



ECE 4813

Semiconductor Device and Material Characterization

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As with all of these lecture slides, I am indebted to Dr. Dieter Schroder from Arizona State University for his generous contributions and freely given resources. Most of (>80%) the figures/slides in this lecture came from Dieter. Some of these figures are copyrighted and can be found within the class text, *Semiconductor Device and Materials Characterization*. **Every serious microelectronics student should have a copy of this book!**



Doping

Plasma Resonance

Free Carrier Absorption

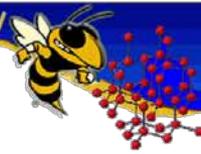
Infrared Spectroscopy

Photoluminescence

Hall Measurements

Magnetoresistance

Time of Flight



Plasma Resonance and Reflectivity Minimum

- *Electron/hole plasmas are ensembles of free carriers that can, at certain frequencies, oscillate in concert as a group.*
- *Such a plasma resonance exists whose frequency / wavelength ($\nu=c/\lambda$) is determined by the free carrier density.*

$$\lambda_{plasma} = \frac{2\pi c}{q} \sqrt{\frac{K_s \epsilon_0 m^*}{n}}$$

- *Good for p (or n) $> \sim 10^{18} \text{ cm}^{-3}$*
- *Since plasma resonances are hard to detect in practice, most of the time, free carrier densities are determined by empirical reflectivity minimums...*

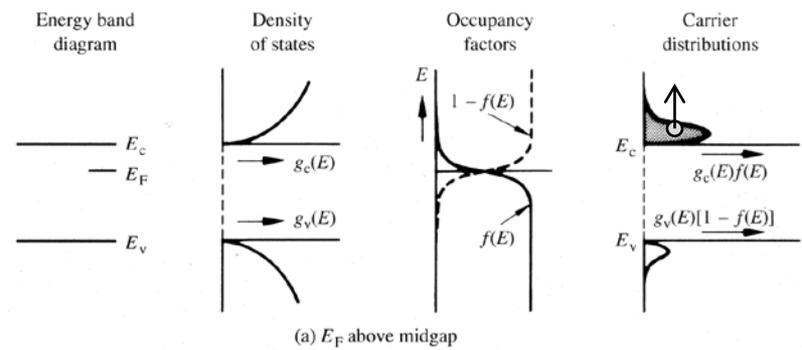
$$n = (A\lambda_{plasma} + B)^c$$

- *... or free carrier absorption*

Free Carrier Absorption

- **Free carrier absorption occurs within the conduction or valance band (not between).**
 - ◆ **For example a conduction electron is absorbs an IR photon and is promoted into a higher energy state still inside the conduction band**

$$\alpha_{fc} = \frac{q^3 \lambda^2 p}{4\pi^2 \epsilon_0 c^3 n (m^*)^2 \mu_p}$$



- **In practice, empirical fitting is used**

$$\alpha_{fc} = A \lambda^2 p$$

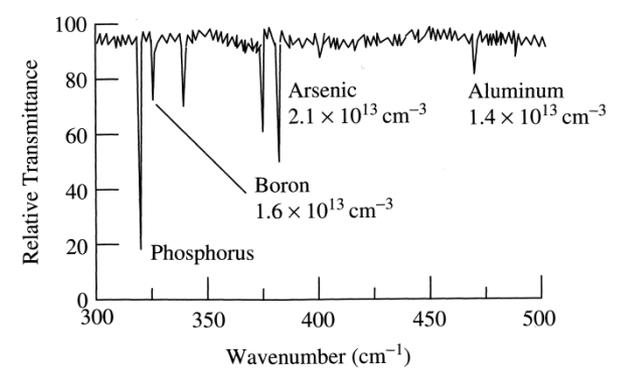
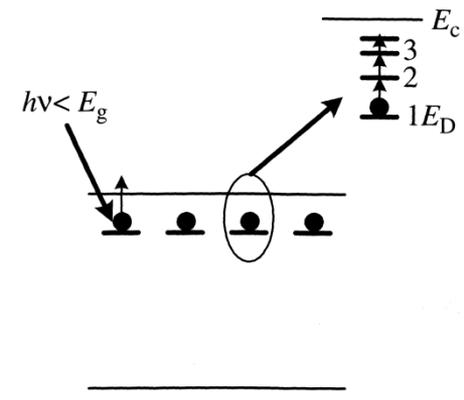
- **Generally measured using Fourier Transmission Infrared (FTIR) Spectrometer**
- **Good for p (or n) $> \sim 10^{17} \text{ cm}^{-3}$**



Infrared Spectroscopy

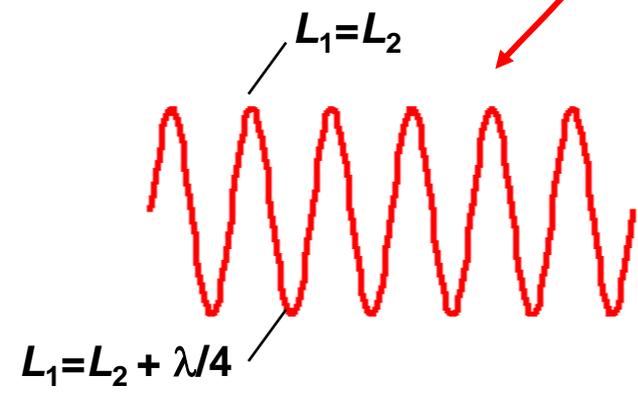
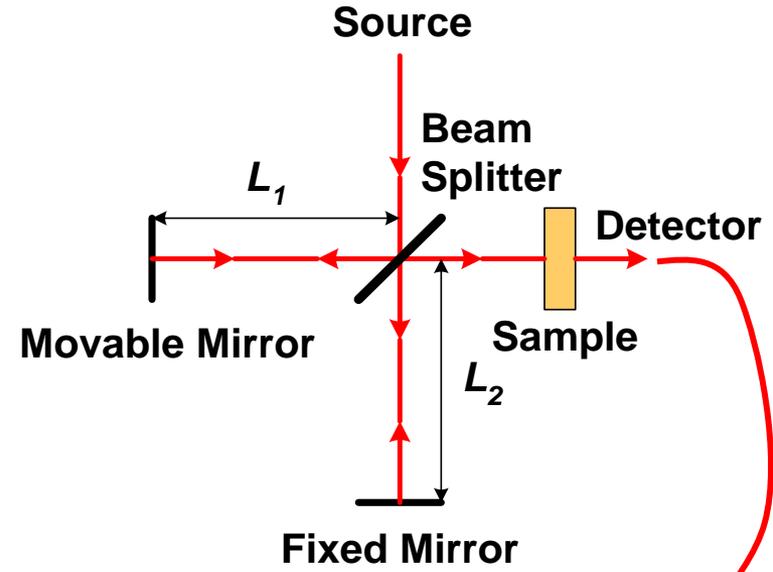
- **Measures dopant concentrations (low temperature) and can be used at room temperature to measure free carrier absorption.**
- **Cryogenic temperatures are used to freeze carriers into their dopant ground state**
- **IR (very small energy) light is used to excite electrons/holes into their dopant “excited state” creating sharp absorption lines**
- **Absorption line intensity is calibrated to dopant density**

- **Good for N_A (or N_D) $> \sim 10^{11} \text{ cm}^{-3}$**



Interferometer

- Let source be $\cos 2\pi f x$
 - ◆ f : frequency of light
 - ◆ x : movable mirror location
- $L_1 = L_2$
 - ◆ Constructive interference
 - ◆ Maximum detector output
- $L_1 = L_2 + \lambda/4$
 - ◆ Destructive interference
 - ◆ Zero detector output





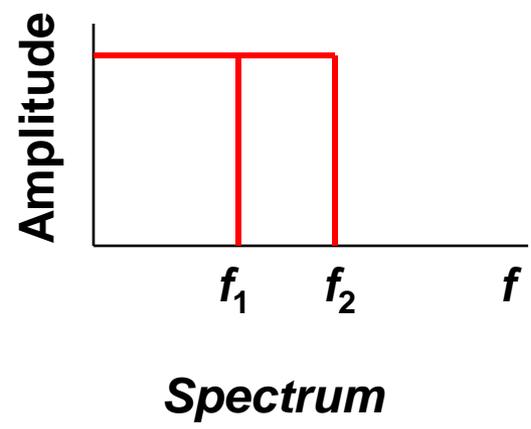
Fourier Transform Infrared Spectroscopy

- Fourier transform infrared spectroscopy (FTIR)

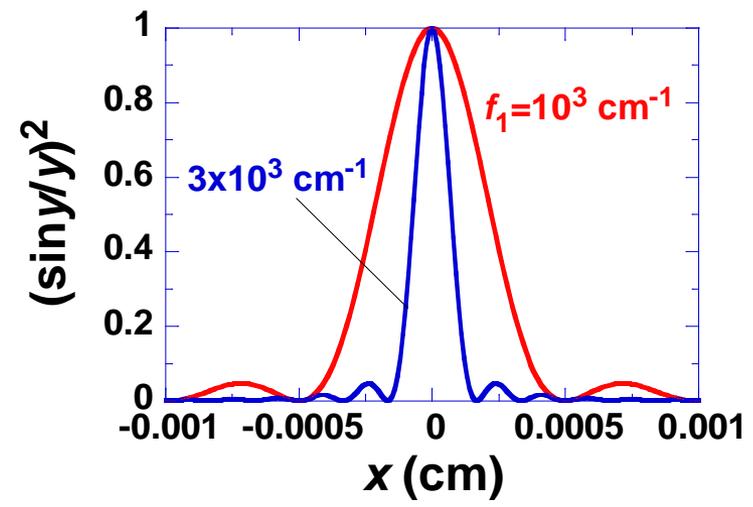
$$I(x) = B(f)[1 + \cos 2\pi xf] \quad I(x) = \int_0^f B(f)[1 + \cos 2\pi xf] df$$

$$I(x) = \int_0^{f_1} A \cos 2\pi xf df = Af_1 \frac{\sin 2\pi xf_1}{2\pi xf_1}$$

$$B(f) = \int_{-\infty}^{\infty} I(x) \cos 2\pi xf dx$$



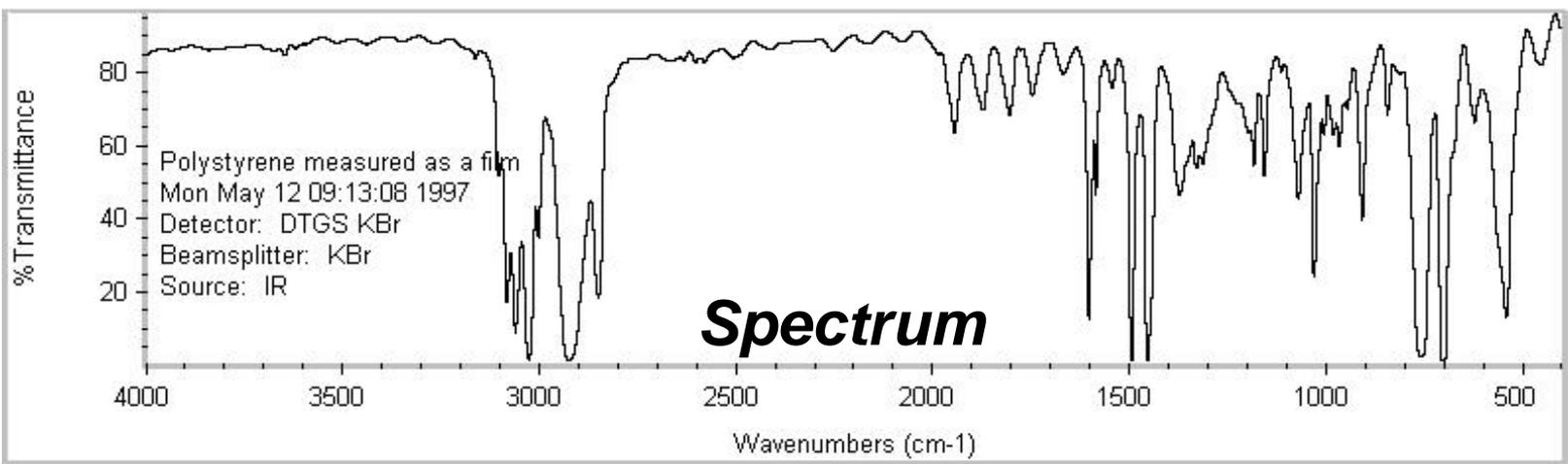
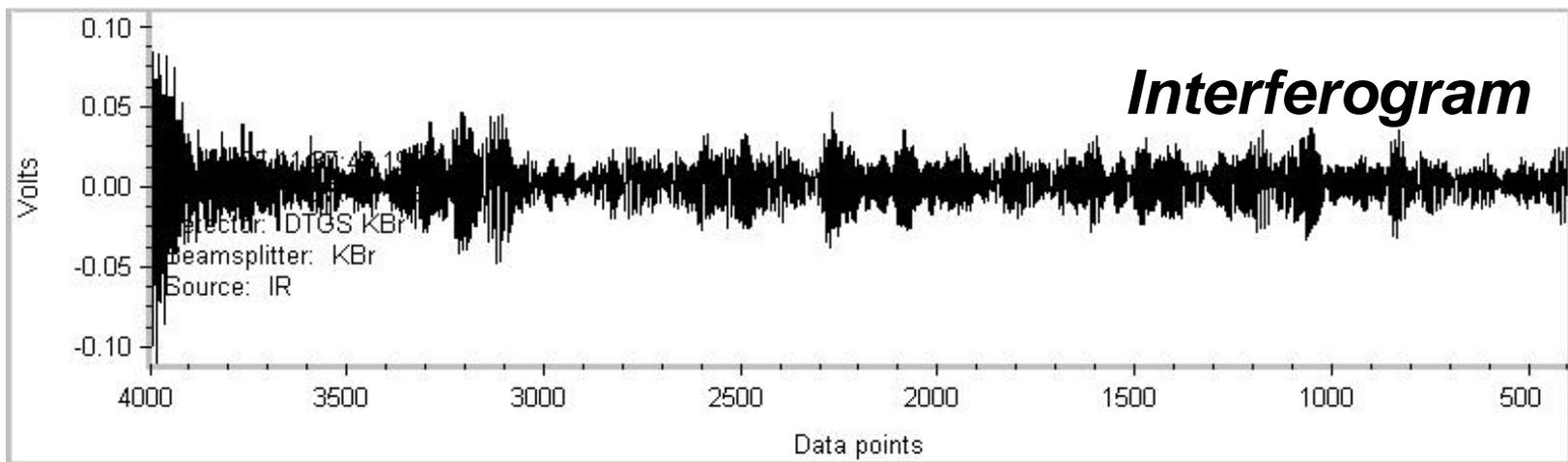
Spectrum



Interferogram

In a Fourier spectrum, frequency bandwidth determines resolution.

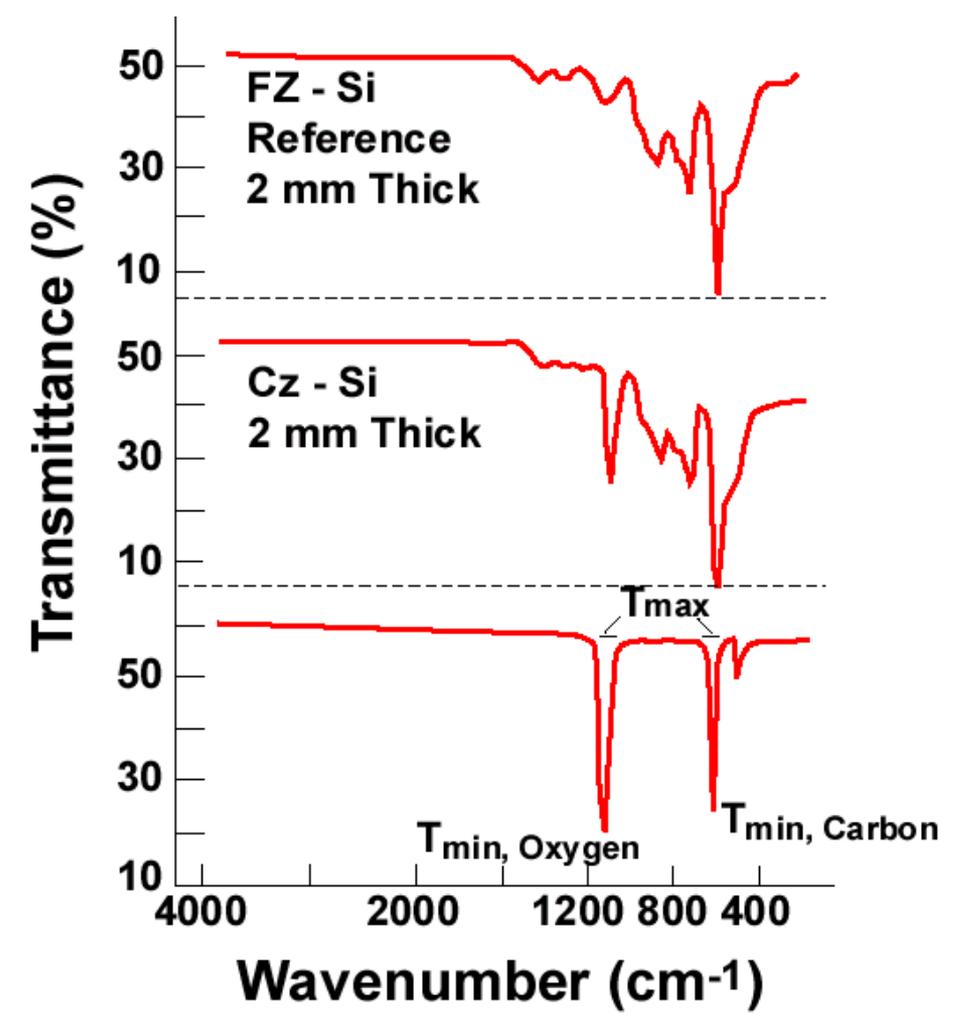
Interferogram - Spectrum





FTIR Applications

- Determine oxygen and carbon density by transmission dip





Mobilities

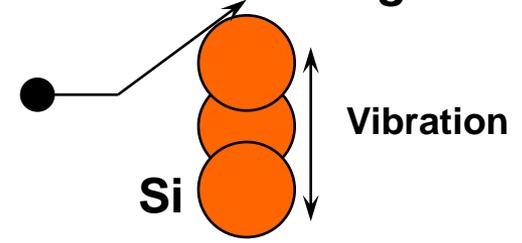
- **Conductivity Mobility:** $\mu_p = 1/q\rho$
 - ◆ Majority carrier mobility; need carrier concentration and resistivity
- **Drift Mobility:** $\mu_p = v_d/\varepsilon$
 - ◆ Minority carrier mobility
 - ◆ Need drift velocity and electric field (Haynes-Shockley experiment)
- **Hall Mobility:** $\mu_H = R_H/\rho$
 - ◆ Need Hall measurement
 - ◆ Hall mobility does not necessarily equal conductivity mobility
- **MOSFET Mobility:**
 - ◆ MOSFET mobility lowest, carriers are scattered at the Si-SiO₂ interface
 - ◆ Interface is microscopically rough



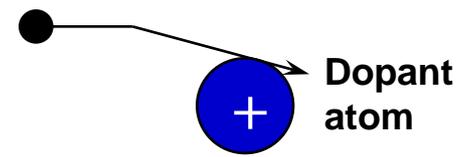
Mobility

- **Electron/hole mobility is a measure of carrier scattering in the semiconductor**
 - ◆ **Lattice scattering**
 - Silicon atoms
 - ◆ **Ionized impurity scattering**
 - Dopant atoms
 - ◆ **Interface scattering**
 - Surface roughness at SiO₂/Si interface
 - Polar scattering

Lattice Scattering:



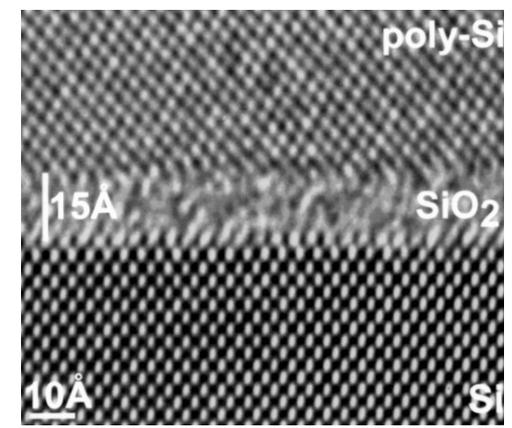
Ionized Impurity Scattering:



- **Silicon bulk**

- ◆ $\mu_n \approx 3 \mu_p$
- ◆ **MOSFET mobility (effective mobility) ≈ 0.3 bulk mobility**

$$\frac{1}{\mu} = \frac{1}{\mu_l} + \frac{1}{\mu_i} + \frac{1}{\mu_s}$$



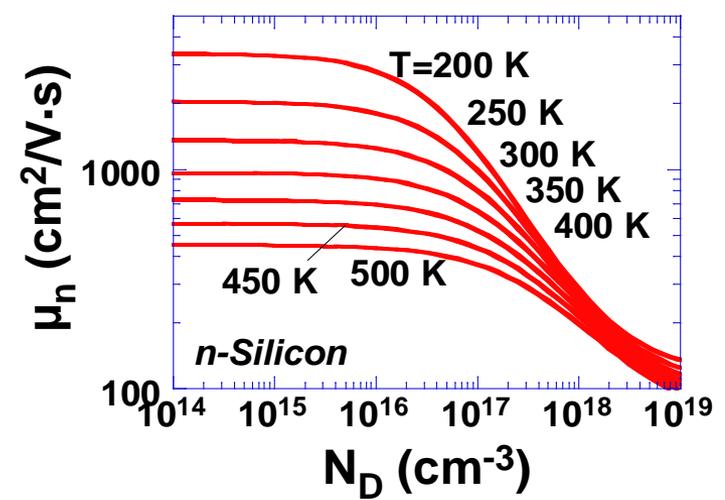
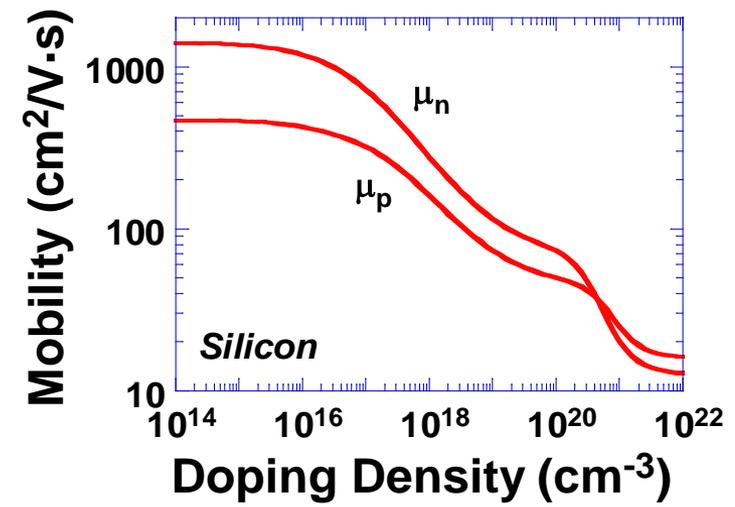
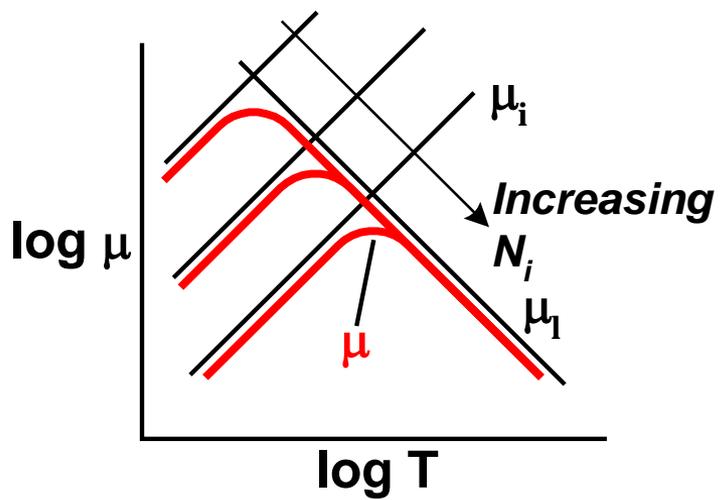
Courtesy of M.A. Gribelyuk, IBM.



Mobilities

- For bulk semiconductors, lattice and ionized impurity scattering dominate the mobility

$$\mu_l = T^{-1.5}; \mu_i = \frac{T^{1.5}}{N_i}$$





“Simple” Hall Effect

- Hall effect is commonly used during the development of new semiconductor material

- Resistivity, carrier concentration AND mobility can all be determined simultaneously

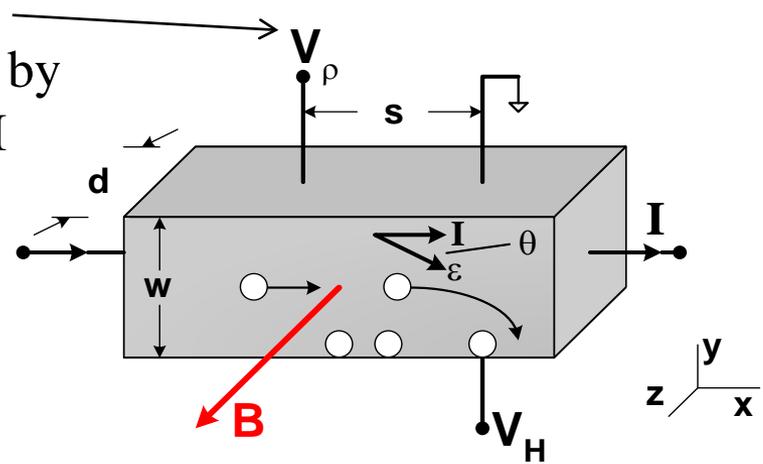
- Lorentz Force – deflection of free carriers by an applied magnetic field

- Temperature dependent Hall is very powerful and can elucidate scattering mechanisms (plotting mobility vs T^a), and determine dopant activation energies
 - ◆ Compensated Dopant Freeze out regime – Arrhenius slope results in E_A
 - ◆ Uncompensated Dopant Freeze out regime – Arrhenius slope results in $E_A/2$
 - ◆ At moderate temperatures, $p \sim (N_A - N_D)$
 - ◆ At elevated temperatures, $p \sim n_i$



“Simple” Hall Effect

Voltage induced by current I



Lorentz Force

$$\vec{F} = q(\vec{\varepsilon} + \vec{v} \times \vec{B})$$

$$I = qA p v_x = q w d p v_x$$

In steady state, the magnetic force is balanced by the induced electric field

$$\varepsilon_y = B v_x = \frac{B I}{q w d p}$$

Hall voltage

$$\int_0^{V_H} dV = V_H = - \int_w^0 \varepsilon_y dy = - \int_w^0 \frac{B I}{q w d p} dy = \frac{B I}{q d p}$$

$$R_H = \frac{dV_H}{B I}$$

Hall coefficient [m^3/C or cm^3/C]



“Simple” Hall Effect

- Resistivity is simply found from the voltage drop along the length (no magnetic field),

$$\rho = \frac{dV}{s} \frac{V}{I}$$

- Carrier density $p = \frac{r}{qR_H}$; $n = -\frac{r}{qR_H}$

($r \sim 1 - 2$, Hall scattering factor)

- Mobility

$$p = \frac{r}{qR_H}$$

$$q\mu_p p = \sigma = \frac{r\mu_p}{R_H} = \frac{\mu_H}{R_H}$$

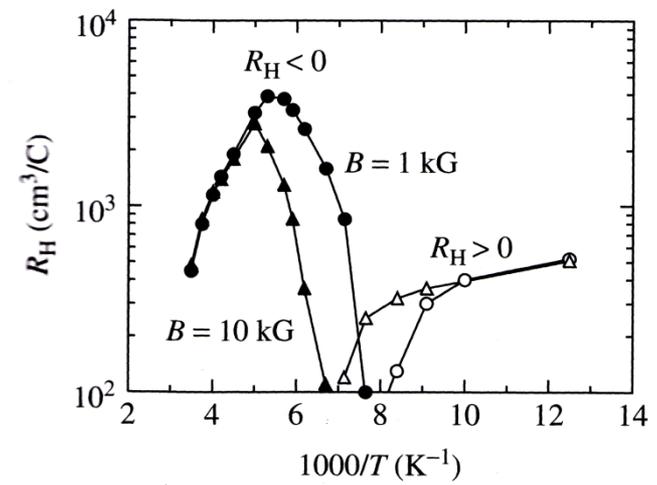
$$\mu_H = |\sigma R_H| = r\mu_p$$



Detailed Hall Effect

- The Hall Coefficient for both electrons and holes present in the same material is in general:

$$R_H = r \left(\frac{\left(p - \left(\frac{\mu_n}{\mu_p} \right)^2 n \right) + (\mu_n B)^2 (p - n)}{q \left[\left(p + \left(\frac{\mu_n}{\mu_p} \right) n \right)^2 + (\mu_n B)^2 (p - n)^2 \right]} \right)$$





Detailed Hall Effect

- The Hall Coefficient is in general:

$$R_H = r \frac{\left(p - \left(\frac{\mu_n}{\mu_p} \right)^2 n \right) + (\mu_n B)^2 (p - n)}{q \left[\left(p + \left(\frac{\mu_n}{\mu_p} \right) n \right)^2 + (\mu_n B)^2 (p - n)^2 \right]}$$

- At low fields ($B \ll 1/\mu_n$)...

$$R_H = \frac{r \left(p - \left(\frac{\mu_n}{\mu_p} \right)^2 n \right)}{q \left(p + \left(\frac{\mu_n}{\mu_p} \right) n \right)^2} \approx \frac{r}{qp} \quad \text{or} \quad -\frac{r}{qn}$$

$$r = \frac{\langle \tau^2 \rangle}{\langle \tau \rangle^2} \quad \text{where } \tau \text{ is the mean time between collisions}$$

- And at high fields ($B \gg 1/\mu_n$)...

$$R_H = \frac{r}{q(p - n)}$$



Two Layer Hall Effect

- Sometimes, a semiconductor has two different conduction layers (surface inversion, fermi-level pinning, substrate layers, n-p junctions or p+/n or n+/n layers)
- The Hall coefficient is then a weighted sum of both layers and can be either positive or negative leading to confusion (shown for the low B field limit):

$$R_H = R_{H1} \left(\frac{t_1}{t_{total}} \right) \left(\frac{\sigma_1}{\sigma} \right)^2 + R_{H2} \left(\frac{t_2}{t_{total}} \right) \left(\frac{\sigma_2}{\sigma} \right)^2$$

where $\sigma = \left(\frac{t_1}{t_{total}} \right) \sigma_1 + \left(\frac{t_2}{t_{total}} \right) \sigma_2$

and $t_{total} = t_1 + t_2$



Two Layer Hall Effect (more detail)

- The Hall coefficient is then a weighted sum of both layers and can be either positive or negative leading to confusion:

$$R_H = \left(\frac{t_{total} \left[(R_{H1} \sigma_1^2 t_1 + R_{H2} \sigma_2^2 t_2) + R_{H1} \sigma_1 R_{H2} \sigma_2^2 (R_{H1} t_2 + R_{H2} t_1) B^2 \right]}{(\sigma_1 t_1 + \sigma_2 t_2)^2 + \sigma_1^2 \sigma_2^2 (R_{H1} t_2 + R_{H2} t_1) B^2} \right)$$

Low B
Field

High B
Field

$$R_H = R_{H1} \left(\frac{t_1}{t_{total}} \right) \left(\frac{\sigma_1}{\sigma} \right)^2 + R_{H2} \left(\frac{t_2}{t_{total}} \right) \left(\frac{\sigma_2}{\sigma} \right)^2$$

$$R_H = \left(\frac{R_{H1} R_{H2} t_{total}}{R_{H1} t_2 + R_{H2} t_1} \right)$$

where $\sigma = \left(\frac{t_1}{t_{total}} \right) \sigma_1 + \left(\frac{t_2}{t_{total}} \right) \sigma_2$

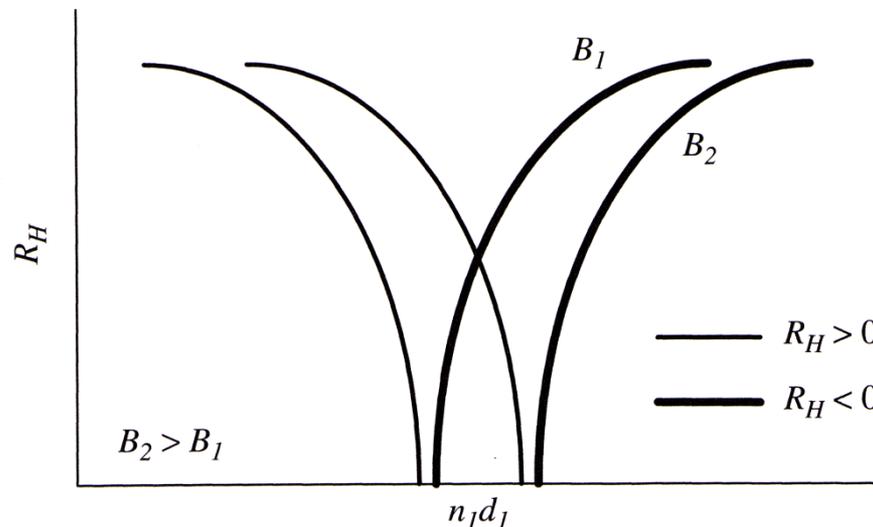
and $t_{total} = t_1 + t_2$



Two Layer Hall Effect (more detail)

- The Hall coefficient is then a weighted sum of both layers and can be either positive or negative leading to confusion (generally):

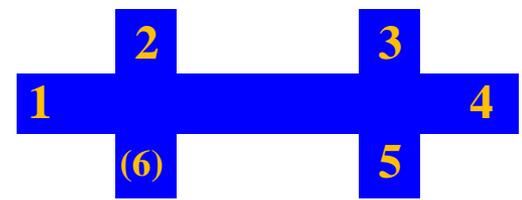
$$R_H = \left(\frac{t_{total} \left[(R_{H1} \sigma_1^2 t_1 + R_{H2} \sigma_2^2 t_2) + R_{H1} \sigma_1 R_{H2} \sigma_2 (R_{H1} t_2 + R_{H2} t_1) B^2 \right]}{(\sigma_1 t_1 + \sigma_2 t_2)^2 + \sigma_1 \sigma_2 (R_{H1} t_2 + R_{H2} t_1) B^2} \right)$$



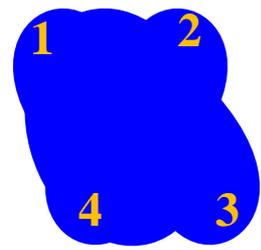


Hall Effect Measurements

- Two approaches:
 - ◆ Hall Bar (5 or 6 contacts)

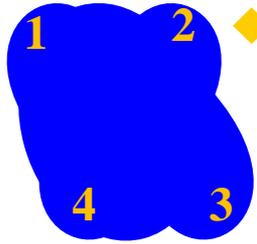


- ◆ Van der Pauw configuration
 - Based on Conformal mapping theory
 - Contacts assumed point sources
 - Uniform thickness
 - Cannot contain isolated (interior) holes





Hall Effect Measurements



◆ Van der Pauw configuration

● Measure resistivity first by “perimeter measurements”...

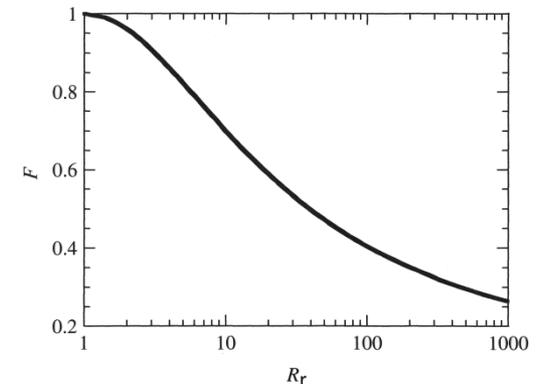
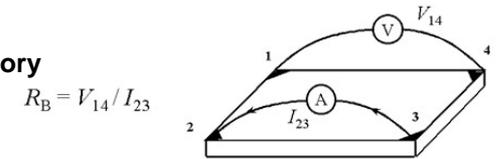
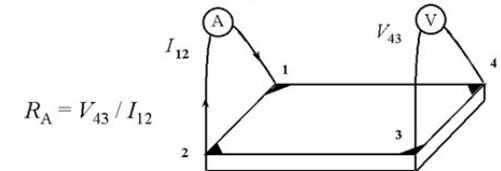
- ◆ Example: determine $R_{12,34}$ where current goes in 1 and leaves 2 and voltage is measured between terminals 3 and 4. Next determine $R_{23,14}$ where current goes in 2 and leaves 3 and voltage is measured between terminals 1 and 4.
- ◆ Use:

$$\rho = \left(\frac{\pi t}{\ln(2)} \right) \left(\frac{R_{12,34} + R_{23,14}}{2} \right) F$$

- ◆ ...where F is a symmetry term derived from conformal mapping theory
- ◆ F is determined from:

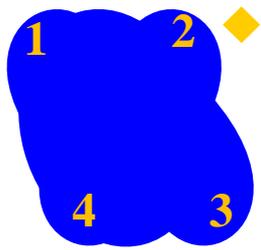
$$\left(\frac{R_r - 1}{R_r + 1} \right) = \frac{F}{\ln(2)} \cosh^{-1} \left(e^{\left(\frac{\ln(2)}{F} \right)} \right)$$

where $R_r = \frac{R_{12,34}}{R_{23,14}}$





Hall Effect Measurements



◆ Van der Pauw configuration

- Now measure the Hall voltage using “Crossing configurations”

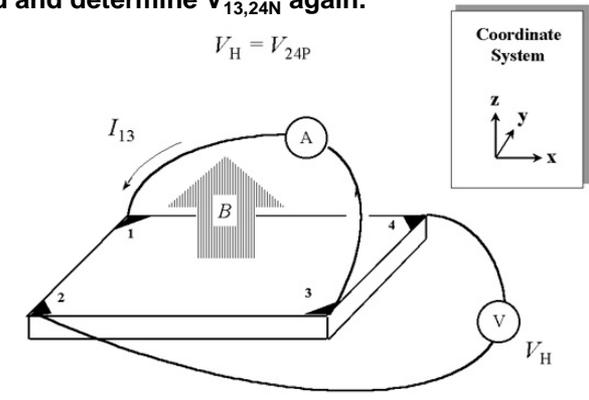
- ◆ Example: Apply the magnetic field and determine $V_{13,24P}$ where current goes in 1 and leaves 3 and voltage is measured between terminals 2 and 4. Next reverse the field and determine $V_{13,24N}$ again.
- ◆ To find the sheet concentration ($\#/cm^2$) use:

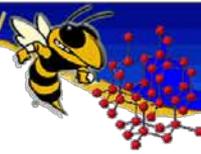
$$\rho \propto \left(\frac{IB}{q(V_{13,24P} + V_{13,24N})} \right)$$

- ◆ ...where we have intentionally left out the proportionality constant
- ◆ In reality, 8 resistivity and eight hall voltage measurements are made to reduce contact related offset voltage errors resulting in an equation that is of the form:

$$\rho = \left(\frac{(8 \times 10^{-8})IB}{q[(V_{13,24P} - V_{13,24N}) + (V_{31,42P} - V_{31,42N}) + (V_{42,13P} - V_{42,13N}) + (V_{24,31P} - V_{24,13N})]} \right)$$

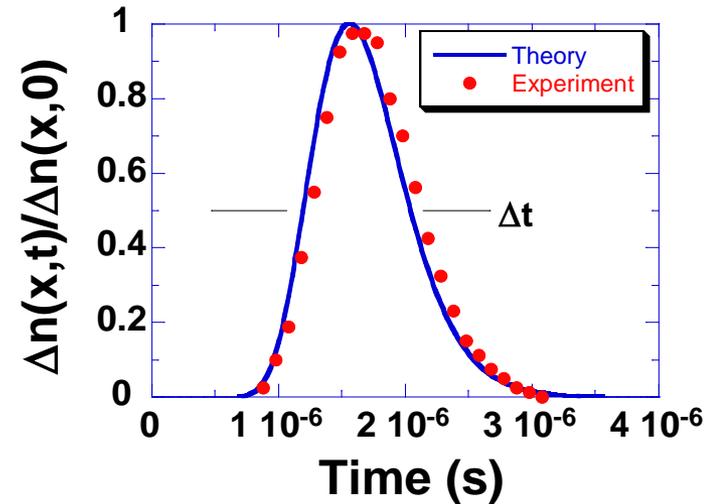
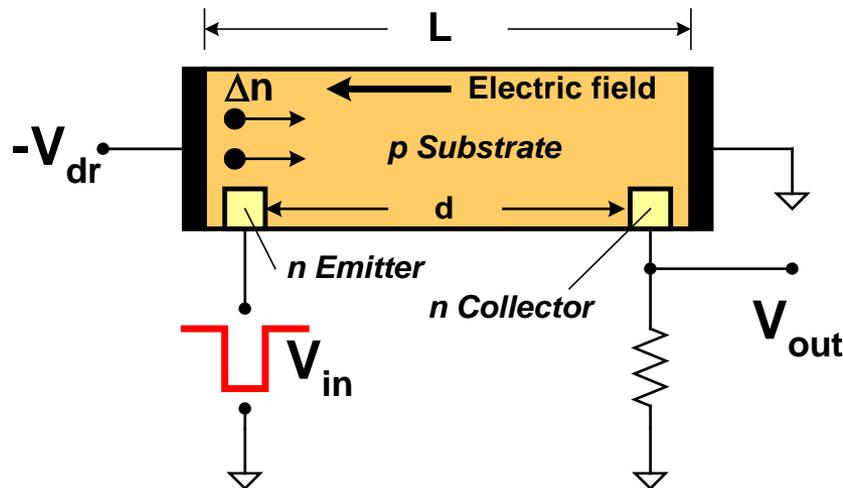
- See text for important sample geometry considerations (if ignored, significant error can result)





Haynes - Shockley Experiment

- Allows *mobility, diffusion constant, and minority carrier lifetime* to be determined

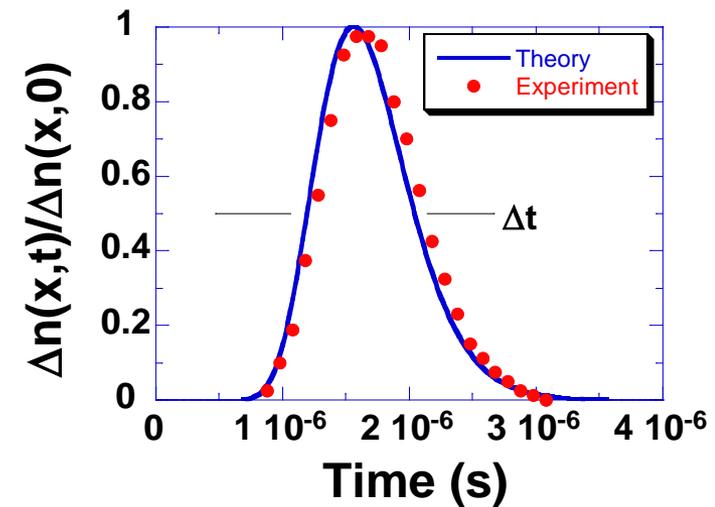
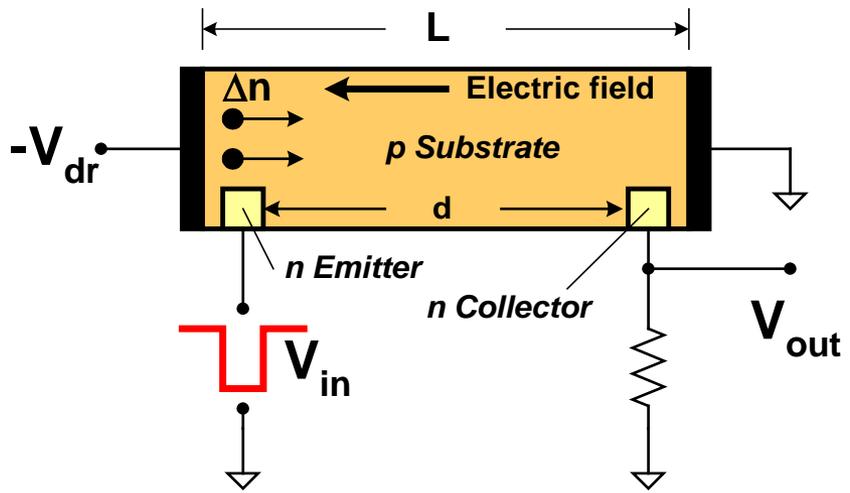


$$\Delta n(x, t) = \frac{N}{\sqrt{4\pi D_n t}} e^{\left(-\frac{(x-vt)^2}{4D_n t} - \frac{t}{\tau_n} \right)}$$



Haynes - Shockley Experiment

- Allows *mobility, diffusion constant, and minority carrier lifetime* to be determined



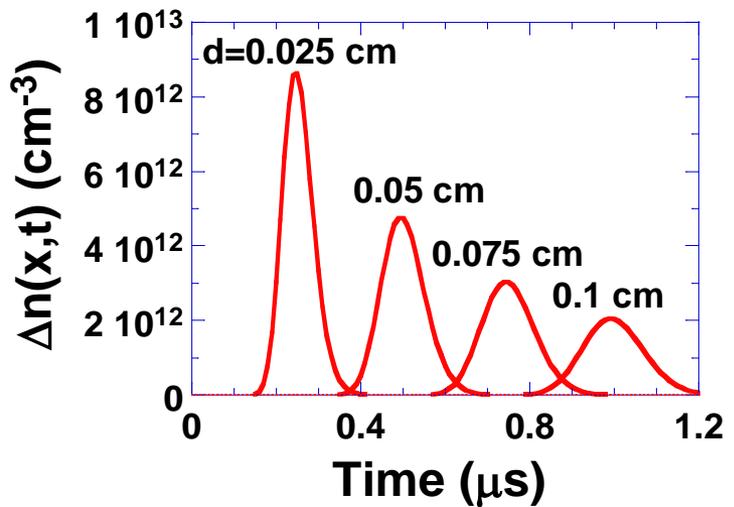
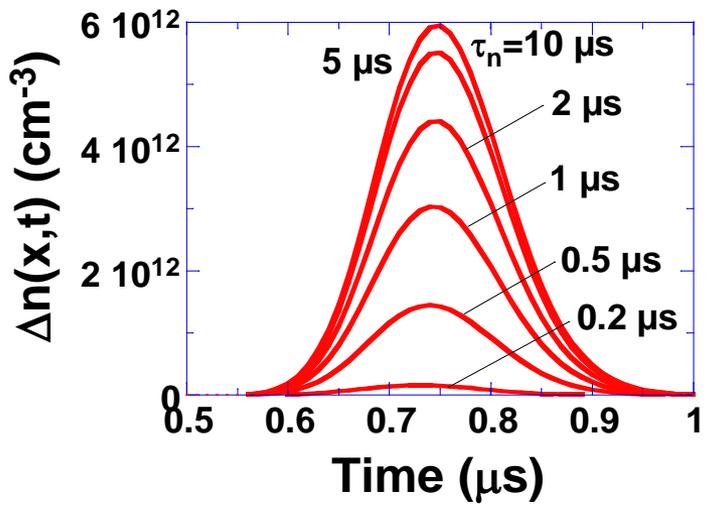
- If at least two lengths and two times are measured, the FWHM of the time plot, Δt can be used to...

$$t_d = d / v_{drift}; \quad \mu_n = \frac{d}{\epsilon t_d}; \quad D_n = \frac{(d\Delta t)^2}{16t_d^3 \ln 2}; \quad \tau_n = \frac{t_{d2} - t_{d1}}{\ln(V_{out1}/V_{out2}) - 0.5 \ln(t_{d2}/t_{d1})}$$



Haynes – Shockley Experiment

$$\Delta n(x,t) = \frac{N}{\sqrt{4\pi D_n t}} \exp\left(-\frac{(x-vt)^2}{4D_n t} - \frac{t}{\tau_n}\right)$$





MOSFET *Effective* Mobility

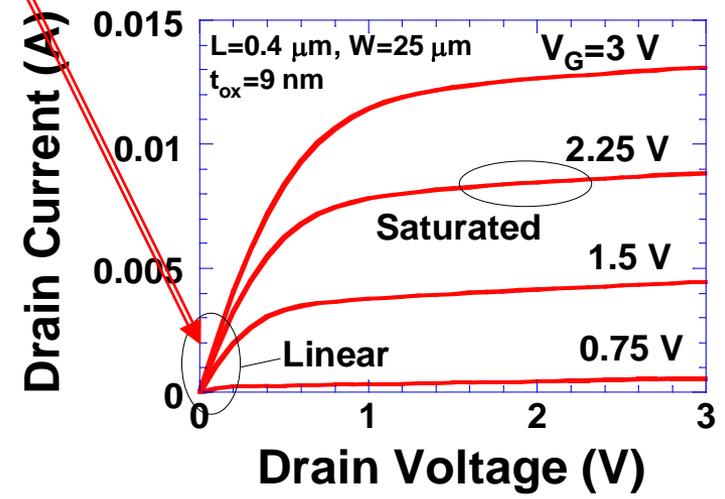
- **Effective mobility** determined from drain current – drain voltage characteristics
- The MOSFET drain current for small V_D (50 - 100 mV) is

$$I_D = (W / L)\mu_{eff} Q_N V_D \approx (W / L)\mu_{eff} C_{ox} (V_G - V_T)V_D$$

- Determine $g_d = \Delta I_D / \Delta V_D$ for low V_D
- Solve for μ_{eff}

$$\mu_{eff} = \frac{Lg_d}{WQ_N} \approx \frac{Lg_d}{WC_{ox}(V_G - V_T)}$$

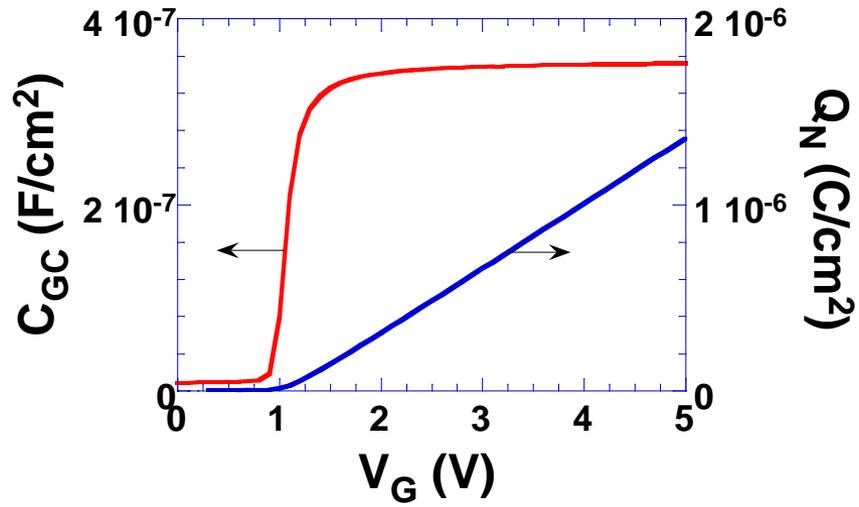
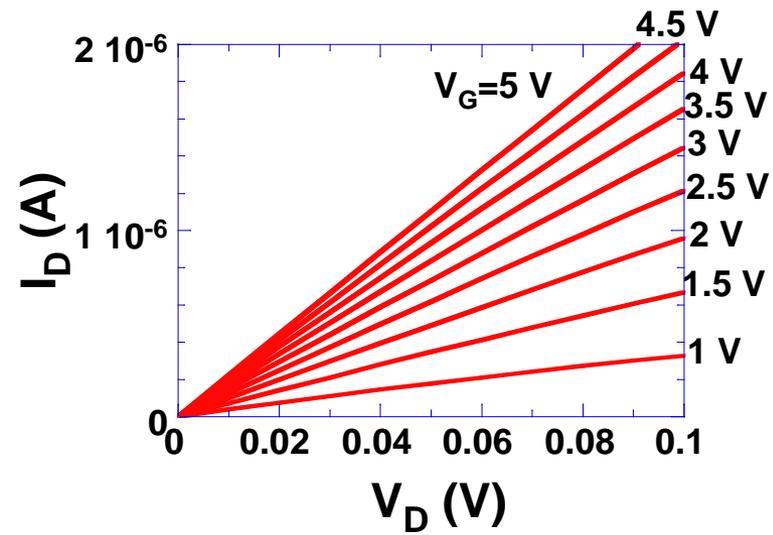
- Need g_d, Q_N, V_T





MOSFET *Effective* Mobility

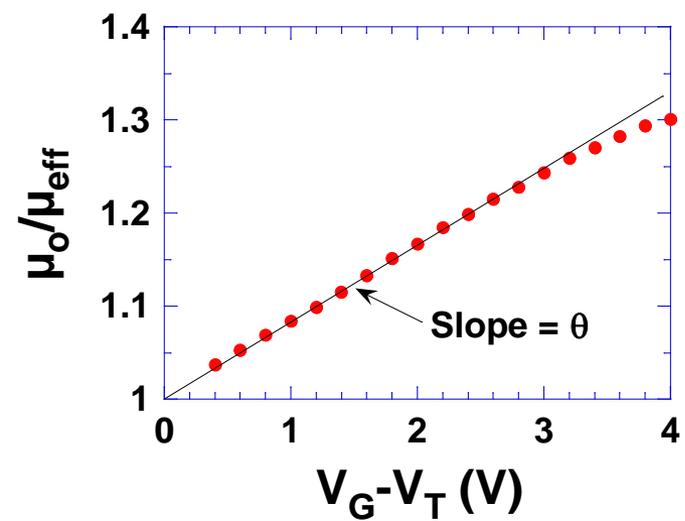
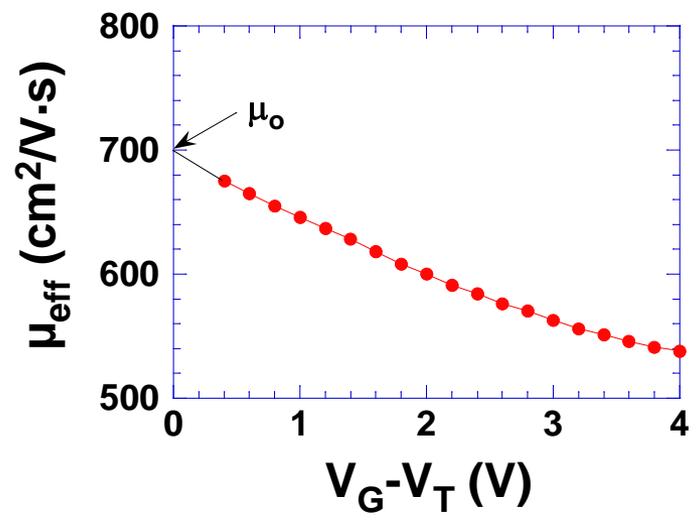
- $I_D - V_D \Rightarrow g_d$; $C_{GC} - V_G \Rightarrow Q_N$; $I_D - V_G \Rightarrow V_T$



$$Q_N = \int_{-\infty}^{V_G} C_{GC} dV_G$$



MOSFET *Effective* Mobility



$$\mu_{eff} = \frac{\mu_o}{1 + \theta(V_G - V_T)}$$

μ_o = low-field mobility; θ = mobility degradation factor



Review Questions

- What are the different mobilities?
- Why is the MOS effective mobility less than the bulk mobility?
- How is μ_{eff} most commonly determined?
- Why does the Hall mobility differ from the conductivity mobility
- How does a Hall mobility measurement work?
- How does the Haynes-Shockley experiment work?
- What is determined with the Haynes-Shockley experiment ?
- For what is the time-of-flight technique used?