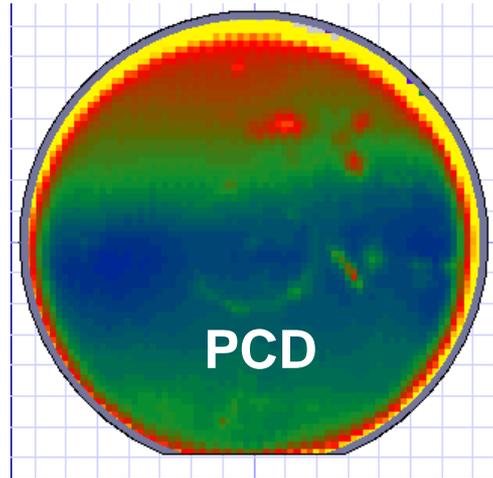
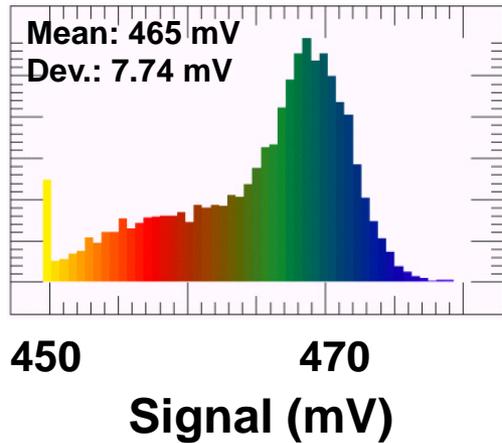
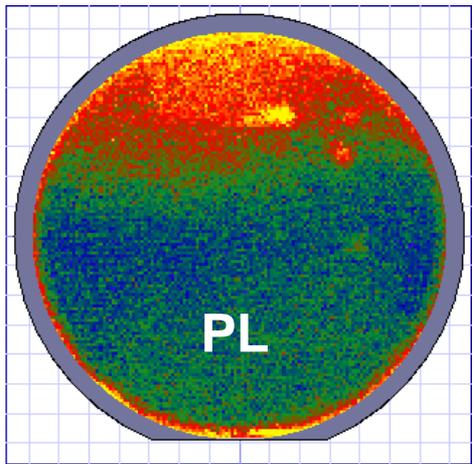


Depth Dependent PL Signals





Iron In Si by PL And PCD





Review Questions

- What determines the resolution limit in conventional optical microscopy?
- What is near field optical microscopy?
- What are the basic elements of ellipsometry?
- How does FTIR work?
- Where are transmission measurements used?
- Where are reflection measurements used?
- What is luminescence?
- How can photoluminescence be used in Si characterization?