

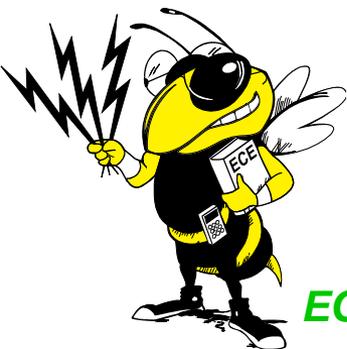


# Generalized Magneto-Optical Ellipsometry

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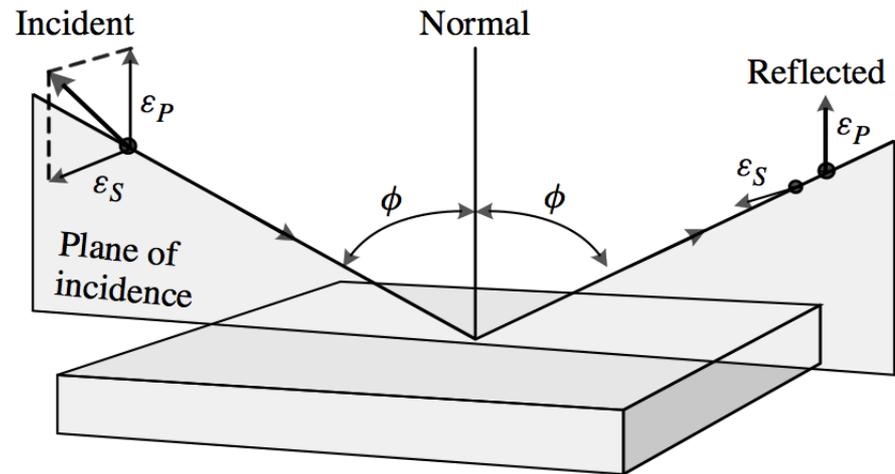
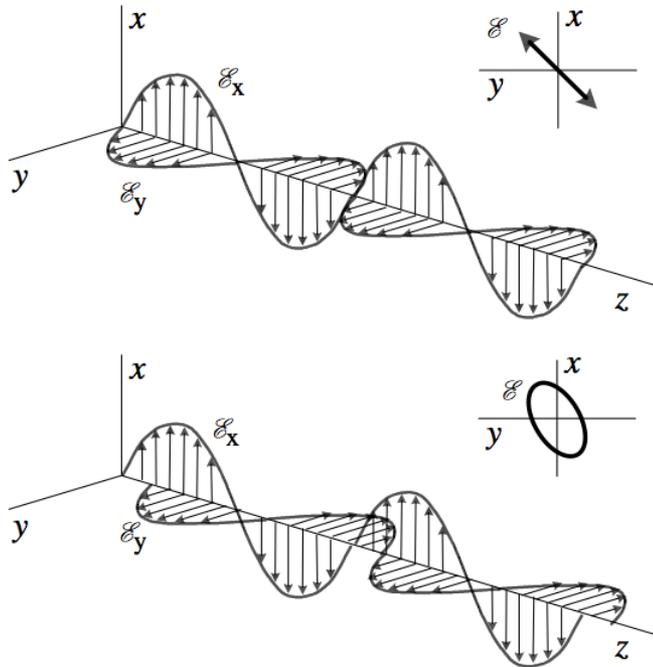
***ECE 4813 - Semiconductor Materials and Device Characterization***  
***Dr. Alan Doolittle***



- **Fundamentals of Polarized Light**
- **Overview of Traditional Ellipsometry**
- **Magneto-Optical Characterization**
- **Generalized Magneto-Optical Ellipsometry**
- **Vector Generalized Magneto-Optical Ellipsometry (Vector Magnetometer)**



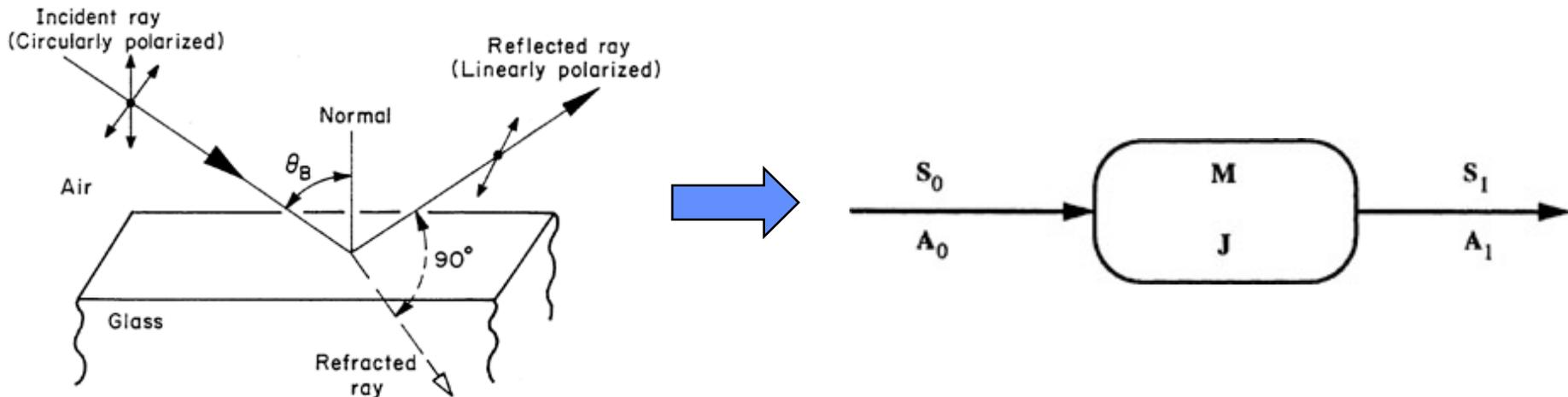
- Light can be fully polarized, partially polarized, unpolarized
  - Fully Polarized Light
    - Linearly Polarized
    - Elliptically Polarized





- **Developed by Dr. Robert Clark Jones**

- Developed between 1941-1956 at Harvard / Polaroid Corporation
- Mathematical model for describing polarized coherent light
- Randomly polarized, partially polarized, and incoherent light cannot be modeled using Jones Calculus
  - Mueller Calculus (Stokes Vectors)





- **Polarized light represented by Jones Vector**

- Linearly Polarized Light

X-Direction:  $\begin{pmatrix} 1 \\ 0 \end{pmatrix}$

Y-Direction:  $\begin{pmatrix} 0 \\ 1 \end{pmatrix}$

- Circular Polarized Light

Left-Hand (LHCP):  $\frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ i \end{pmatrix}$

Right-Hand (RHCP):  $\frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ -i \end{pmatrix}$

- **Linear Optical Element represented by Jones Matrix**

- Horizontal Linear Polarizer:  $\begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}$

- Vertical Linear Polarizer:  $\begin{pmatrix} 0 & 0 \\ 0 & 1 \end{pmatrix}$

- Right Circular Polarizer:  $\frac{1}{2} \begin{pmatrix} 1 & i \\ -i & 1 \end{pmatrix}$

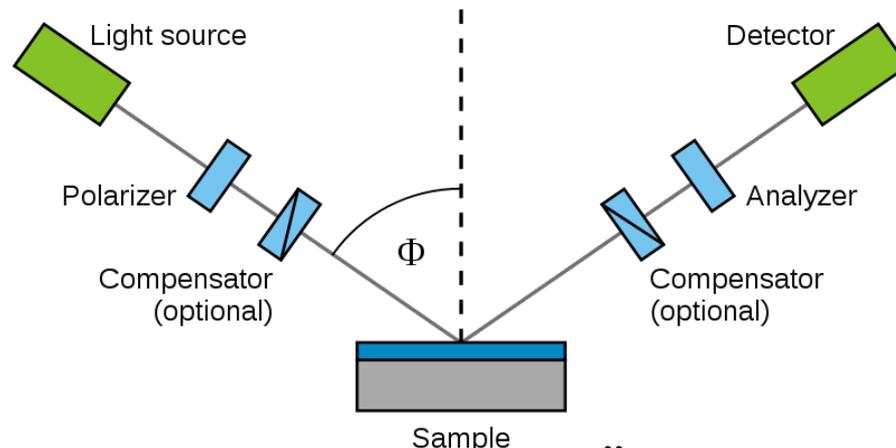


- Interested in optical parameters of thin films and/or semiconductor substrates

- Air ( $n_0$ ) – Semiconductor ( $n_1 - jk_1$ ) Interface
- Air ( $n_0$ ) – Thin Film ( $n_1$ ) – Semiconductor ( $n_2 - jk_2$ ) Interface
- Complex Index of Refraction:  $\tilde{n} = n - jk$ 
  - $n$ : phase velocity in medium
  - $k$ : absorption loss through medium

$$\rho = \frac{R_p}{R_s} = \tan(\Psi)e^{j\Delta}$$

- Example: Null Ellipsometry (PCSA)





- **Applications**

- Optical Properties of Materials
- Film Thickness
- Film Deposition / Etching
  - Process Control
  - In-situ Monitoring

- **GT MiRC Cleanroom**

- Woollam Ellipsometer
- Plas-Mos Ellipsometer



Photos courtesy of GT Microelectronics Research Center



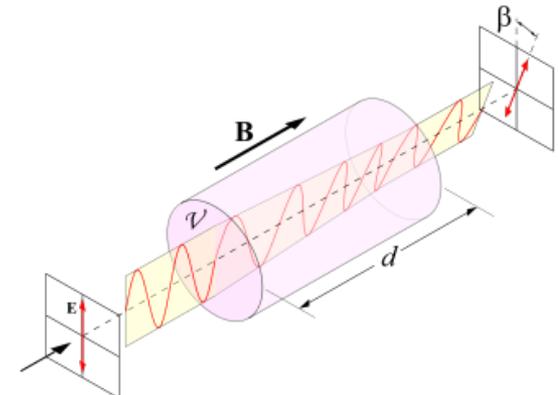
- **Traditional Ellipsometry determine optical properties, but there are also magneto-optical properties**

- Magneto-Optical Storage Devices
  - Ultra thin-film magnetism
- Ferromagnetic Materials
  - Rare-Earth Magnets
  - Ferrofluids



- **Faraday Effect**

- Occurs for light propagating through magnetic fields and magnetic materials
- Rotation of the plane of polarization





- **Full Magneto-Optical Characterization Process (2 Steps)**

- Optical Characterization

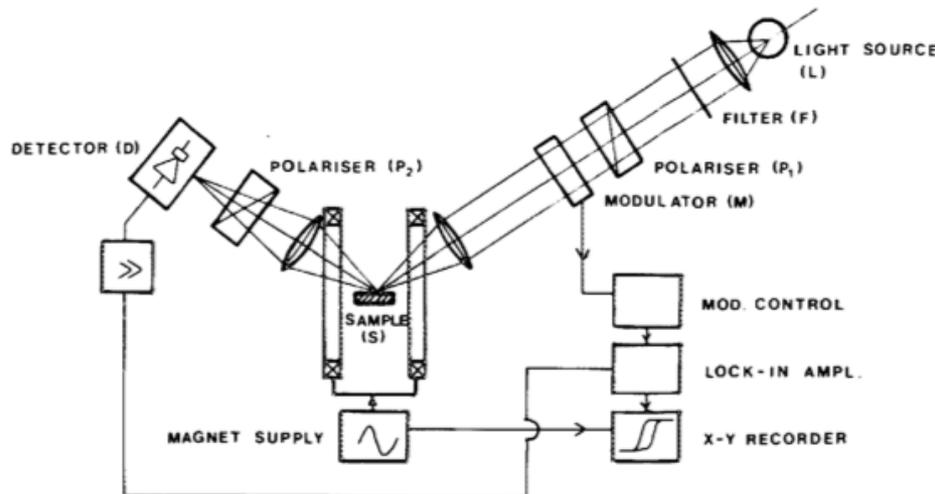
- $\tilde{n} = n - jk$

- Magneto-Optical Characterization

- $Q = Q_r - jQ_i$  (Complex Magneto-Coupling Constant)

- Magnetization Orientation

- **Can we simplify this setup?**



Magneto-optical Ellipsometer  
P. Q. J. Nederpel & J. W. D. Martens  
January 3<sup>rd</sup>, 1985

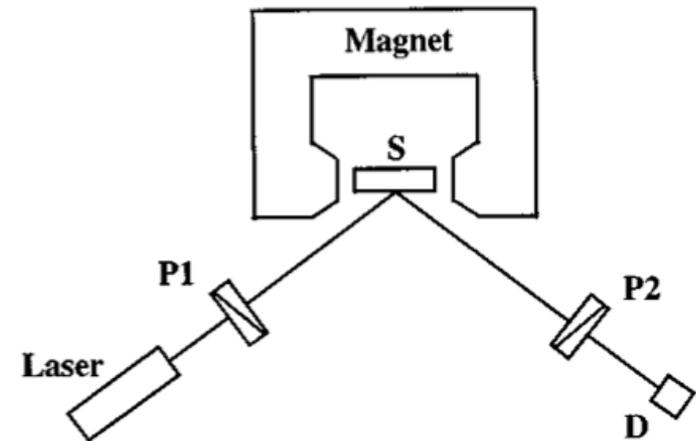


- **Developed by Andreas Berger and Matthew Pufall at University of California – San Diego (1997)**

- Complete magneto-optical characterization
- Combine two-step process into one measurement

- **Measurement Setup**

- HeNe Laser ( $\lambda=632.8$  nm)
- Rotatable Polarizers (Glan-Taylor)
- Torroidal Ferrite Magnet
- Photodiode Detector





- Electric Field Vector at Detector

$$\mathbf{E}_D = \mathbf{P}_2 * \mathbf{R} * \mathbf{P}_1 * \mathbf{E}_L$$

- Glan-Taylor Polarizers defined by Jones matrix

$$\mathbf{P} = \begin{bmatrix} \cos^2(\theta) & \sin(\theta)\cos(\theta) \\ \sin(\theta)\cos(\theta) & \sin^2(\theta) \end{bmatrix}$$

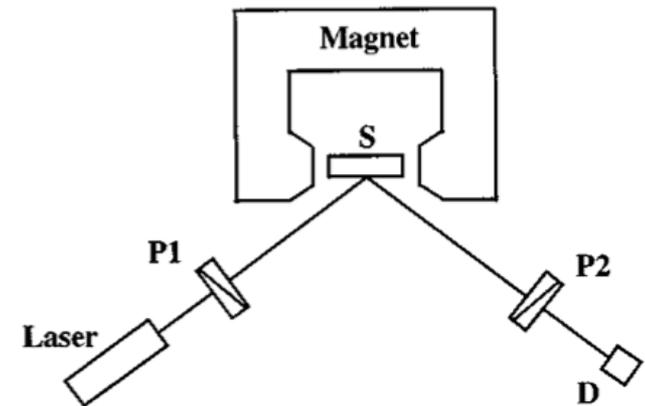
- Reflection (Jones Matrix) of sample

$$\mathbf{R} = \begin{bmatrix} r_s & \alpha \\ -\alpha & r_p + \beta \end{bmatrix} = r_p \begin{bmatrix} \tilde{r}_s & \tilde{\alpha} \\ -\tilde{\alpha} & 1 + \tilde{\beta} \end{bmatrix} = r_p \tilde{\mathbf{R}}$$

- Light Intensity I at detector D

$$I = \mathbf{E}_D \cdot \mathbf{E}_D^*$$

- \*\* Linear approximation:  $\alpha$  and  $\beta$  switch signs at magnetization reversal \*\*





- Fractional intensity change at photodetector,  $\delta I/I$

$$\frac{\delta I}{I} = 4 \frac{B_1 f_1 + B_2 f_2 + B_3 f_3 + B_4 f_4}{f_3 + B_5 f_5 + 2B_6 f_4}$$

$$f_1(\theta_1, \theta_2) = \sin^2(\theta_1) \sin(\theta_2) \cos(\theta_2) \\ - \sin^2(\theta_2) \sin(\theta_1) \cos(\theta_1)$$

$$B_1 = \text{Re}(\tilde{\alpha}) \quad B_2 = \text{Re}(\tilde{r}_s \tilde{\alpha}^*)$$

$$B_3 = \text{Re}(\tilde{\beta}) \quad B_4 = \text{Re}(\tilde{r}_s \tilde{\beta}^*)$$

$$f_2(\theta_1, \theta_2) = \cos^2(\theta_2) \sin(\theta_1) \cos(\theta_1) \\ - \cos^2(\theta_1) \sin(\theta_2) \cos(\theta_2)$$

$$B_5 = |\tilde{r}_s|^2 \quad B_6 = \text{Re}(\tilde{r}_s)$$

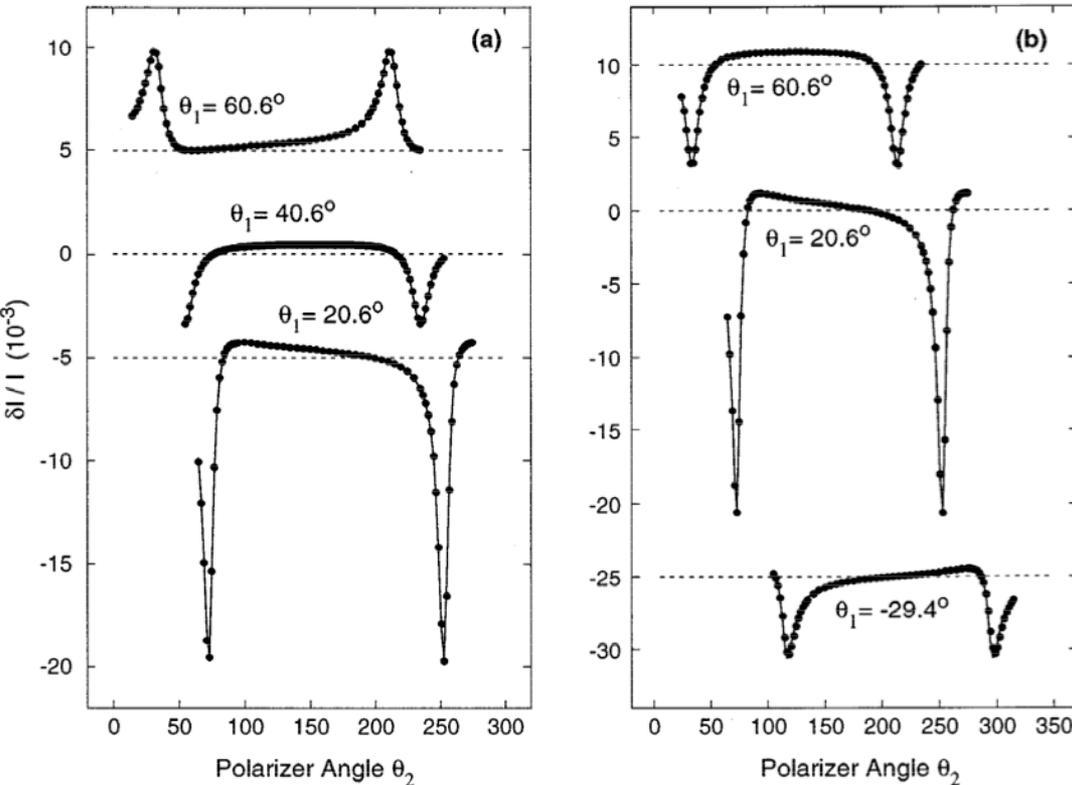
$$f_3(\theta_1, \theta_2) = \sin^2(\theta_1) \sin^2(\theta_2)$$

$$f_4(\theta_1, \theta_2) = \sin(\theta_1) \cos(\theta_1) \sin(\theta_2) \cos(\theta_2)$$

$$f_5(\theta_1, \theta_2) = \cos^2(\theta_1) \cos^2(\theta_2)$$



- Example Data (from Berger & Pufall)

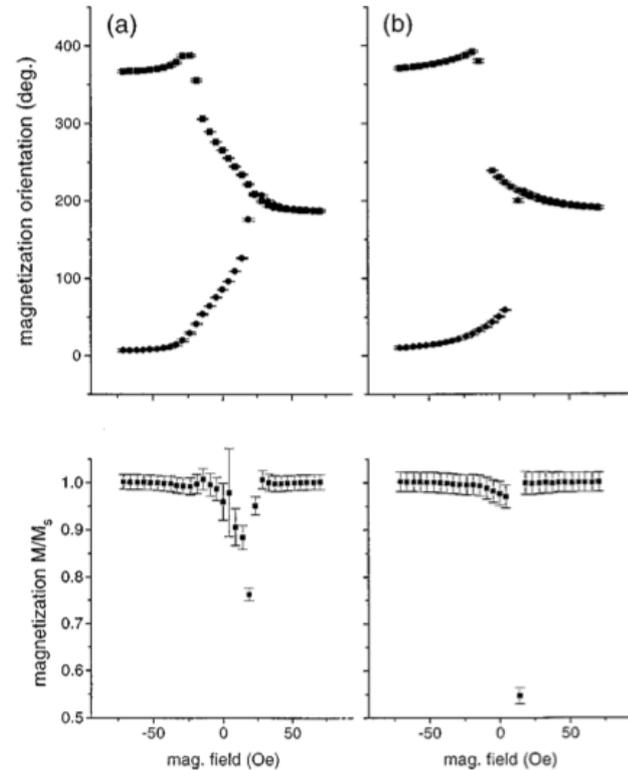
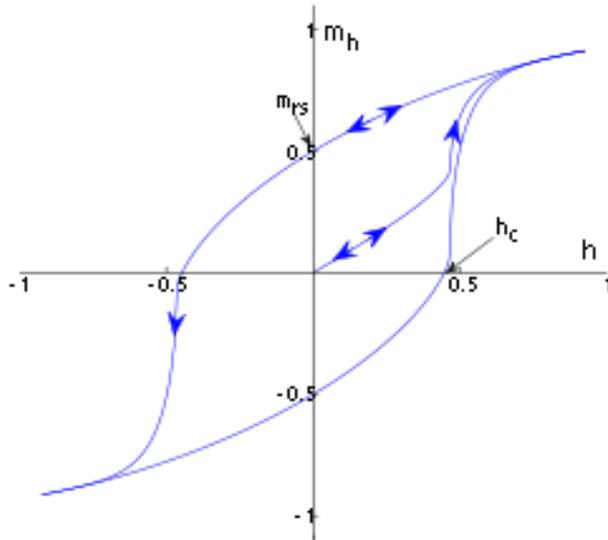


	Data set (a)	Data set (b)
$B_1$	$(-5.034 \pm 0.148) \times 10^{-5}$	$(-2.727 \pm 0.196) \times 10^{-5}$
$B_2$	$(1.850 \pm 0.023) \times 10^{-4}$	$(1.232 \pm 0.028) \times 10^{-4}$
$B_3$	$(1.623 \pm 0.169) \times 10^{-5}$	$(1.980 \pm 0.044) \times 10^{-4}$
$B_4$	$(-3.842 \pm 0.210) \times 10^{-5}$	$(-4.694 \pm 0.074) \times 10^{-4}$
$B_5$	$1.4003 \pm 0.0035$	$1.4279 \pm 0.0048$
$B_6$	$-1.1405 \pm 0.0011$	$-1.1511 \pm 0.0015$

	Data set (a)	Data set (b)	Difference
$n$	$2.403 (\pm 2.4\%)$	$2.439 (\pm 3.3\%)$	1.5%
$k$	$3.693 (\pm 1.4\%)$	$3.561 (\pm 1.9\%)$	3.6%
$Q_r$	$7.346 \times 10^{-3} (\pm 3.5\%)$	$6.781 \times 10^{-3} (\pm 4.4\%)$	8.0%
$Q_i$	$7.781 \times 10^{-3} (\pm 5.5\%)$	$7.926 \times 10^{-3} (\pm 7.3\%)$	1.8%
$\phi$	$3.54^\circ (\pm 0.34^\circ)$	$47.20^\circ (\pm 1.47^\circ)$	43.66°

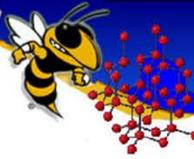


- **Generalized Magneto-Optical Ellipsometry can be used as a vector magnetometer**
  - Andreas Berger and Mathew Pufall
  - Measurement of H vs. M dependence



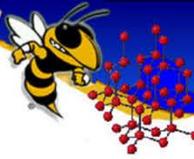


- [1] D.K. Schroder, “Optical Characterization,” in *Semiconductor Material and Device Characterization*, 3rd ed. 2006
- [2] G.G. Fuller, *Optical Rheometry of Complex Fluids*, 1st ed. 1995
- [3] R.M.A. Azzam, *Ellipsometry and Polarized Light*, 1st ed. 1988
- [4] A. Berger, “Generalized Magneto-Optical Ellipsometry,” *Appl. Phys. Lett.*, vol. 71, no. 7, pp. 965-967, August, 1997.
- [5] A. Berger, “Quantitative Vector Magnetometry using Generalized Magneto-Optical Ellipsometry,” *J. Appl. Phys.*, vol. 85, no. 8, pp. 4583-4585, April, 1999.
- [1] D.K. Schroder, “Optical Characterization,” in *Semiconductor Material and Device Characterization*, 3rd ed. 2006



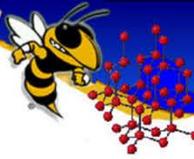
# Scanning Probe Microscopy (SPM)

Brendan Gunning  
ECE 4813



# SPM Flavors

- AFM (Atomic Force Microscopy)
- C-AFM (Conductive Atomic Force Microscopy)
- BEEM (Ballistic Electron Emission Microscopy)
- EFM (Electrostatic Force Microscopy)
- KPFM (Kelvin Probe Force Microscopy)
- NSOM (Near-field Scanning Optical Microscopy)
- SCM (Scanning Capacitance Microscopy)
- STM (Scanning Tunneling Microscopy)
- And more...

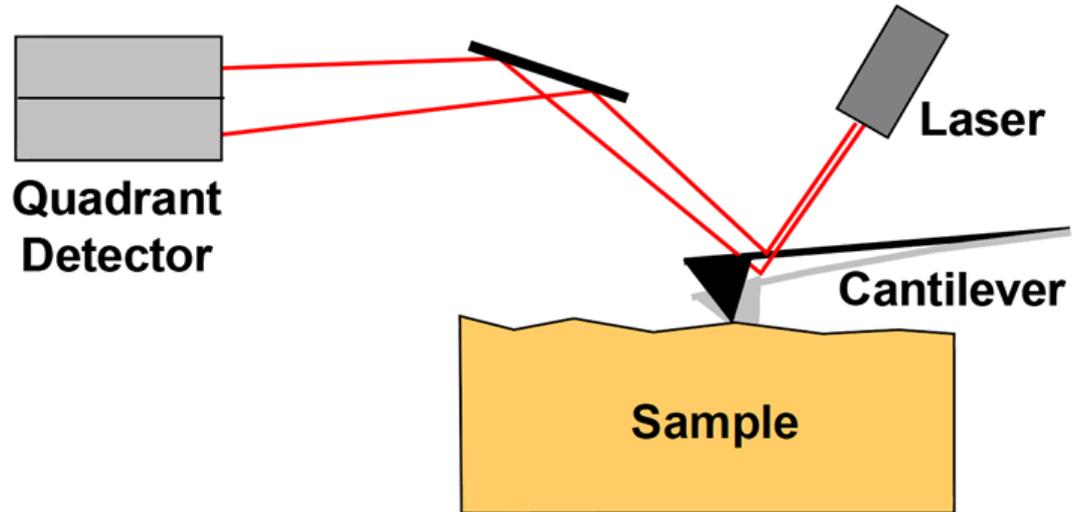


# Conductive Atomic Force Microscopy (C-AFM)

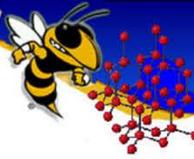


# Conductive AFM

- Like AFM... but it's conductive (duh)
- Cantilever/tip is coated in conductive film (Pt, Pt-Ir, etc)
- Apply bias to tip, ground sample  $\rightarrow$  contact...
- Current flows

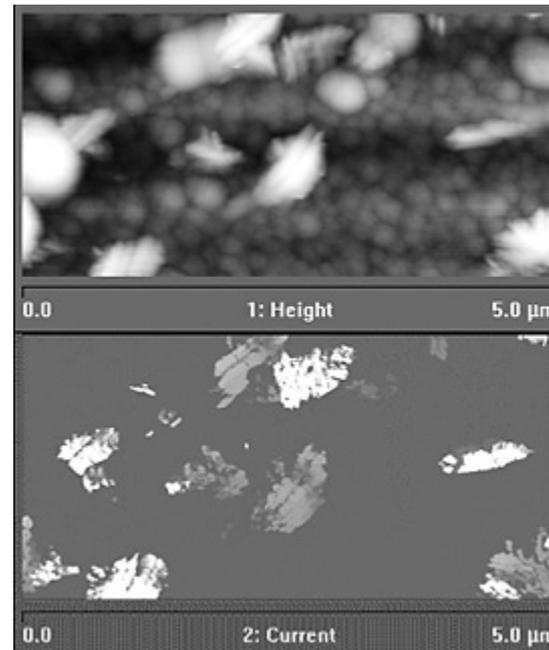


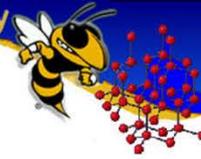
- And... you can still get topography!



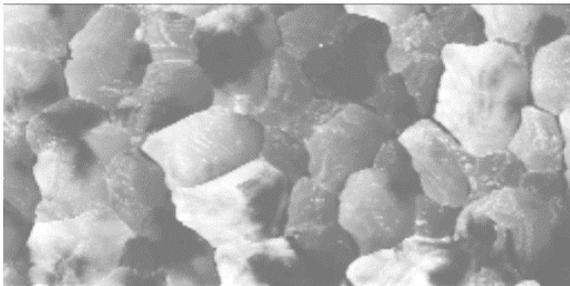
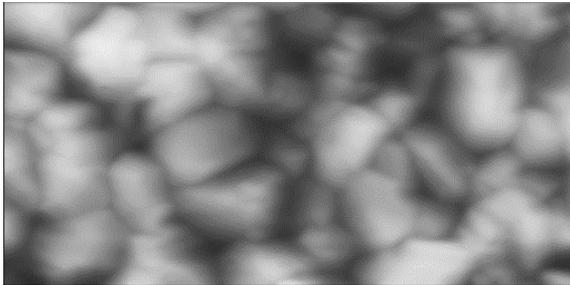
# Current Mapping

- Scan across surface
- Areas with different conductivity will have different currents
- Map current like you do with topography

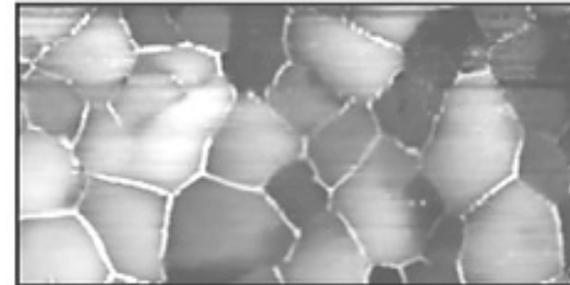




# Processing Characterization



as-grown CdTe/CdS Solar Cell

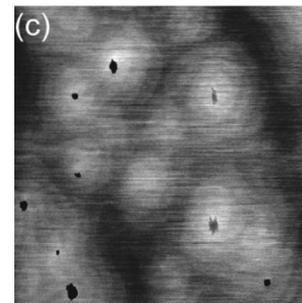
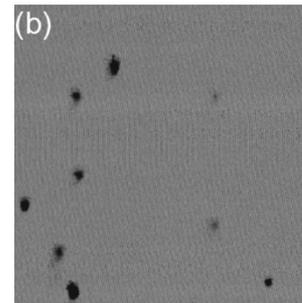
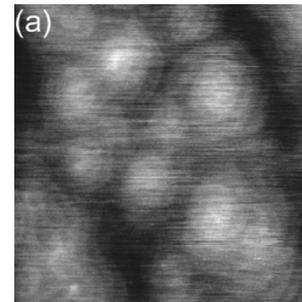


CdTe/CdS Solar Cell  
after bromine-methanol etch

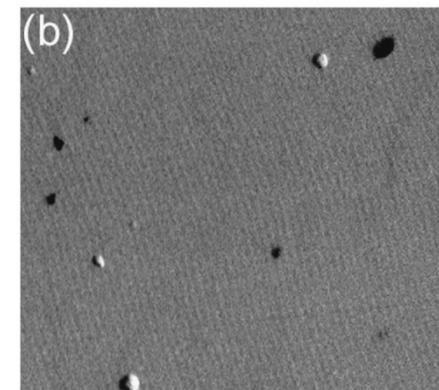
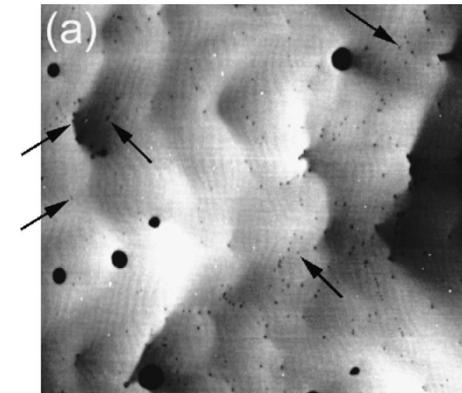


# More Current Mapping

- Mapping the current can shed light on things like:
  - Defects
  - Composition
  - Contamination



500 nm



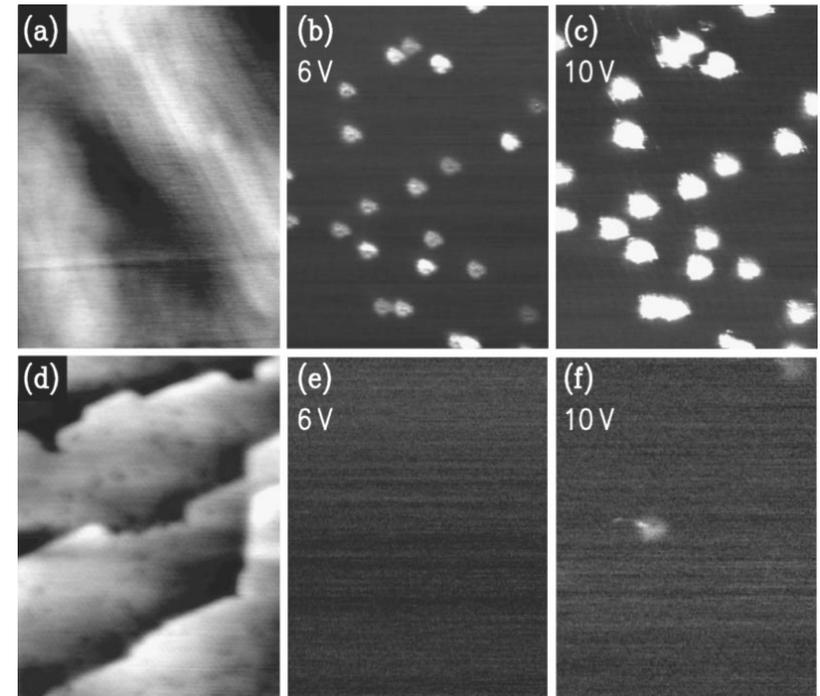
2 μm

Hsu et al., "Direct imaging of reverse-bias leakage through pure screw dislocations in GaN films grown by molecular beam epitaxy on GaN templates", 2002.



# More Current Mapping

- Top samples are GaN grown with just N<sub>2</sub>
- Bottom samples grown with H<sub>2</sub> and N<sub>2</sub>
- H<sub>2</sub> passivated dangling bonds, reducing electrical activity

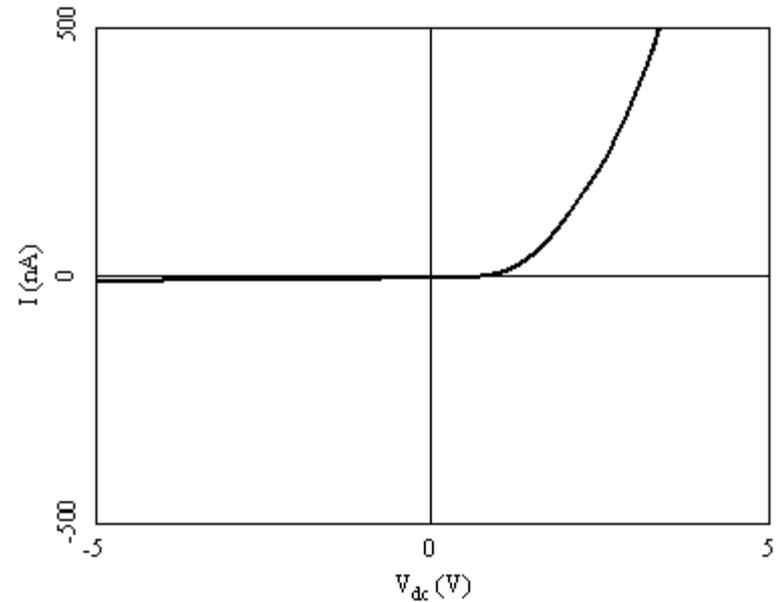


Dong et al., "Effects of hydrogen on the morphology and electrical properties of GaN grown by plasma-assisted molecular-beam epitaxy", 2005.



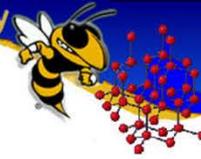
# Scanning Current-Voltage Microscopy (SIVM)

- Tip is held at one x-y location, contacting surface
- Sweep voltage → measure current flow

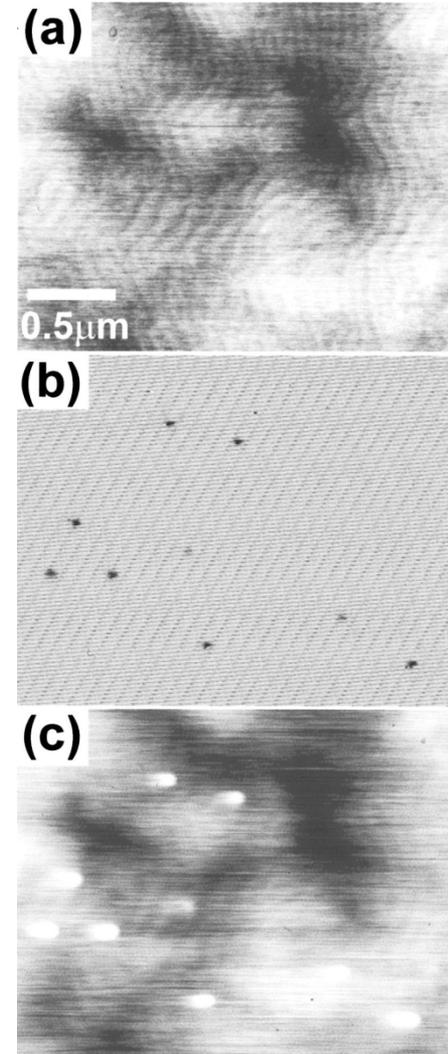
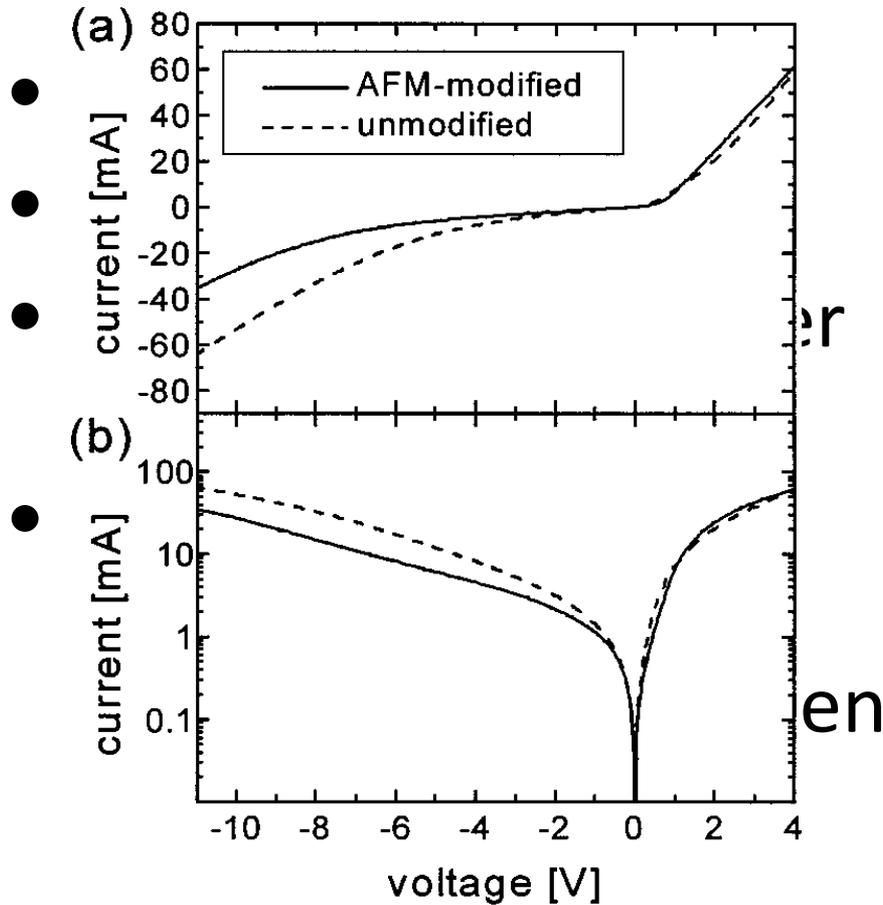


I-V curve of CdTe/CdS taken by  
conductive AFM

Moutinho et al., "Conductive Atomic Force Microscopy Applied to CdTe/CdS Solar Cells", 2004.



# Unintended Side-Effects of C-AFM

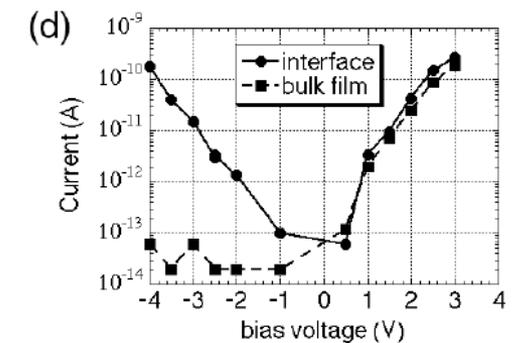
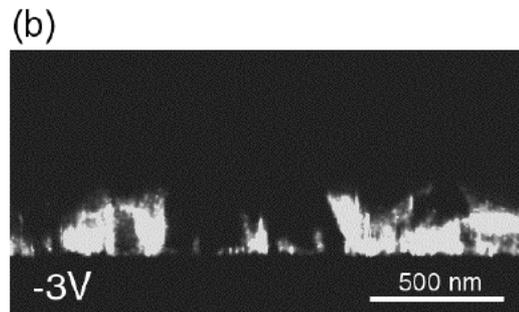
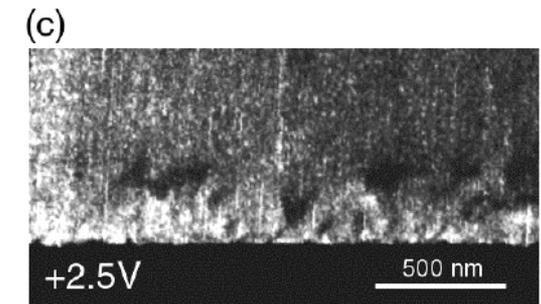
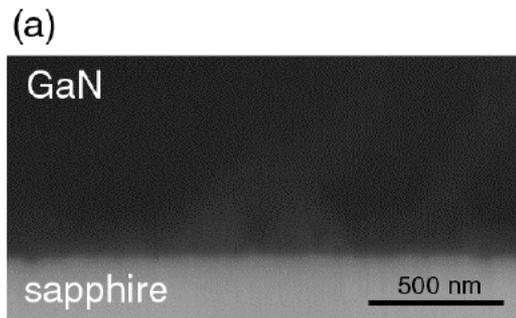


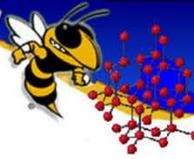
Miller et al., "Reduction of reverse-bias leakage current in Schottky diodes on GaN grown by molecular-beam epitaxy using surface modification with an atomic force microscope", 2002.



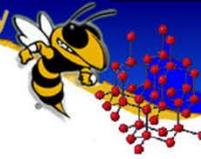
# Cross Sectional C-AFM

- Look at cross section to probe:
  - Multiple layers
  - Interfaces



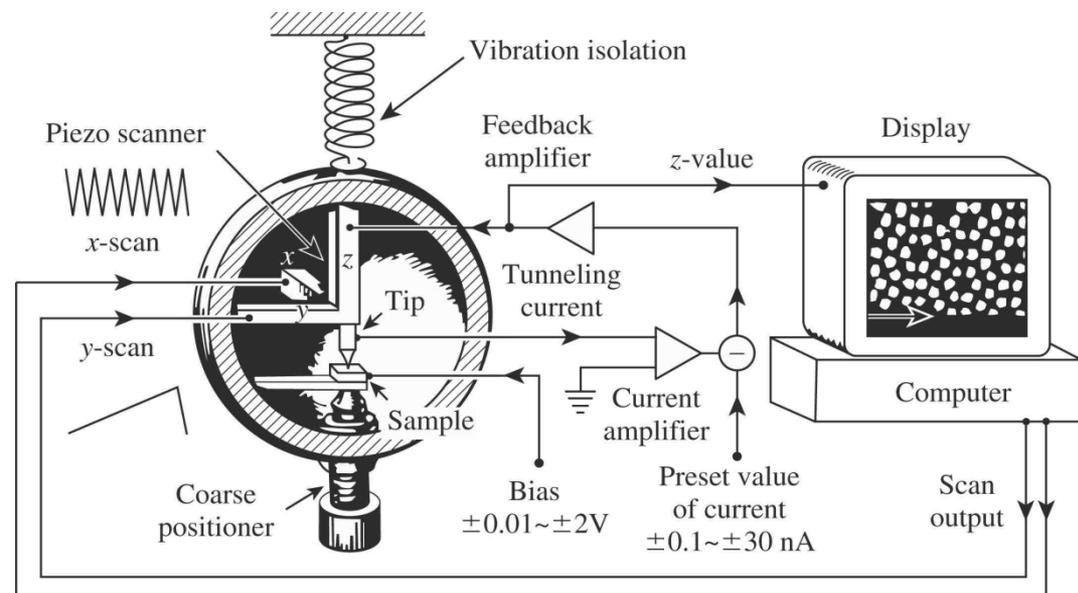


# Scanning Tunneling Microscopy (STM)



# STM Apparatus and Procedure

- Coarse control brings tip (W, Pt-Ir, or Au) close to sample
- Once close enough, z-piezo brings tip within tunneling range ( $\sim 5\text{\AA}$ )
- Z-piezo steps down until preset tunneling current is reached
- As the tip rasters, changes in topography will increase/decrease current
- Feedback raises/lowers tip to maintain constant current
- The distance the tip was raised/lowered forms the topography image



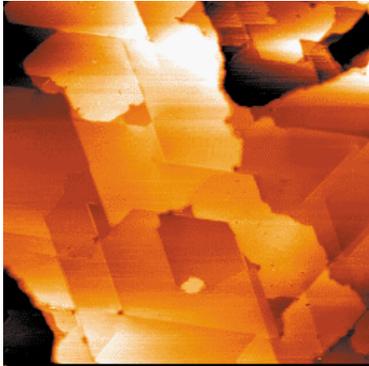


# STM Images

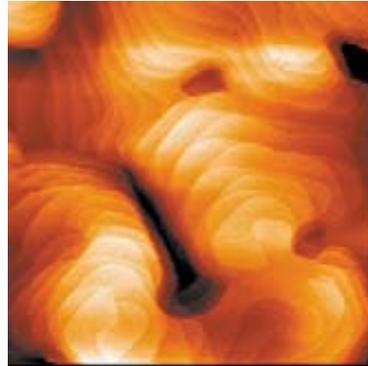
GaN on 6H-SiC

Pit in N-polar GaN on Sapphire

Regular  
(0001)

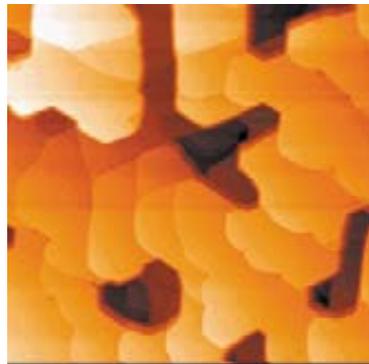


200 nm

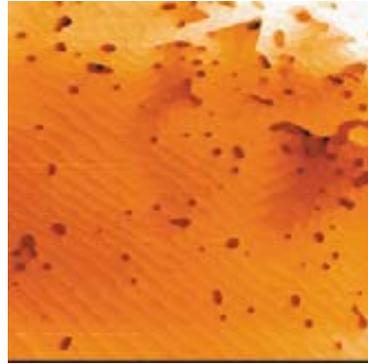


1 μm

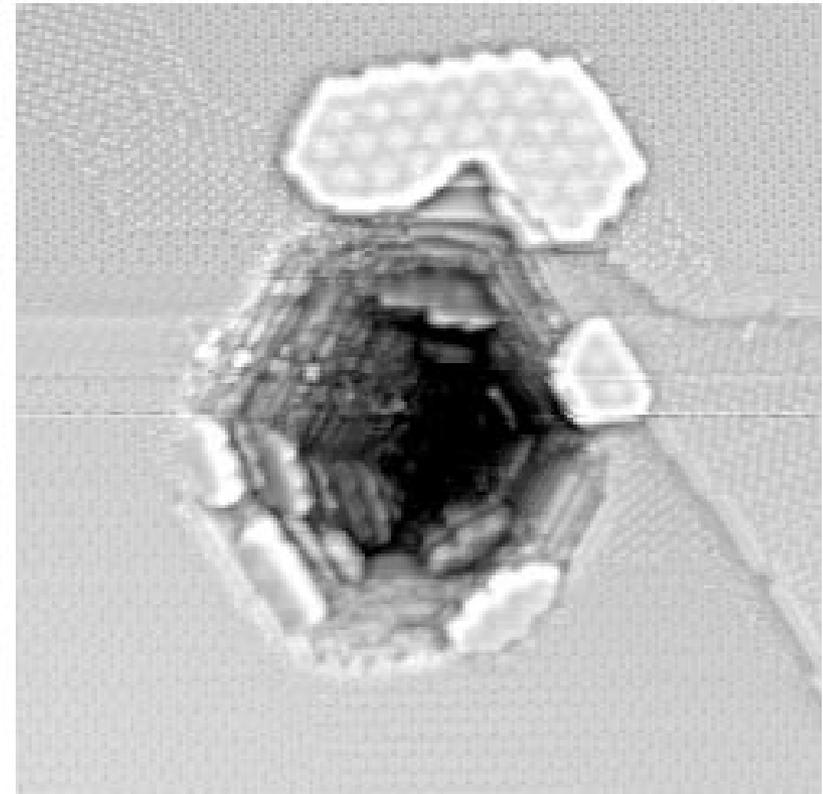
0.4°  
off-cut



500 nm

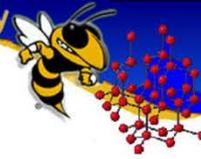


2 μm



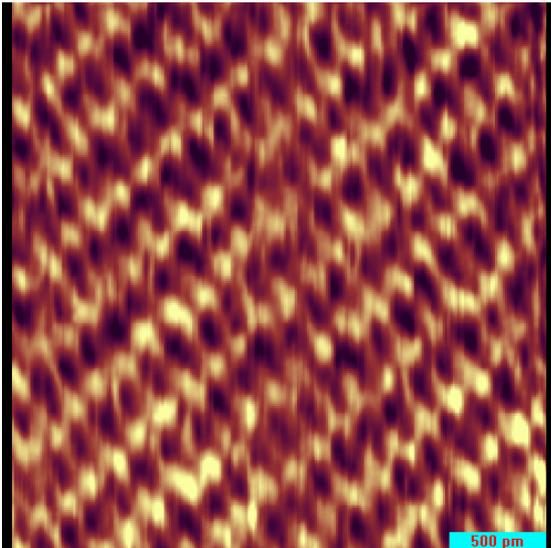
Feenstra et al., "Reconstruction of GaN and InGaN Surfaces", 2000.

Cui et al., "Suppression of Spiral Growth in Molecular Beam Epitaxy of GaN on Vicinal 6H-SiC (0001)", 2001.



# Our STM Images

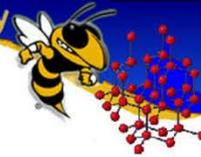
HOPG – Highly Ordered  
Pyrolytic Graphite  
(3nm scan size)



Dirty, non-annealed Gold  
(726nm scan size)

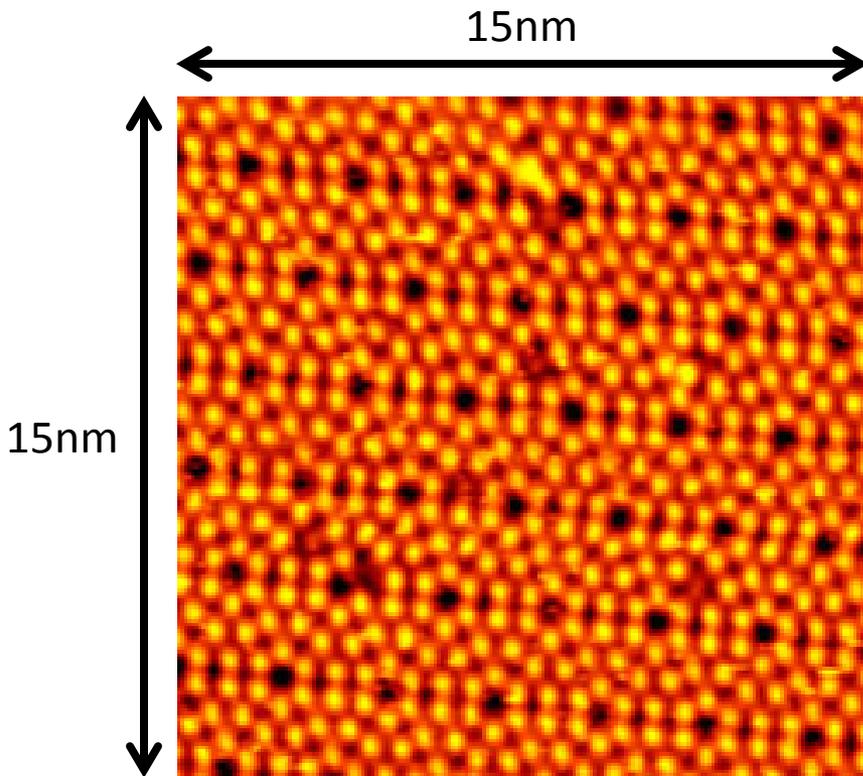


Me! 2010

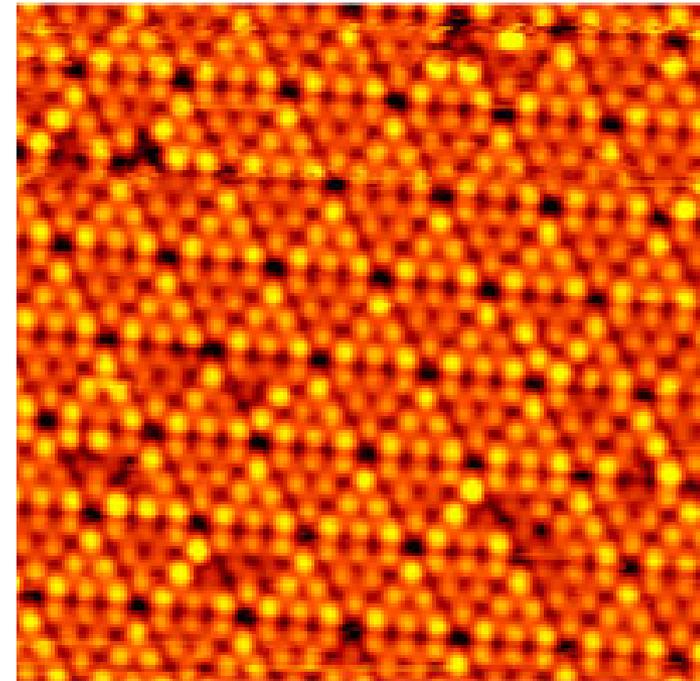


# Empty vs. Filled States

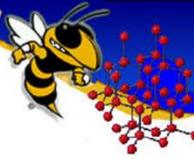
7x7 surface reconstruction of Si (111) – 1.5nA tunneling current



+2V bias = Empty states

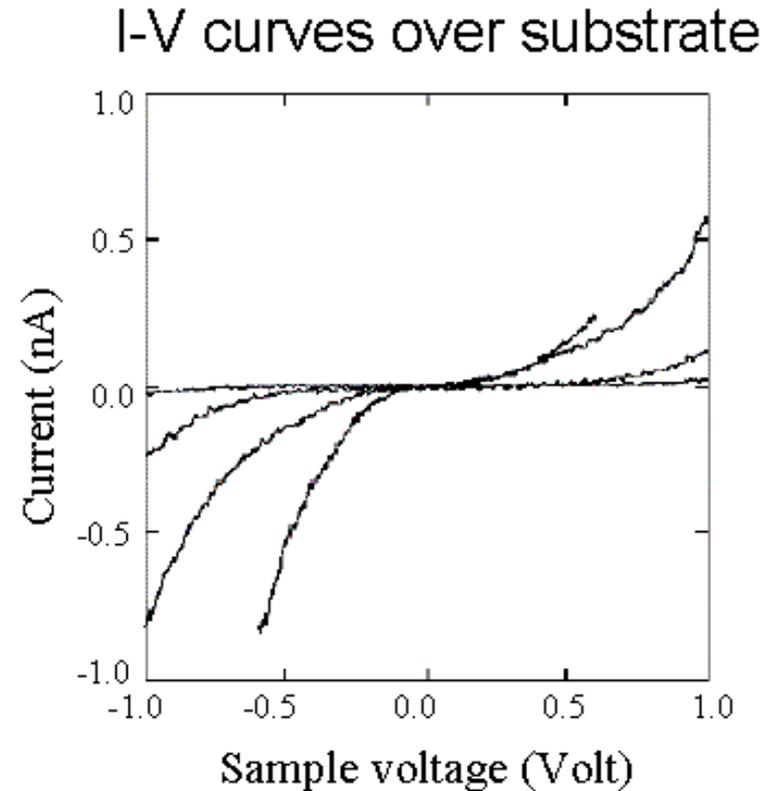


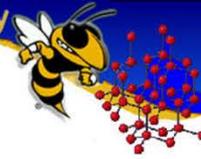
-2V bias = Filled states



# What else can we do?

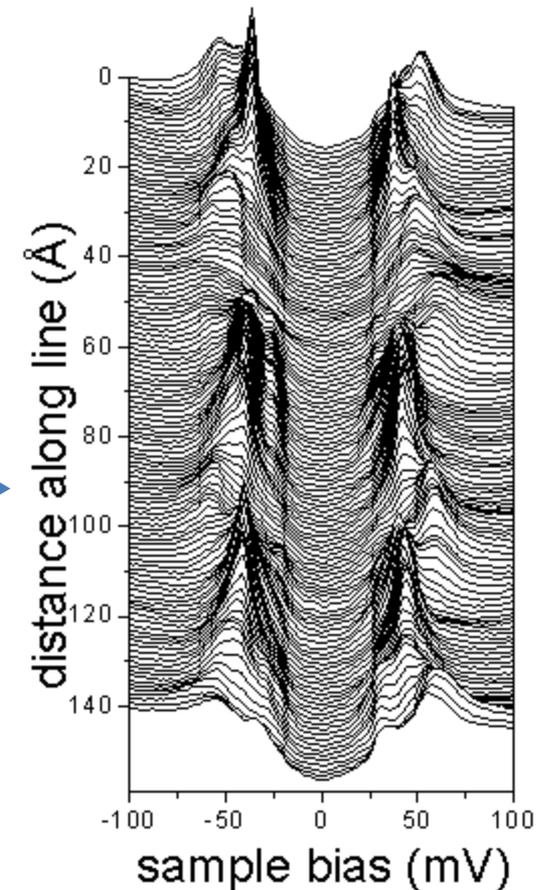
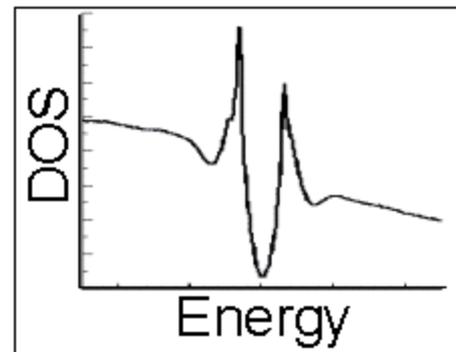
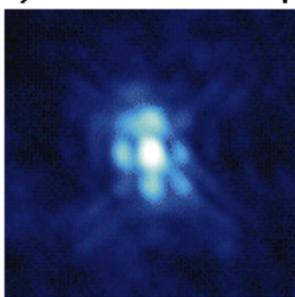
- Rather than just sweeping across the surface with a set bias...
- STS sweeps the bias at a fixed x-y-z position
- Generates a “local” I-V curve, representing the integrated density of states at that position as a function of energy
- The derivative of this I-V curve,  $dI/dV$ , can tell us even more...

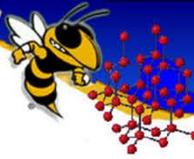




# Scanning Tunneling Spectroscopy

- Instead of the integrated density of states, the  $dI/dV$  spectrum shows us the actual density of states at that location as a function of energy
- Can use the density of states data to create a “map” across a sample area at a chosen energy



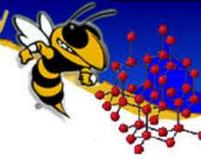


# Conclusion

- SPM covers a huge variety of more specific characterization methods
- Each one of these characterization methods is useful in and of itself

Whether it's C-AFM, STM, or some other method...

SPM is an extremely useful and powerful characterization tool





# Light Beam Induced Current/Voltage

Guy Raz

ECE 4813 – Dr. Alan Doolittle

Fall 2011

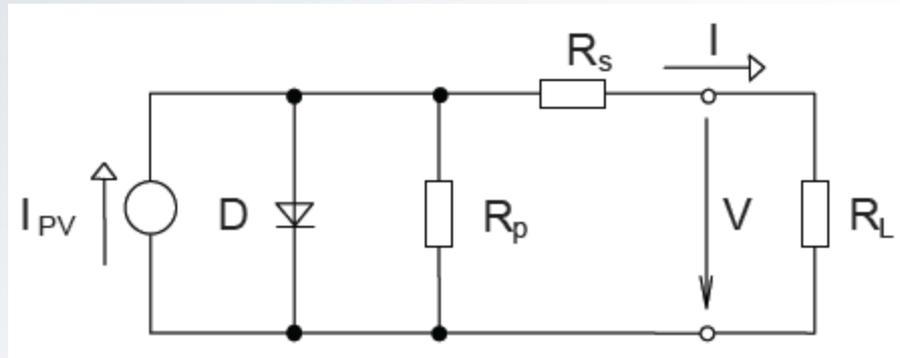


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# Motivation

- The development and production of polycrystalline solar cells creates a necessity for analysis with high spatial resolution
- Contactless probes can be used to examine:
- EBIC - has been widely applied
- LBIC is more appropriate for solar cells
  - for study of defects
  - LBIV – measuring  $V_{OC}$  instead of  $J_{SC}$

# Solar Cell Modeling



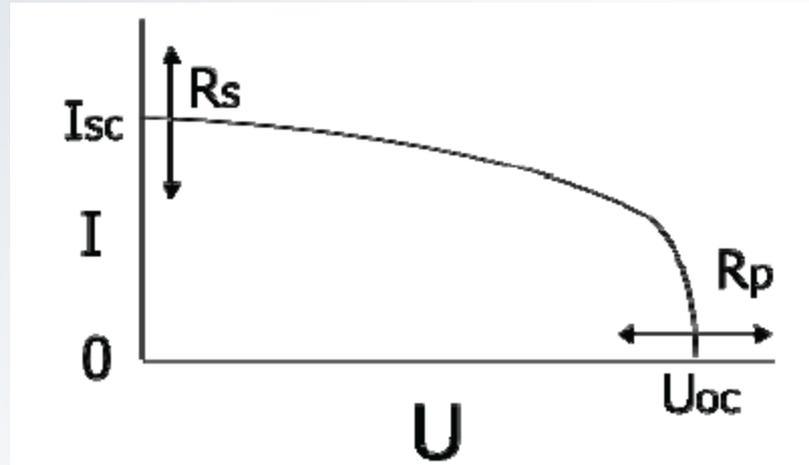
- For a short circuit current (LBIC method) where  $V=0$

$$I_{sc} = AJ_{PV} - I_{01} \left[ \exp\left(e \frac{R_s I}{kT}\right) - 1 \right] - I_{02} \left[ \exp\left(e \frac{R_s I}{2kT}\right) - 1 \right] - \frac{R_s I}{R_p}$$

- For open circuit voltage (LBIV method)

$$V_{oc} = \frac{2kT}{e} \ln\left(\frac{-I_{02} + \sqrt{I_{02}^2 + 4I_{01}(I_{02} + I_{01} + AJ_{PV})}}{2I_{01}}\right)$$

# Solar Cell Modeling (cont.)



- LBIC measurements are made around  $V=0$ 
  - Slope is low, current changes slowly
- LBIV made around  $I = 0$

# Introduction

- When a light beam strikes a semiconductor, it will generate electron-hole pairs (EHPs) within the beam's interaction volume.
- These EHPs will be separated by drift due to the internal electric field.
- The E/Hs can be collected at the contacts of the object.
- Amplifying and analyzing these measurements show variations in generation, drift and recombination which can be measured and displayed.

# Apparatus

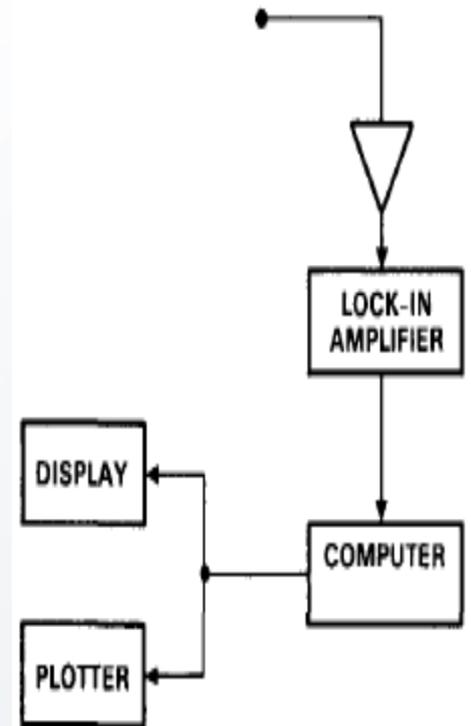
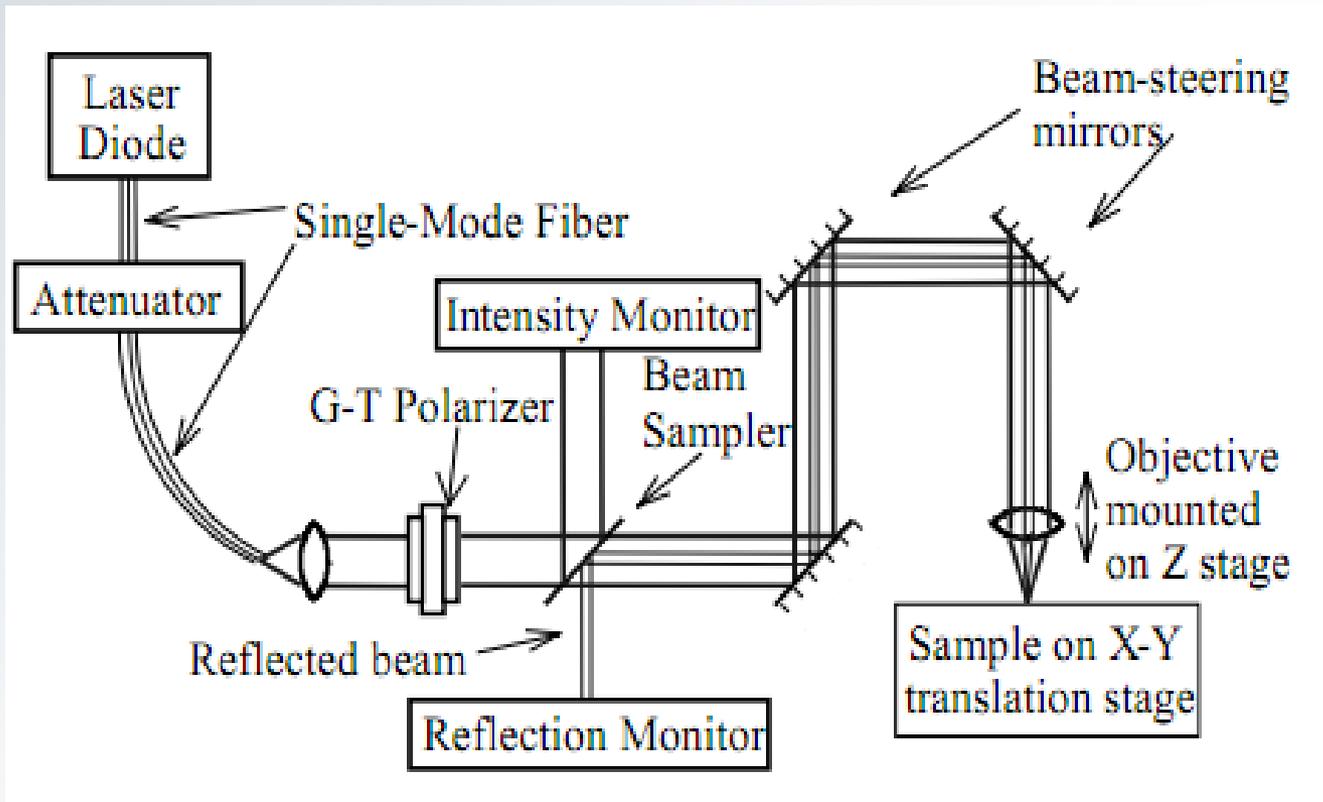


Figure from: Hiltner & Sires

# Quantum Efficiency

- QE is the ratio of the number of charge carriers collected by the solar cell to the number of photons shinning on the solar cell.

$$IQE = \frac{1}{1 - R} \frac{I_{sc} / e}{P_L / (h \cdot c / \lambda)}$$

- EQE
- $I_{sc}$  is dependent on the amount of absorbed light
  - Corrected by first factor

# Photon Penetration/Absorption

- Energy of a photon depend only on its wavelength by

$$E = \frac{h \cdot c}{\lambda}$$

- The depth of penetration depend on Energy (KeV) and material. (silicon example)

Wavelength (nm)	Penetration Depth ( $\mu\text{m}$ )
400	0.19
500	2.3
600	5.0
700	8.5
800	23
900	62
1000	470

# Diffusion Length

- Photo-induced current decay is dependant on the relative thickness of sample
- It is necessary to consider two cases when analyzing LBIC intensity :
  - Thick Sample Cases ( $W > 4L_b$ )
  - Thin Sample cases ( $W < 4L_b$ )

# Sample Cases

- Thick Sample Cases ( $W > 4L_b$ )
  - EBIC intensity as a function of distance  $x$  from the barrier, in a semiconductor of semi-infinite thickness and far from the collector edge ( $x \gg L_b$ )

$$I(x) = C \exp\left(-\frac{x}{L_b}\right) x^{-n}$$

- Thin Sample Cases ( $W < 4L_b$ )
  - In thin samples, the influence of the front and rear surface recombination becomes very important

$$I(x) = I_0 \exp\left(-\frac{x}{L_{eff}}\right)$$

# Surface Recombination Velocity

- If surface recombination velocities are negligible

$$(s_f = s_r = 0)$$

- $L_{\text{eff}} \approx L_b$

- However, if surface recombination velocities are large

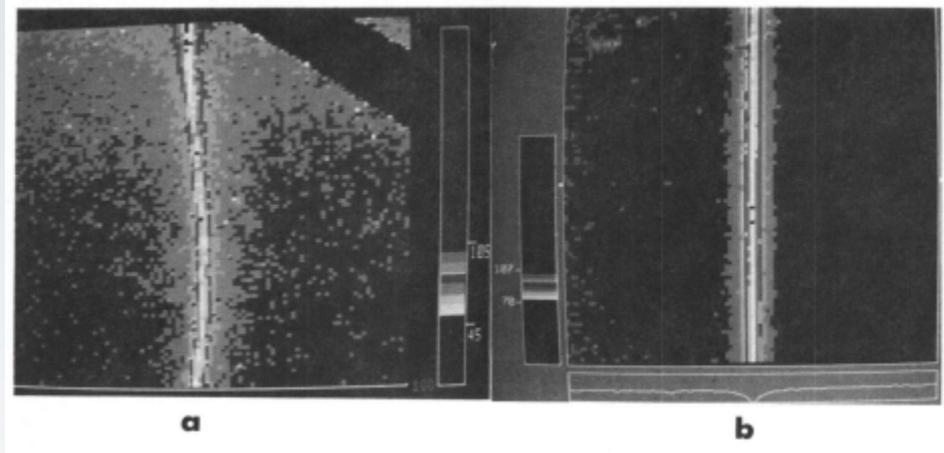
$$(s_f = s_r = \infty)$$

- $\frac{1}{L_{\text{eff}}} = \sqrt{\frac{1}{L_b^2} + \frac{\pi^2}{W^2}}$

- If  $s_f = 0$  and  $s_r = \infty$ , or the opposite

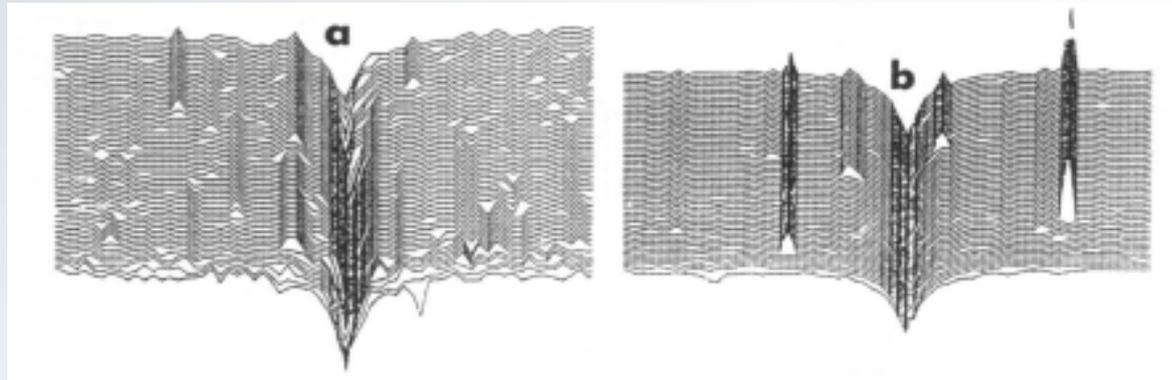
- $\frac{1}{L_{\text{eff}}} = \sqrt{\frac{1}{L_b^2} + \frac{\pi^2}{4W^2}}$

# LBIC topography



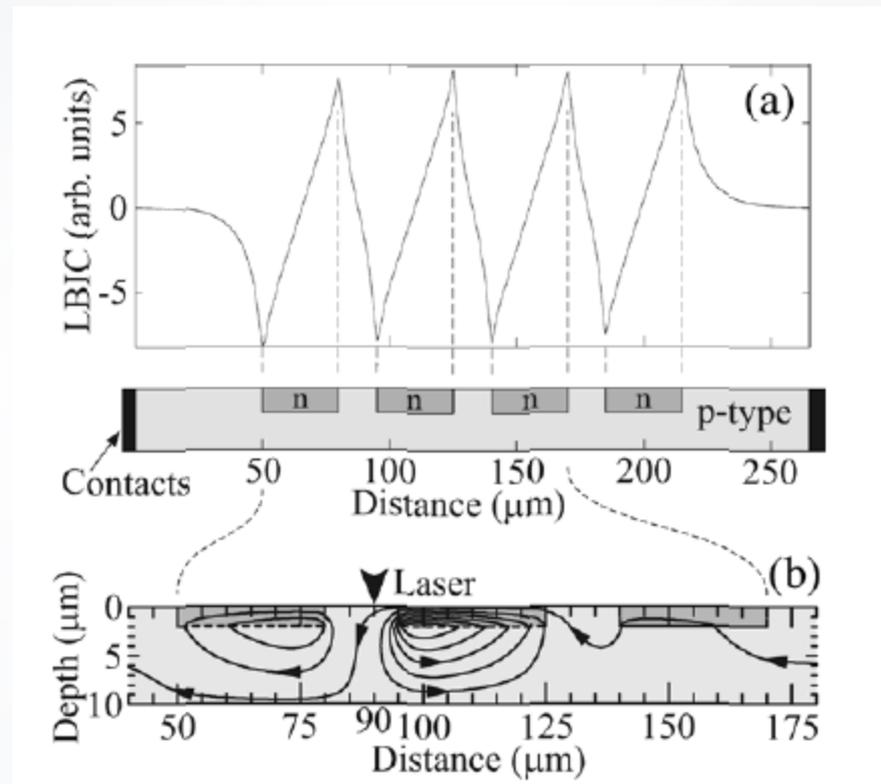
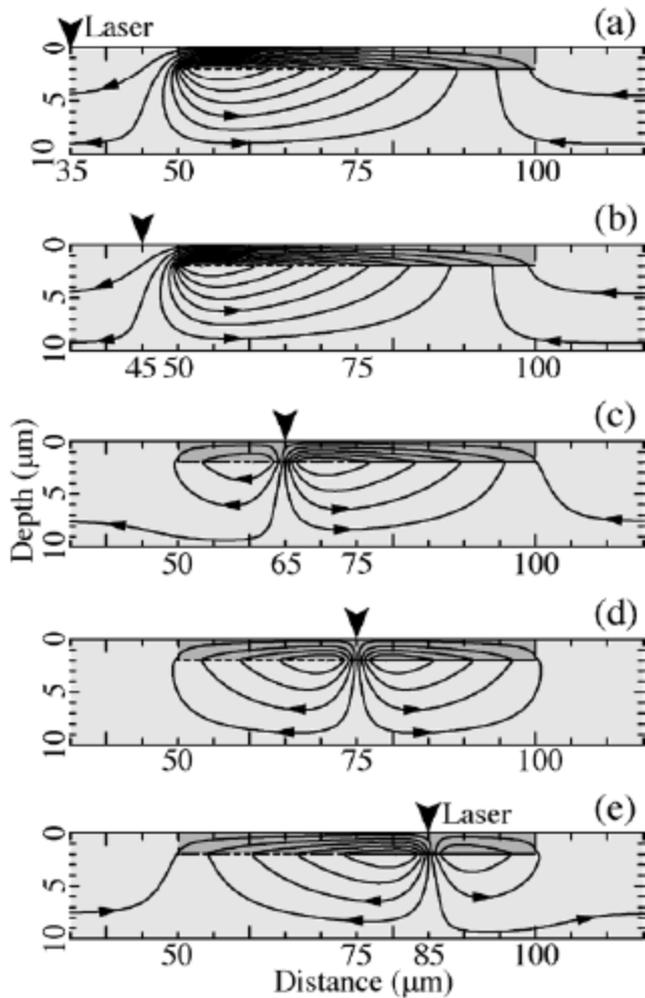
- Imaging carried out using 100 line with 100 points each at a step of  $10\mu\text{m}$ 
  - Solar cell area is  $1\text{mm}^2$
- Minority carrier recombination is clearly evident
- Photocurrent reduced by 25% near grain boundary

# LBIC topography (cont.)

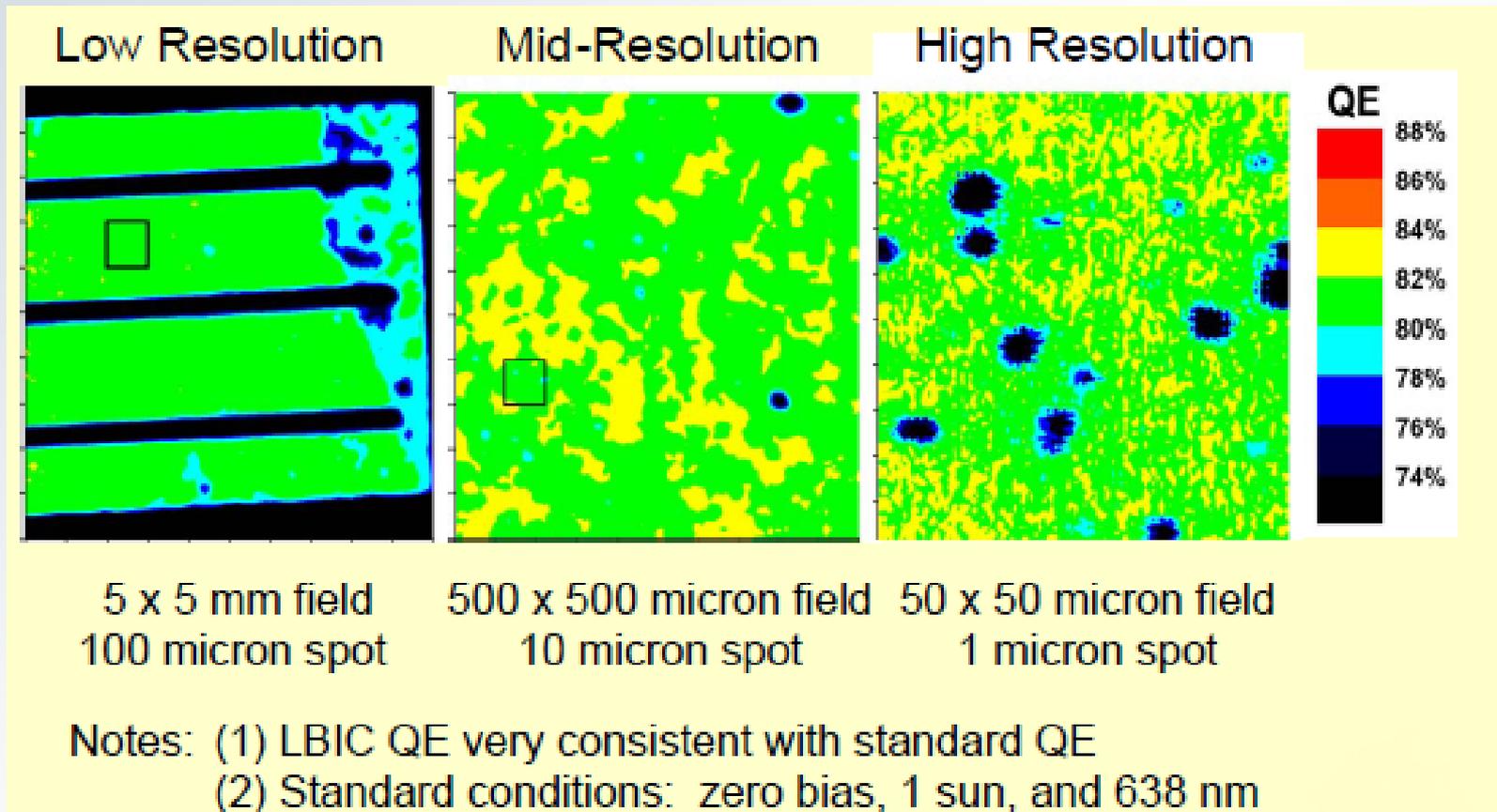


- Finding the surface recombination velocity we can find the diffusion length  $L_1$ .
- The background current density is given by
  - $I_0 = qN(1 - R)\alpha L(1 + \alpha L)^{-1}$
- We can solve for diffusion length  $L_2$
- The observed difference between the two above  $L$ s leads us to interface layers and/or the presence of impurities in the sample

# Light Sweep

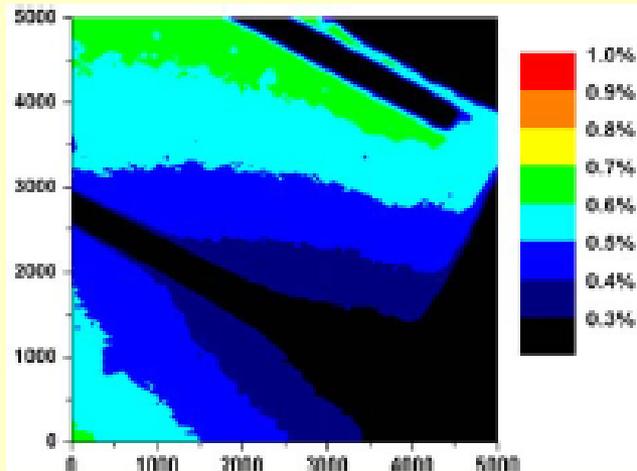


# Resolution

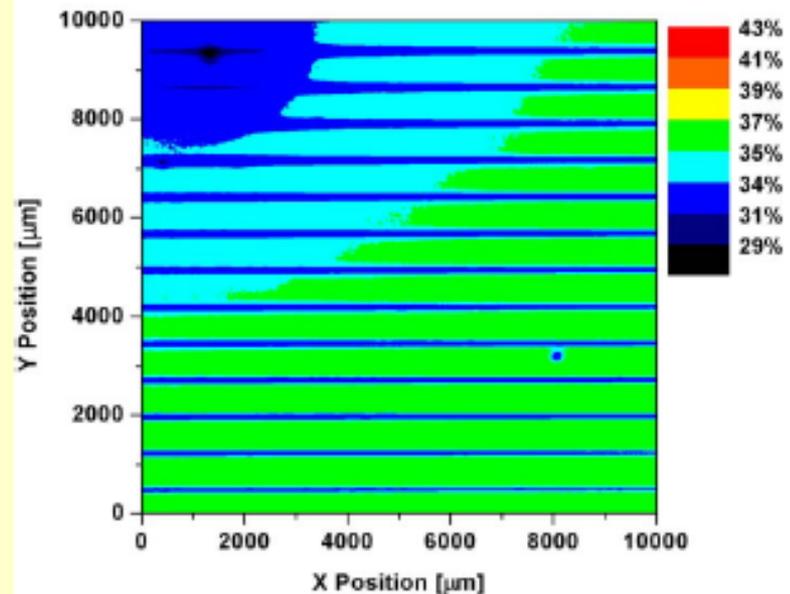


# Defect Detection

CIGS cell with grid finger edge short. Very low QE.



Shunt is located very near grid line.

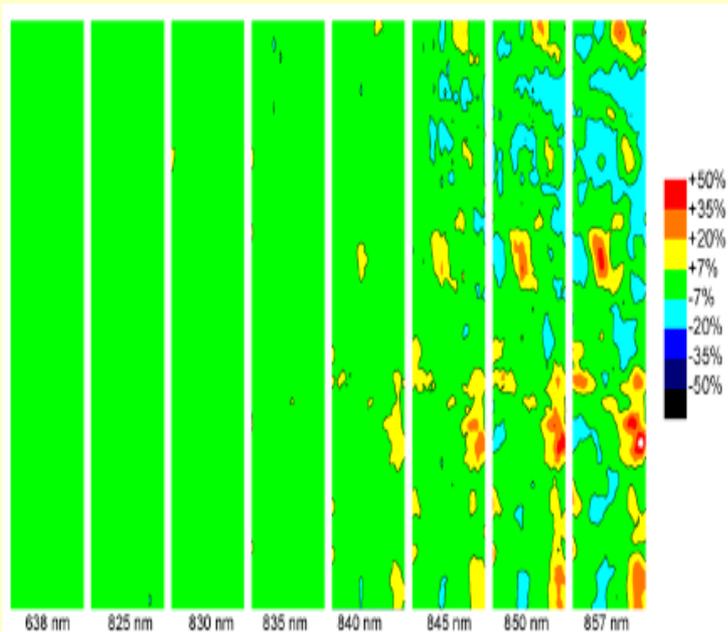


Shunt affects large area: field is 1 cm<sup>2</sup>

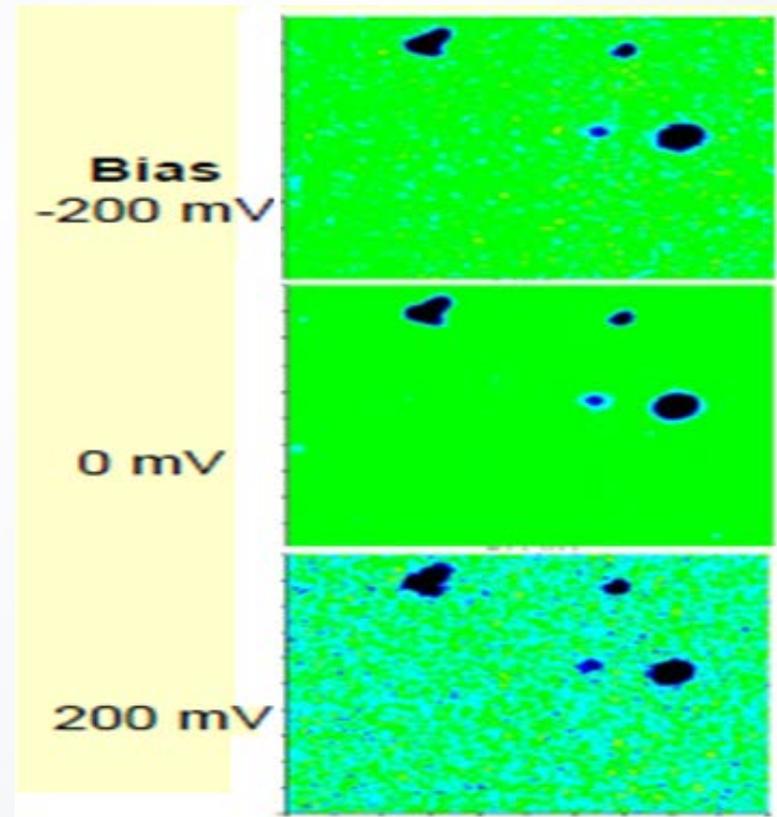
# LBIC Variations

## Wavelength Variation

High-resolution maps of CdTe cell with increasing wavelength  
10x50 micron field, 1 micron spot



## Bias Variation



# Quiz

1. What does LBIC stand for?
2. How is light generated for the LBIC apparatus?
3. What is the limit for defining a thick/thin sample?  
( $W >/< \text{___}$ )
4. Which would have a greater affect on the  $I_{sc}$ ?  $R_s$  or  $R_p$
5. What is the highest resolution that can be seen with LBIC?



# Vibrating Sample Magnetometer

Brooks Tellekamp

ECE 4813

November 2011



**Georgia** Institute  
of **Technology**<sup>®</sup>

# Outline

- Overview of Magnetic Properties
- Units
- Basic Magnetic Relations
- History
- VSM Basics
- Mechanical Design
- Properties of VSM

# Overview of Magnetic Properties

- B = Magnetic Flux Density or Magnetic Induction
- H = Magnetic Field (typically applied to a sample)
- m = Magnetic Dipole Moment
- M = Magnetization
- $\mu$  = Magnetic Permeability
  - Permeability of free space  $\mu_0 = 4\pi \times 10^{-7} \frac{V \cdot S}{A \cdot m}$  (SI)
- $\chi_m$  = Magnetic Susceptibility

# Units

- Gaussian units – a physical system for electromagnetic units based in CGS (centimeter-gram-second) base units

Unit	SI	CGS	Conversion
B	Tesla	Gauss	$1T=10,000G$
H	$\frac{A}{m}$	Oersted (Oe)	$\frac{A}{m} = \frac{4\pi}{1000} Oe$
m	$A \cdot m^2$	$emu(\frac{erg}{G})$	$A \cdot m^2 = 1000emu$
M	$\frac{A}{m} = \frac{J}{T}$	$\frac{emu}{cm^3}$	$\frac{A}{m} = .001 \frac{emu}{cm^3}$
$\mu$	$\frac{H}{m}$	Unitless	$\frac{\mu}{\mu_0} = \mu^G$
$\chi_m$	Unitless	Unitless	$\chi_m^{SI} = 4\pi\chi_m^G$

# Overview of Magnetic Relations

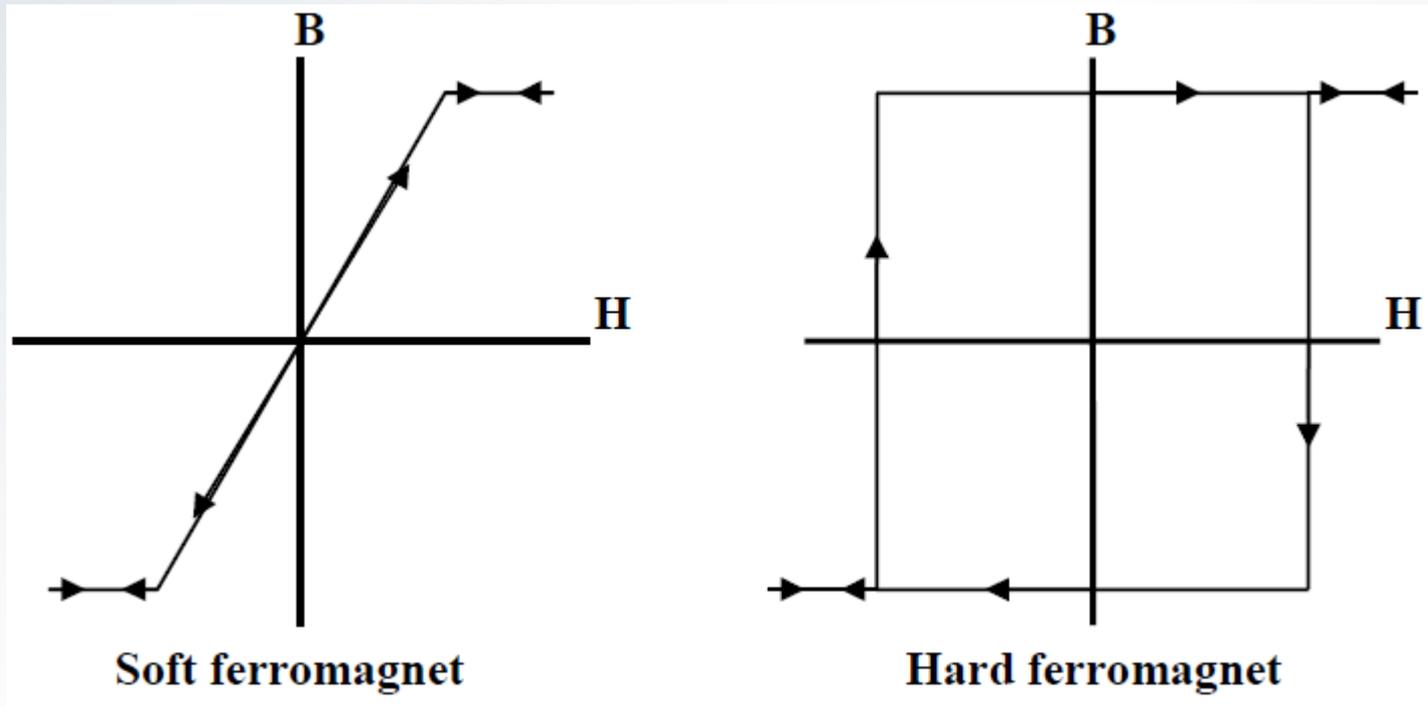
SI	CGS
$B = \mu H = \mu_0(H + M)$ $M = \chi_m H$ $\mu = \mu_0(1 + \chi_m)$	$B = \mu H = H + 4\pi M$ $M = \chi_m H$ $\mu = 1 + 4\pi\chi_m$

Where  $\frac{\mu}{\mu_0} = \mu_r =$  relative permeability (material dependant)

And  $M = nm$  where  $n = \frac{N}{V}$  (number of acting moments per unit volume)

# Hysteresis

- Ferromagnetic materials retain magnetic orientation
- Ferromagnetic materials exhibit different curves for directional field sweeps (+ to -, or - to +)

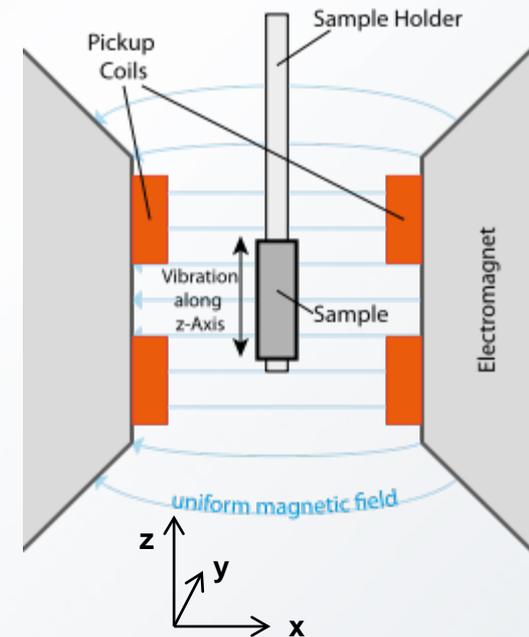


# History

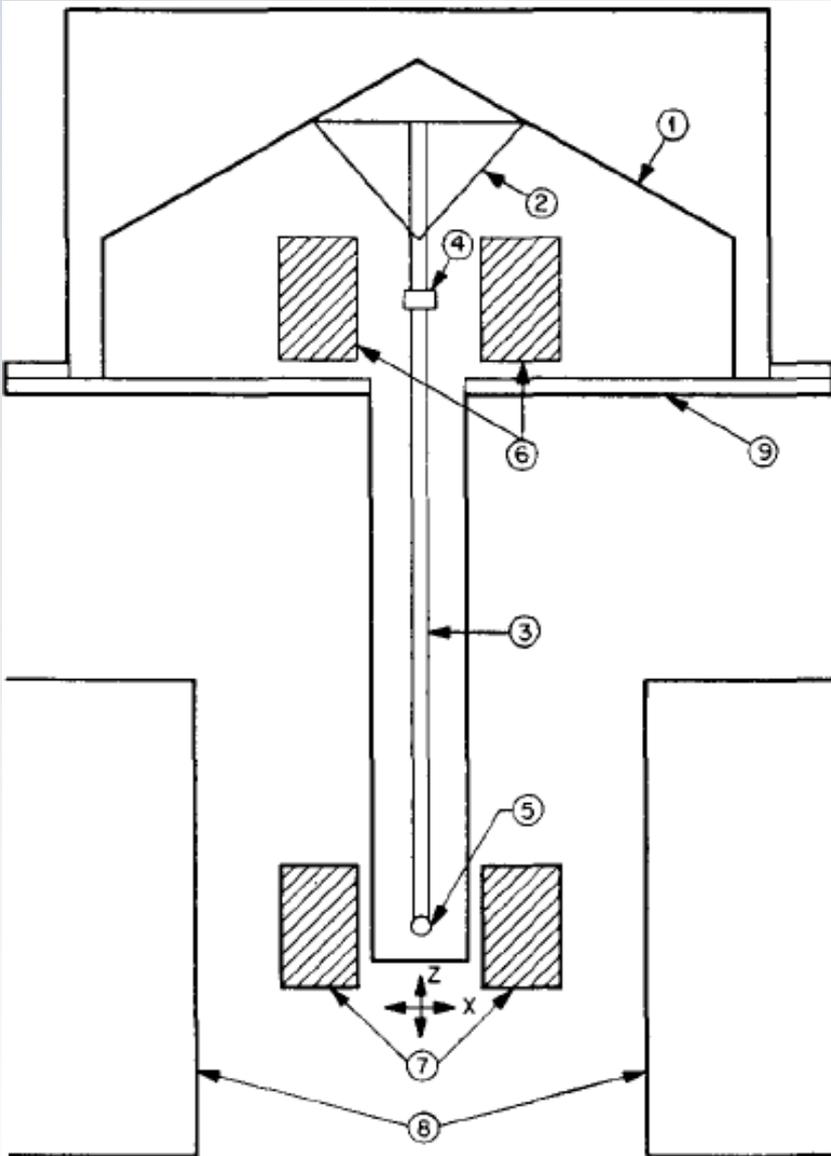
- Developed in the late 1950's
- No good way to measure magnetic moments without considerable prior knowledge of material properties
- Force methods are very sensitive and require a field gradient
- Other specific techniques existed, but were not adaptable to many material classes
- Vibrating coil technique used a coil with the detection axis parallel to the applied field
  - Idea modified by Dr. Simon Foner of MIT to vibrate the sample and use a coil perpendicular to the applied field

# VSM Basics

- In a uniform magnetic field, a ferromagnetic sample is vibrated along the z axis
- The dipole field induces a current in the pickup coils, which is proportional to the magnetic moment
- Susceptibility is obtained as the slope of the M-H Curve
- Permeability is obtained as the slope of the B-H Curve



# Mechanical Design



- 1) Loudspeaker Transducer
- 2) Paper Cup Support
- 3) Sample Holder "Straw"
- 4) Reference Sample
- 5) Sample
- 6) Reference Coils
- 7) Pickup Coils
- 8) Magnets
- 9) Housing

# Frequency Invariance

- Reference sample attached to sample holder
  - High coercivity material
- Identical coil arrangement to pickup coils
- Loudspeaker vibrates the sample and reference sample at the same frequency
- Phase and Amplitude of coil voltages are directly related via the magnetic moment of the sample

# Time-Varying Dipole Field

Fixed Dipole Scalar Potential

$$\varphi = \frac{Mx}{r^3}$$

Time variant field

$$\varphi_1 e^{j\omega t} \text{ where}$$

$$\varphi_1 = -a \frac{d\varphi}{dZ} = a \frac{MxZ}{r^5}$$

Where the flux pattern is

$$-\nabla\varphi_1$$

The pattern allows for a variety of coil arrangements where the coil axis is along a flux line.

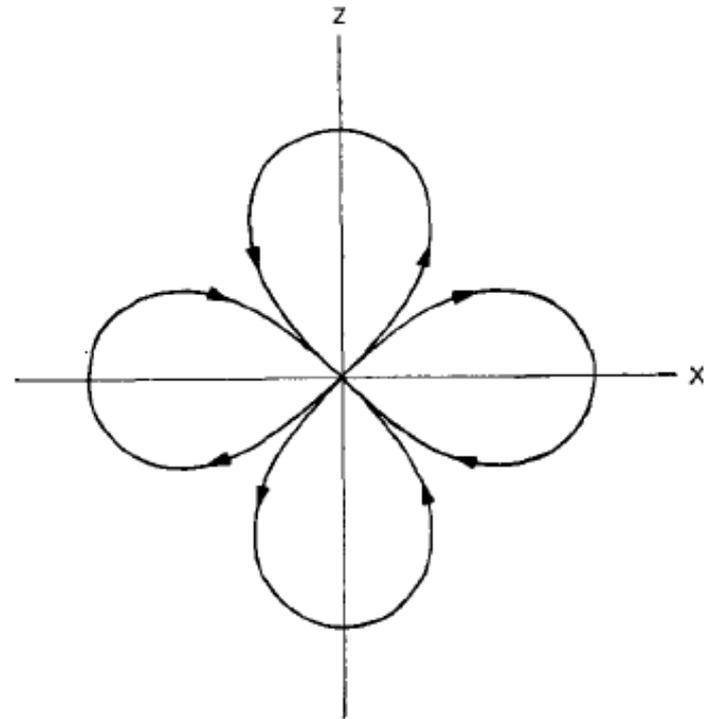


FIG. 4. Time varying part of dipole field in X-Z plane for vibration parallel to Z and dipole moment parallel to X.

# Circuitry

- Many options for output signal measurement
  - Always a temperature controlled resistor in series with the pickup coils
    - Voltage drop is proportional to magnetic moment,  $m$
  - Lock-in Amplifier to compare reference signal and sample signal.
  - Null Amplifier from a calibrated diode bridge
  - Reference signal is controlled with a potentiometer for precise voltage division to balance with the sample output

# Sensitivity

- Sensitivity depends on coil geometry
- With a 2 vertical coil method
  - Susceptibility changes of  $5 \times 10^{-10}$  can be measured
  - Magnetic moment changes of  $5 \times 10^{-6}$  emu
  - Average stability of balanced signals is 1 part in 10,000

# Calibration

- Can be calibrated by 2 methods
  - Using a sample of known magnetic properties and mass
    - Usually 8mg of pure Nickel (high coercivity)
  - For weakly magnetic samples of obscure shape
    - First measure the sample in vacuum
    - Then measure in pure O<sub>2</sub> gas (well known susceptibility)
    - The difference of the two gives the susceptibility of the sample, which is used to calibrate that specific shape

# Demagnetizing Factor

- Calibration is used to determine the Demagnetizing Factor,  $\gamma$
- Once  $\gamma$  and  $m$  are determined, the BH curve can be extracted

$$M = 4\pi \frac{m}{V}$$

$$H_{internal} = H_{applied} - 4\pi\gamma M$$

$$B = H_{internal} + 4\pi M = H_{applied} + 4\pi M(1 - \gamma)$$

Sample  $\gamma$  values...

Sphere:  $\gamma = \frac{4\pi}{3}$ ,

Infinite plane:  $\gamma = 4\pi$ ,

Cylinder:  $\gamma = 2\pi$

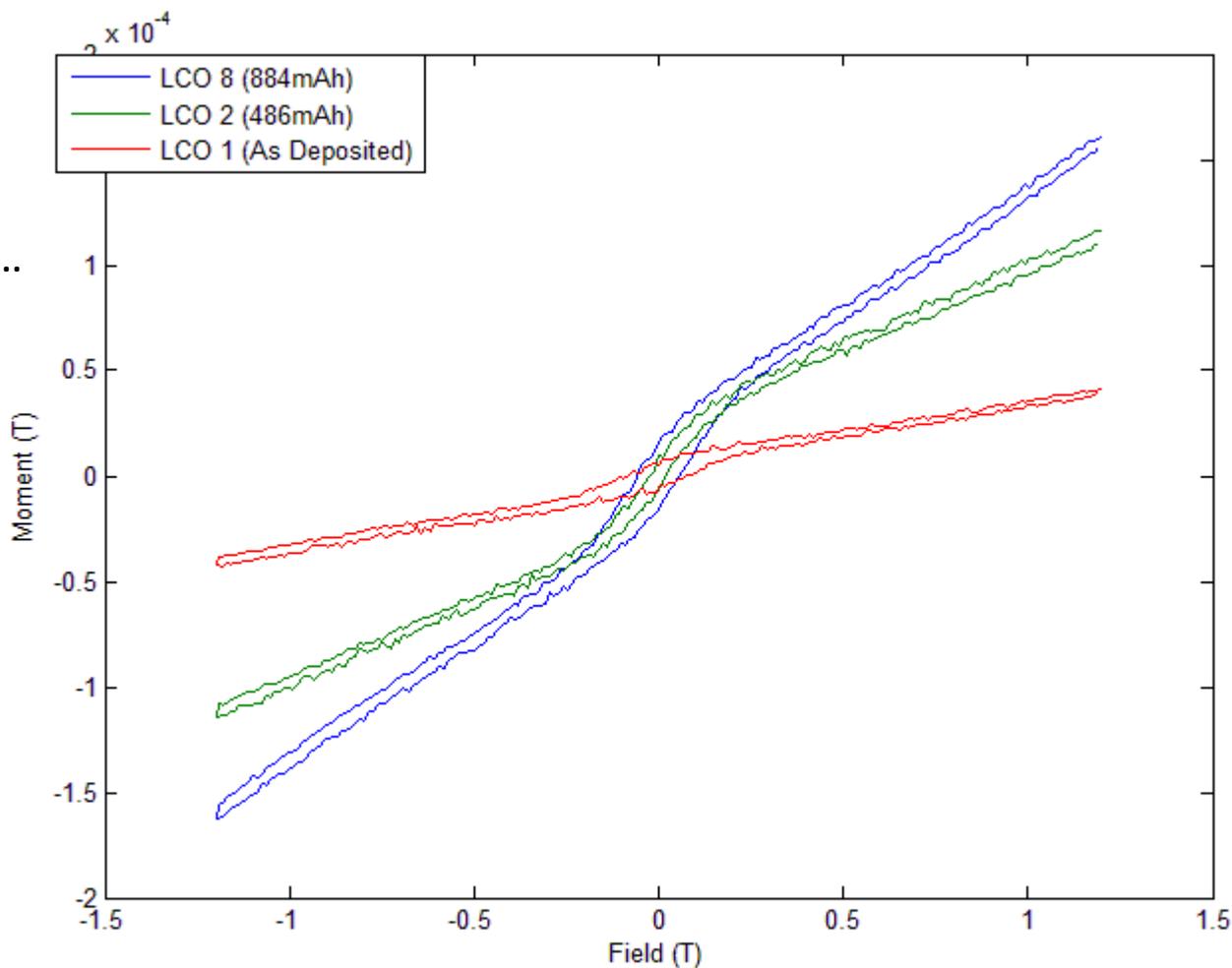
Other shapes are well documented

Note: SI equations only, CGS equations vary

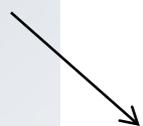
# Measurements

- Low-Conductivity Materials
  - Spherical or ellipsoid samples are preferred
  - Cubic crystals should be oriented 110 perpendicular to the z-axis
- High Conductivity Materials
  - Demagnetization corrections are not necessary
- Paramagnetic Samples
  - VSM can measure the magnetic field created by paramagnetic materials by the average value over the sample volume

# Sample Data



Actually emu...



# Sources

- FONER, S. "Versatile and Sensitive Vibrating-sample Magnetometer." Review of Scientific Instruments, 30.7 (1959): 548-557.
- <http://stephenmullens.co.uk/projectwork/Vibrating%20Sample%20Magnetometer.pdf>
- [http://www.lakeshore.com/pdf\\_files/systems/vsm/Permanent%20Magnet%20Paper.pdf](http://www.lakeshore.com/pdf_files/systems/vsm/Permanent%20Magnet%20Paper.pdf)
- <http://magician.ucsd.edu/essentials/WebBookse7.html>
- <http://bohr.physics.berkeley.edu/classes/221/0708/notes/emunits.pdf>



# Transmission Electron Microscopy (TEM)

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ECE-4813

Fall 2011

Dr. Alan Doolittle



**Georgia** Institute  
of **Technology**<sup>®</sup>

# Why TEM?

- Limited image resolution in light microscopes
- Smallest distance that can be resolved by VLM:

$$\delta = \frac{0.61\lambda}{NA}$$

- Around 300nm for green light ( $\lambda=550\text{nm}$ ) w/  $NA=1$
- That is 1000 atom diameters
- Need to image details all the way down to the atomic level
  - Solution: TEM

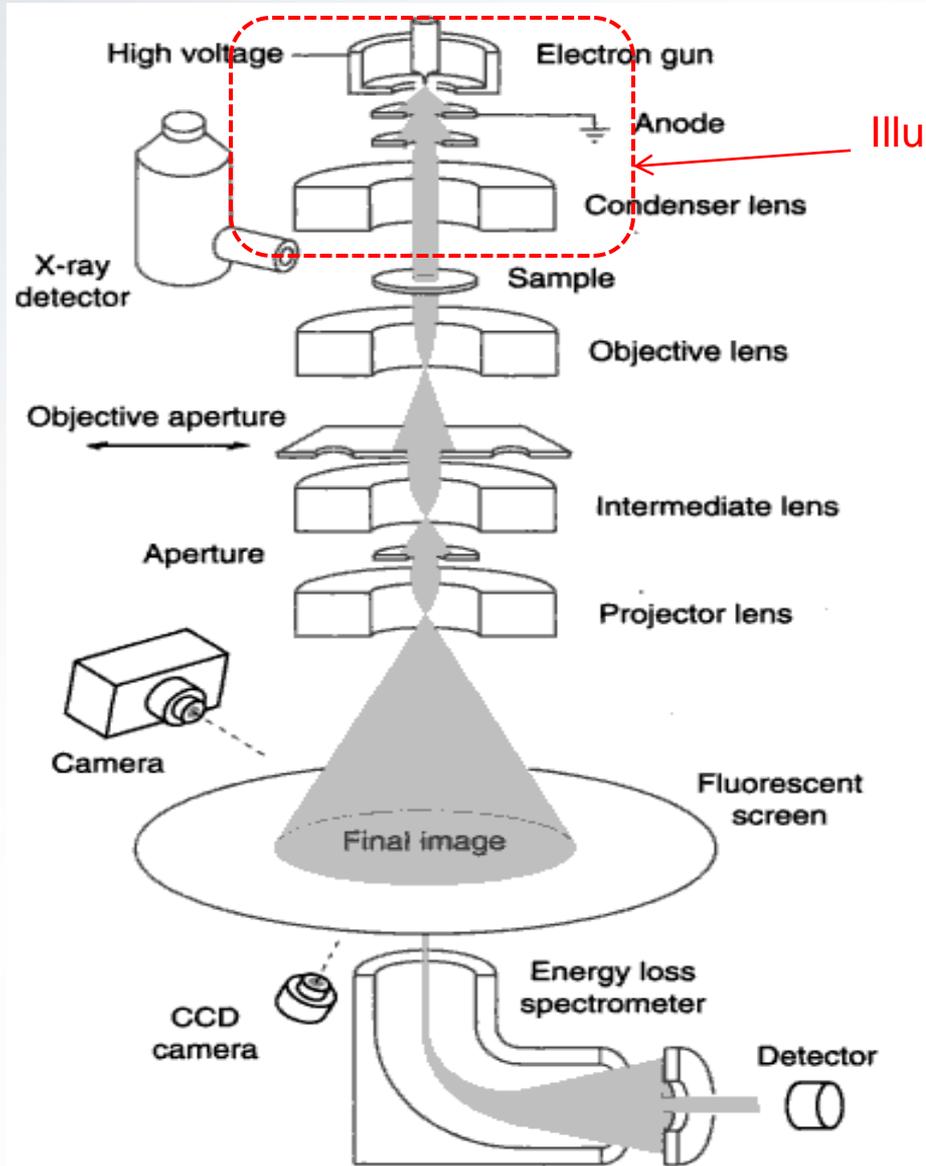
# Electron Wavelength

$$\lambda = \frac{h}{\left[2m_0E\left(1 + \frac{E}{2m_0c^2}\right)\right]^{1/2}}$$

- At high energies electrons approach the speed of light
- Relativistic effect must be taken into account

Accelerating voltage (kV)	Non-relativistic wavelength (nm)	Relativistic wavelength (nm)	Mass ( $\times m_0$ )	Velocity ( $\times 10^8$ m/s)
100	0.00386	0.00370	1.196	1.644
120	0.00352	0.00335	1.235	1.759
200	0.00273	0.00251	1.391	2.086
300	0.00223	0.00197	1.587	2.330
400	0.00193	0.00164	1.783	2.484
1000	0.00122	0.00087	2.957	2.823

# Schematic of TEM

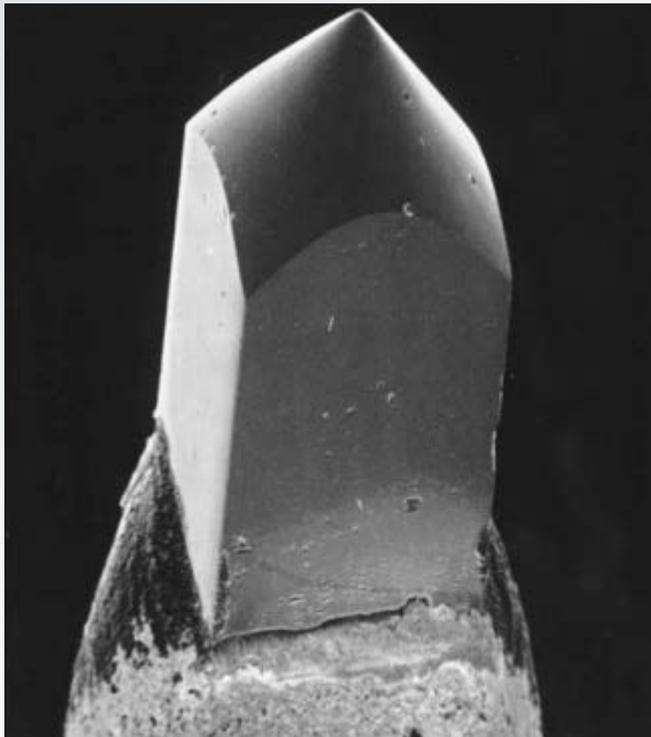


# Illumination System (Electron Emission)

- Field Emission
  - Uses large electric fields at sharp points
  - Electrons tunnel out of source
  - Source: tungsten wire
- Thermionic Emission
  - Uses heat
  - Electrons gain enough energy to overcome natural barrier  $\Phi$
  - Sources:
    - Tungsten filaments
    - LaB6 crystals

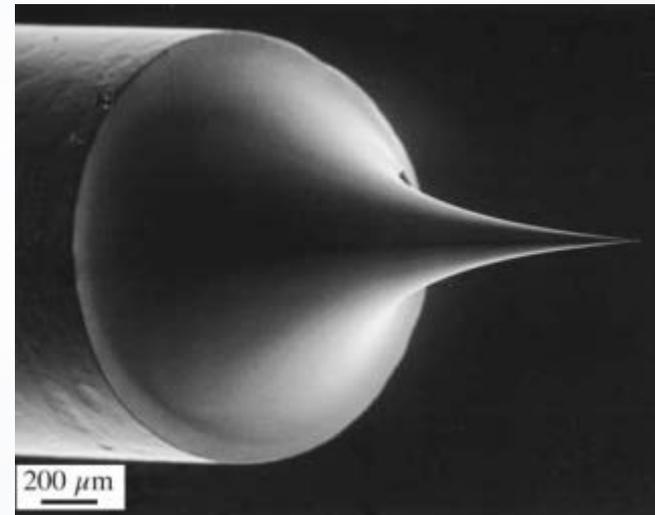
# Electron Sources

## Thermionic emission source



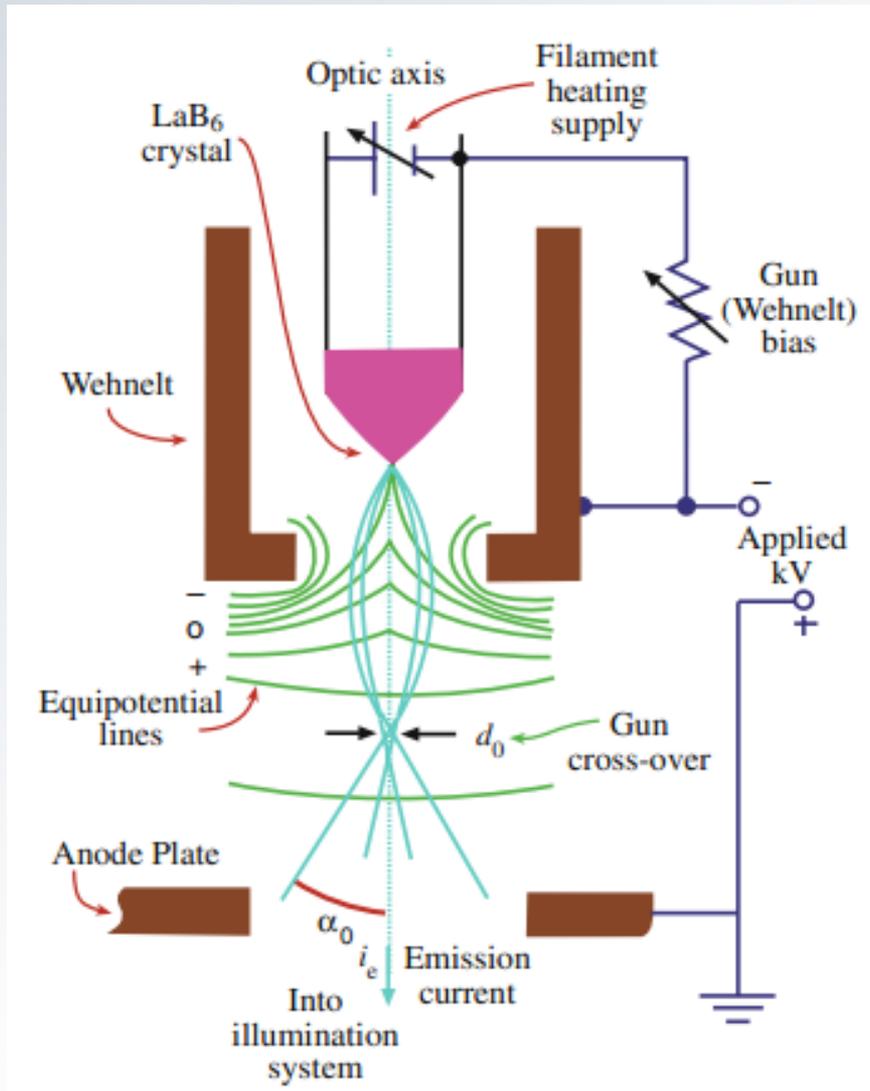
LaB6 crystal

## Field emission source



Tungsten needle

# Illumination System (Electron Gun)

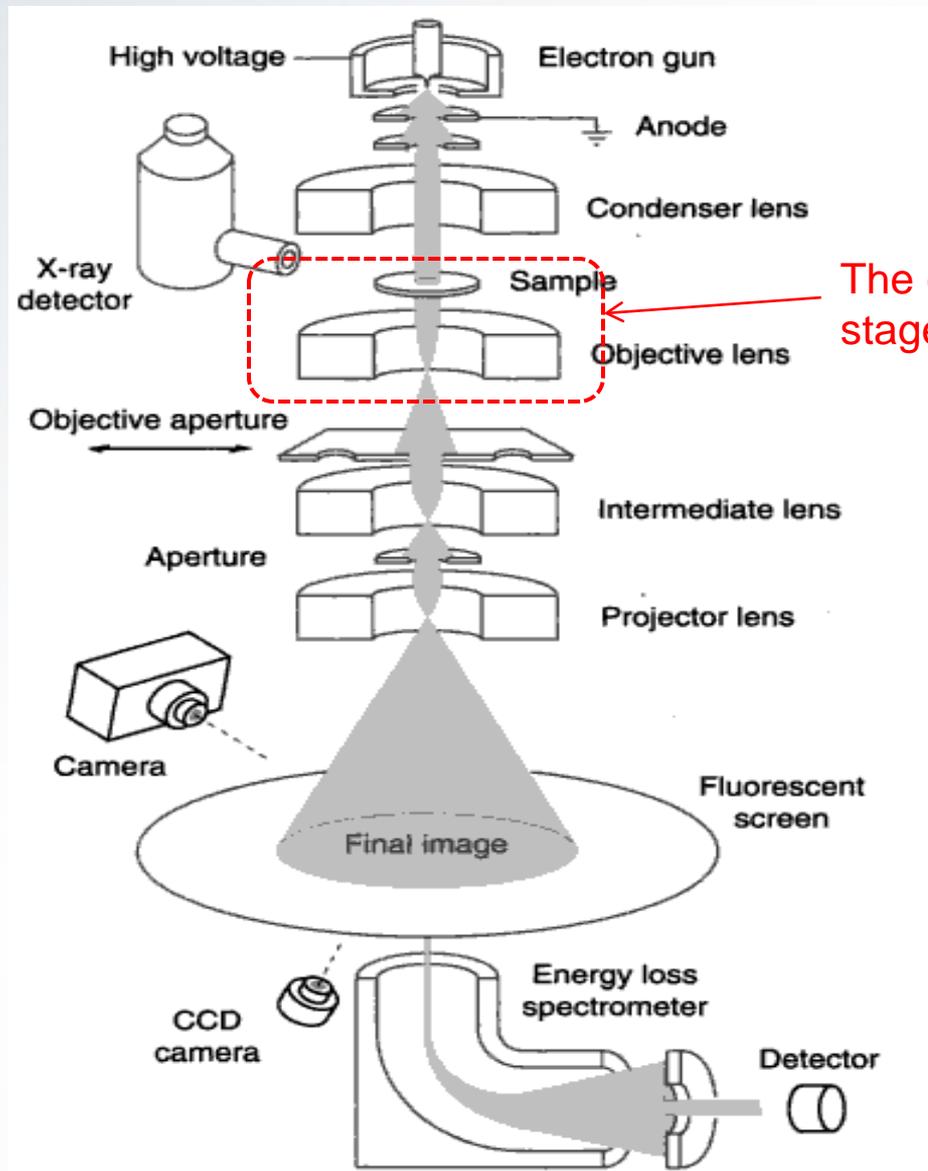


## Thermionic electron gun

# Illumination System (Condenser Lenses)

- Parallel electron beam
  - TEM imaging
  - Selected-area diffraction (SAD)
- Convergent beam
  - STEM
  - AEM
- Dependent on mode of operation

# Schematic of TEM



The objective lens & stage

# Objective Lens (Cs Correction)

- Instrumental resolution is limited primarily by spherical aberration of the objective lens

HRTEM Images

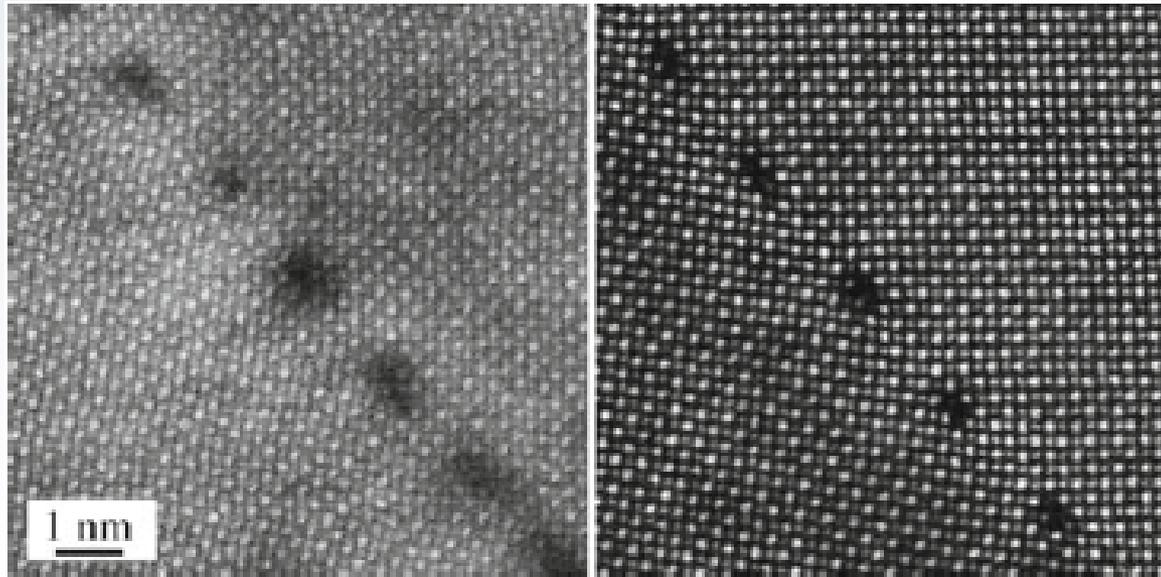
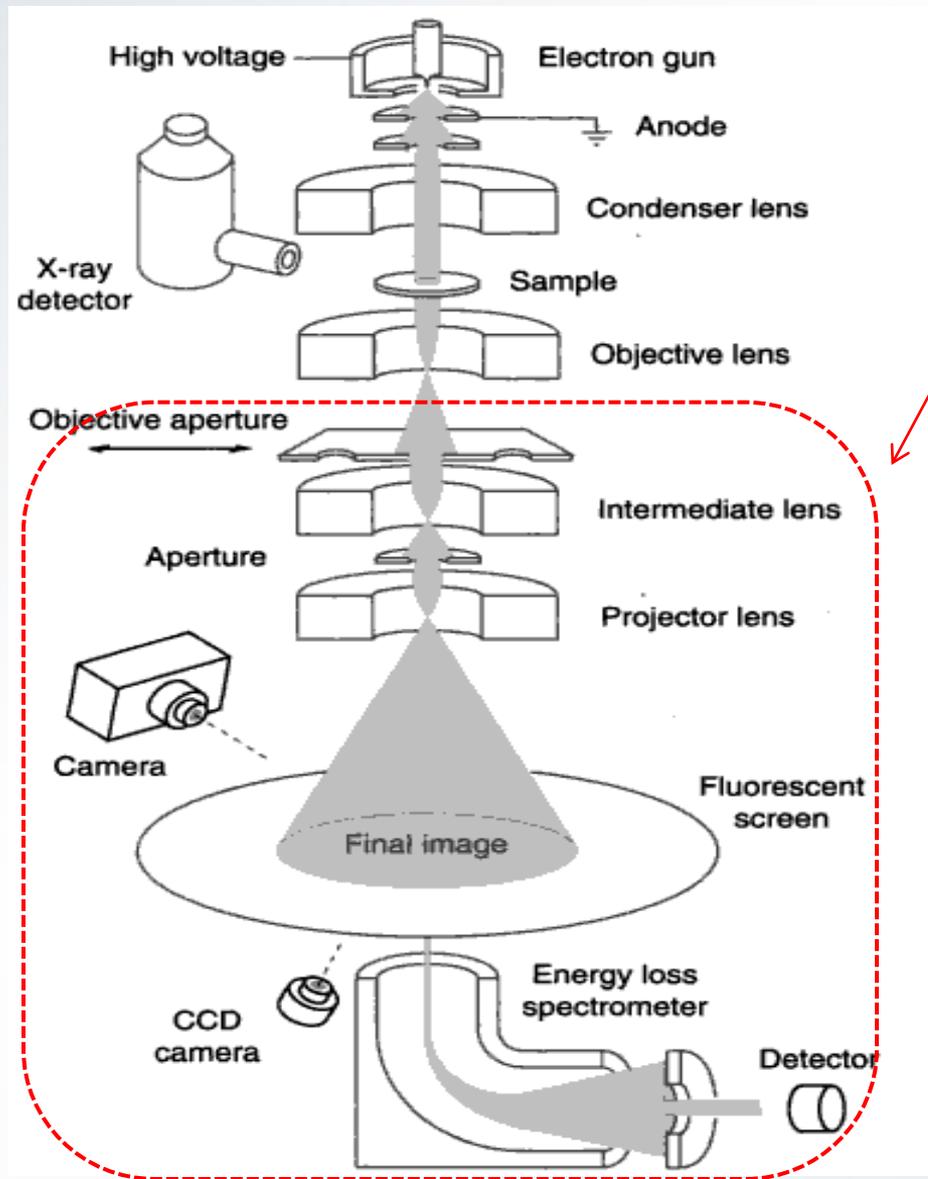


Image w/o Cs correction

Image w/ Cs correction

# Schematic of TEM



Imaging system

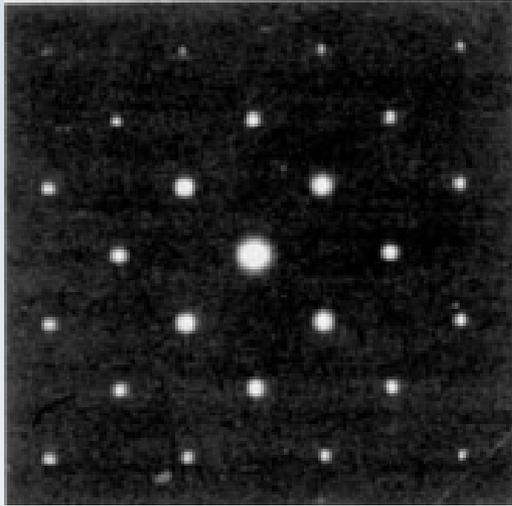
# Imaging System

- Post-specimen lenses
  - Magnify signal transferred by objective lens
    - Diffraction pattern
    - Image
- Viewing images and DPs
  - Fluorescent screen
  - Photographic film
  - CCD camera

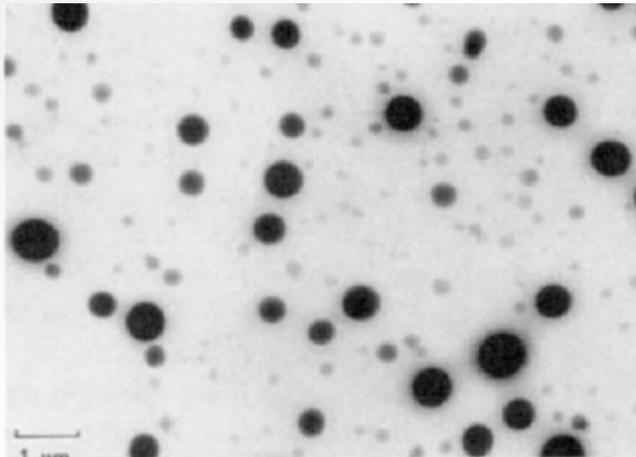
# TEM Modes of Operation

- Diffraction mode
- Image mode
  - Bright-field microscopy
    - Block all diffracted beams and pass only transmitted electron beam
  - Dark-field microscopy
    - Allows diffracted beams and block transmitted electron beam
  - High-resolution electron microscopy
    - Admits transmitted beam and at least one diffracted beam

# Example Images



DP from a single crystal Fe thin film



BF TEM image of a specimen

# TEM Uses

- Crystal structure
- Lattice repeat distance
- Specimen shape
- Analytical measurements
  - Chemical information
- Study of defects
- Failure analysis

# Advantages

- High lateral spatial resolution compared to other type of microscopes
- High quality and detailed images
- Can produce wide range of secondary signals
  - Backscattered electrons, auger electrons, characteristics x-rays, elastically and inelastically electrons, etc.
- Wide range of applications that can be utilized in a variety of different scientific, educational and industrial fields

# Disadvantages

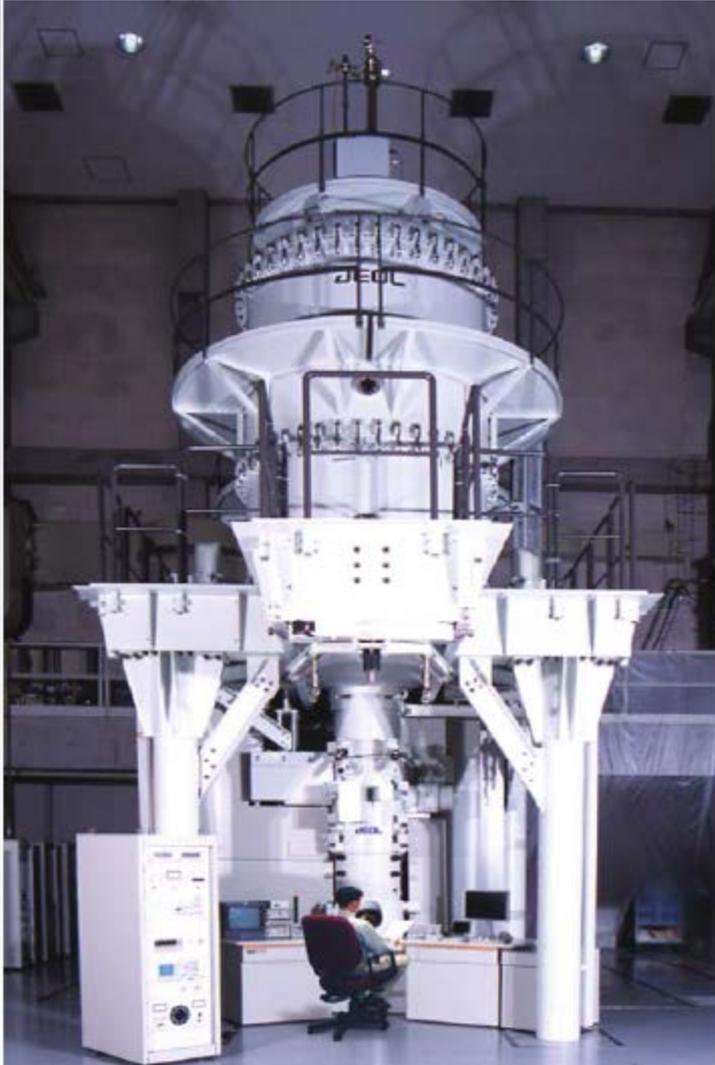
- Limited depth resolution
  - Gives 2D images for 3D specimens
- Specimen preparation
  - Thinning procedure can affect both their structure and chemistry of specimen
  - Time consuming
- Cost
  - About \$5 for each eV

# Types of Transmission Electron Microscopes

- HRTEM (High-resolution)
- HVTEM (High-voltage)
  - Can be damaging to specimen
  - Huge
- IVTEM (Intermediate voltage)
- STEM (Scanning)
- AEM (Analytic)

# Example TEMs

## HVTEM



## HRTEM



# References

- [1] D. Williams and B. Carter, Transmission Electron Microscopy A Textbook for Materials Science, Springer, 2004.
- [2] D. K. Schroder, Semiconductor Material and Device Characterization, Wiley & Sons, 2006.
- [3] C. Evans and R. Brundle, Encyclopedia of Materials Characterization, Butterworth-Heinemann, 1992.
- [4] W. R. Runyan, Semiconductor Measurements and Instrumentation, McGraw-Hill, 1998.

CHICKEN FLAVOR



**Maruchan**

CHICKEN FLAVOR

**Raman**

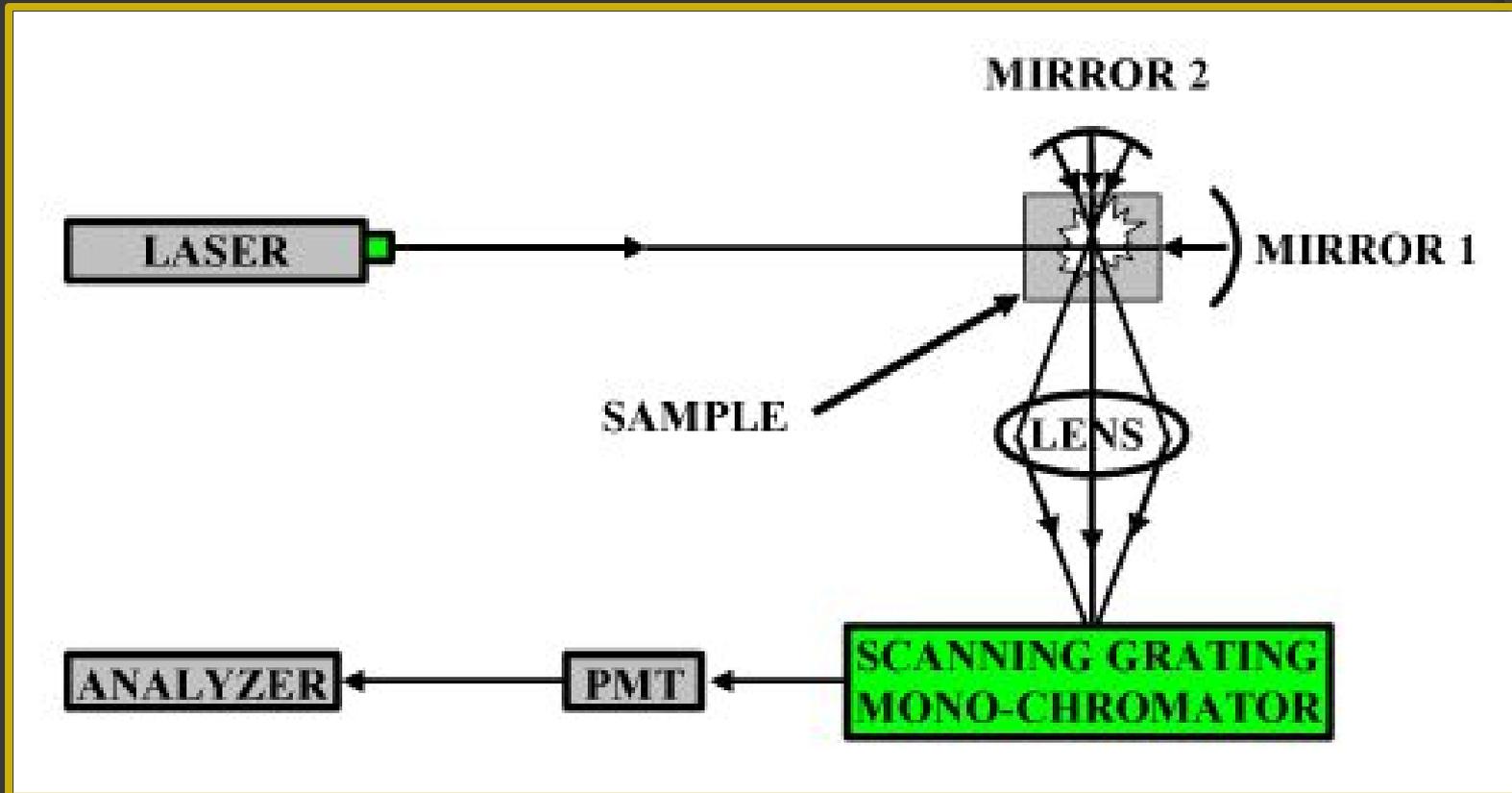
**Spectroscopy**

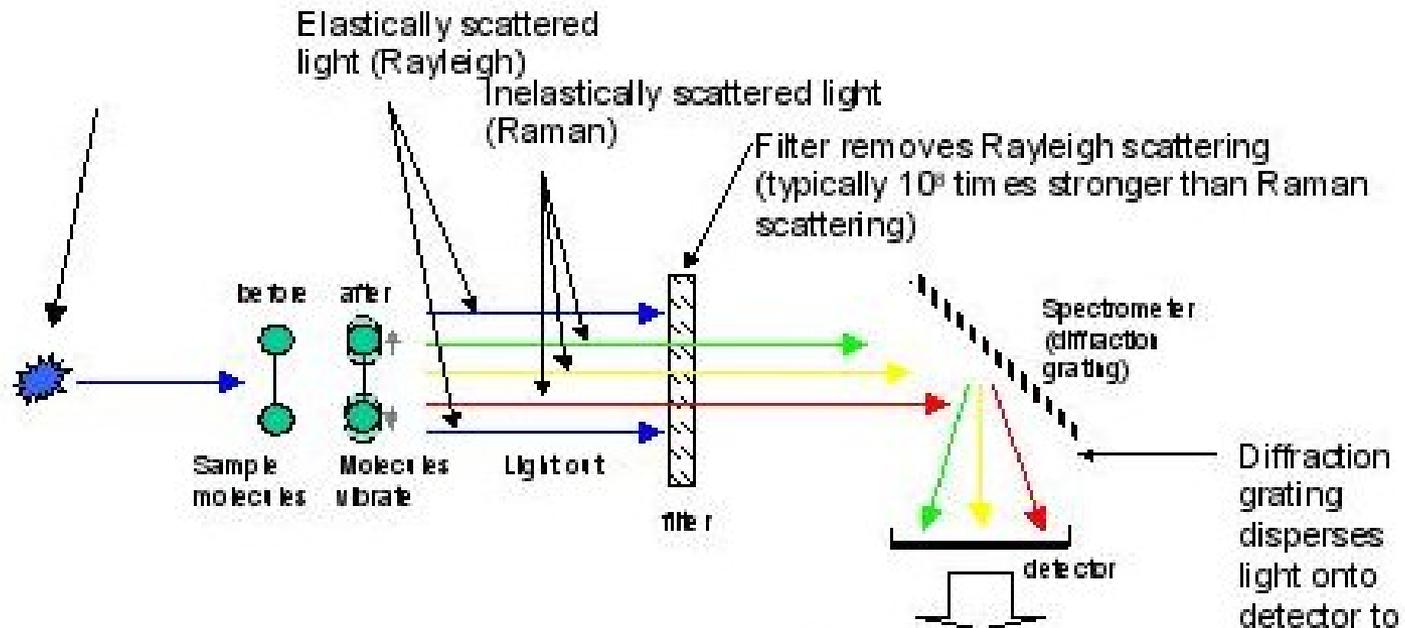
**By Alex Walker**

# Raman Spectroscopy

- ⦿ Based on the effects of Raman effect, first reported in 1928
- ⦿ This is a vibrational spectroscopic technique that can detect both organic and inorganic species and measure the crystallinity of solids
- ⦿ Advantages:
  - Free from charging effects
  - Sensitive to strain

# Raman Spectroscopy

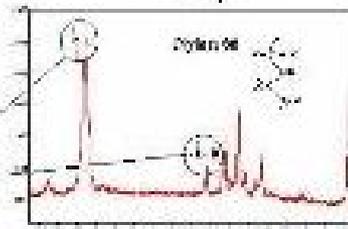




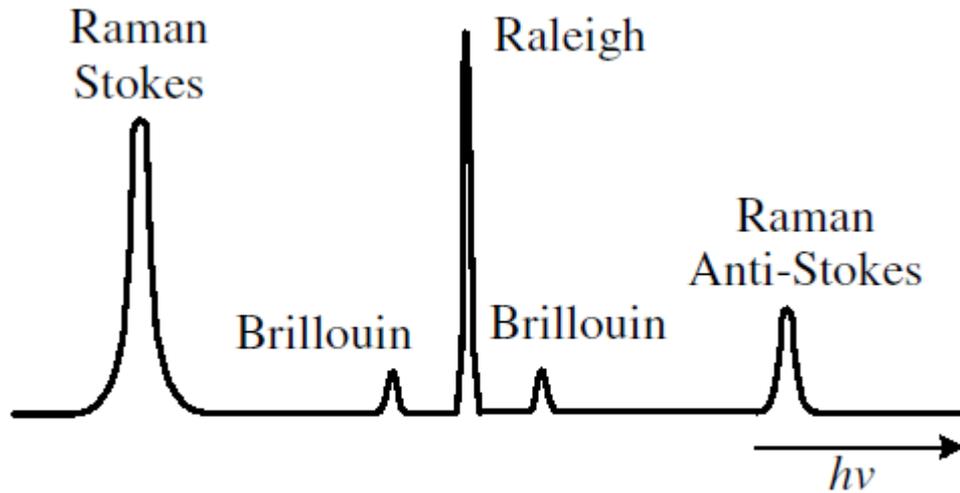
Light loses energy to molecular vibration  
Raman shift:

$$\nu_{\text{laser}} - \nu_{\text{scattered}} = \nu_{\text{Raman}}$$

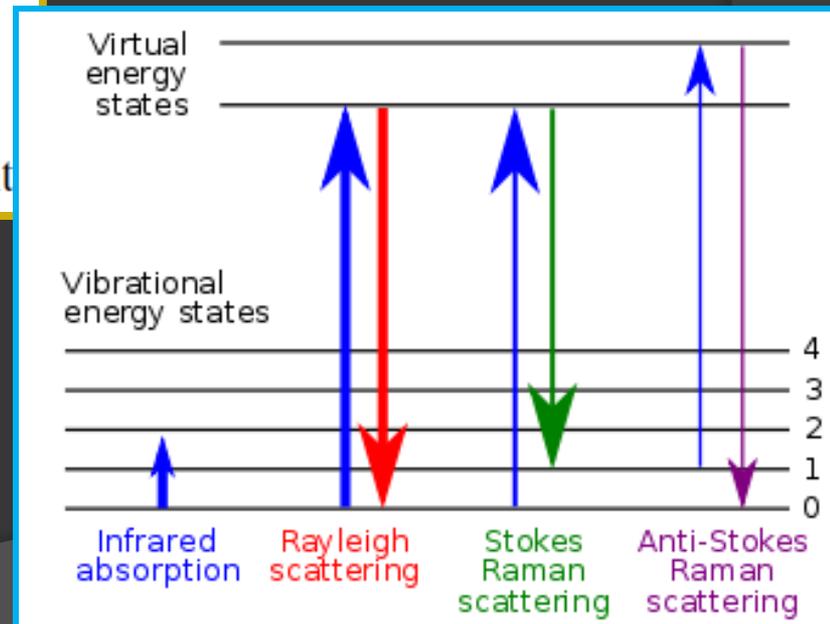
The spectrum gives information  
about molecular bonding



# Types of Scattering



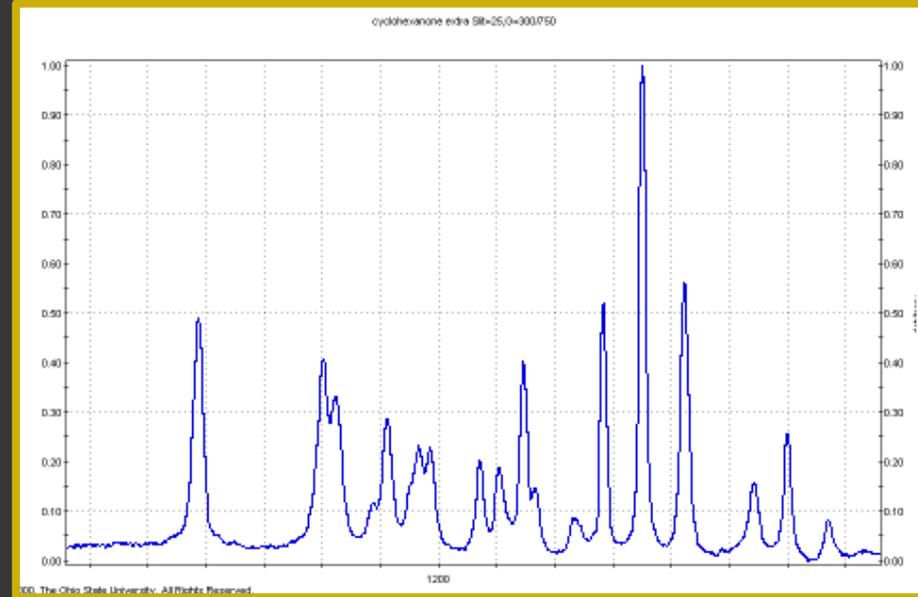
**Fig. 10.31** Energy distribution of scattered light



# Raman Shift

$$\Delta w = \left( \frac{1}{\lambda_0} - \frac{1}{\lambda_1} \right)$$

$$\Delta w(\text{cm}^{-1}) = \left( \frac{1}{\lambda_0(\text{nm})} - \frac{1}{\lambda_1(\text{nm})} \right) \times 10^7 \frac{(\text{nm})}{(\text{cm})}$$



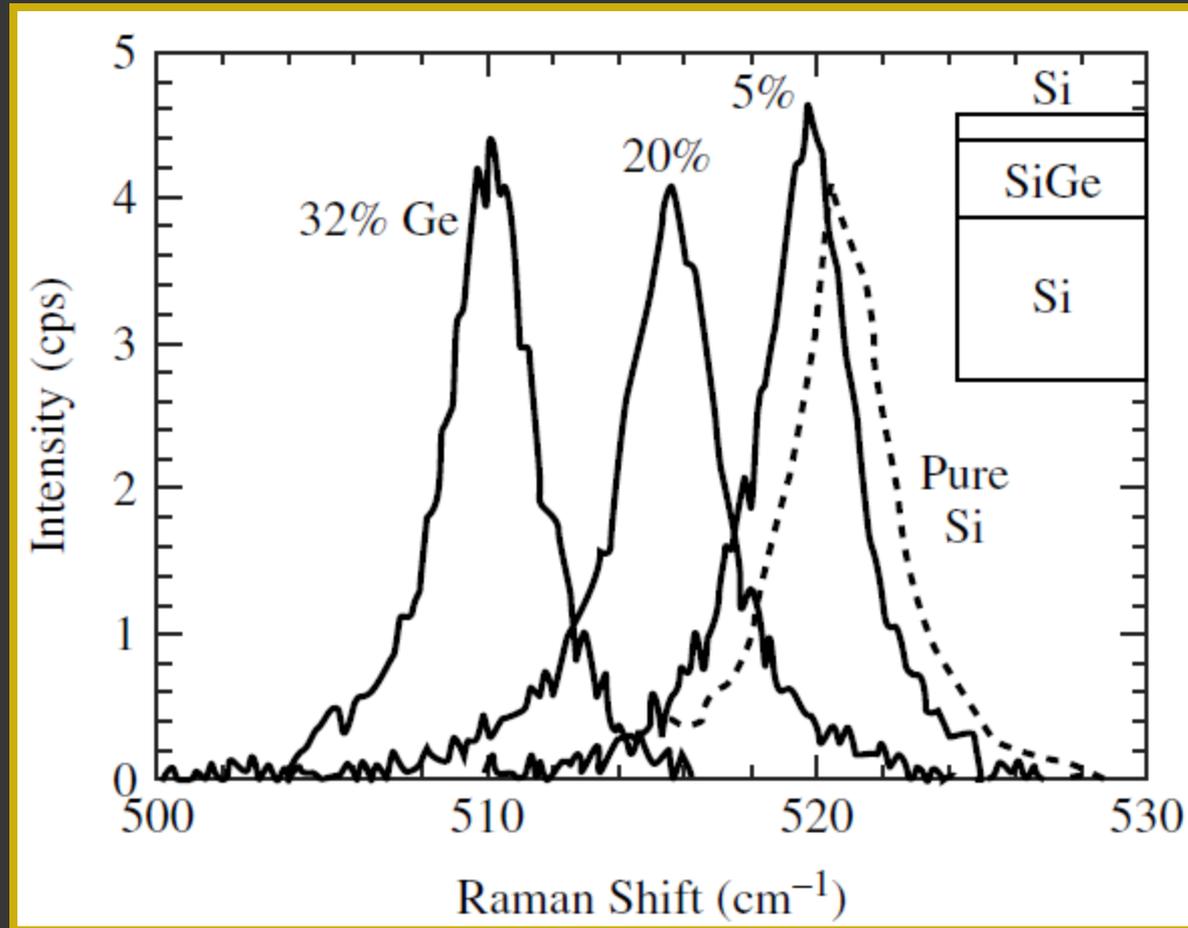
Raman Spectrum of cyclohexanone

$\Delta w =$  Raman shift expressed as a wavenumber

$\Delta\lambda_0 =$  excitation wavelength

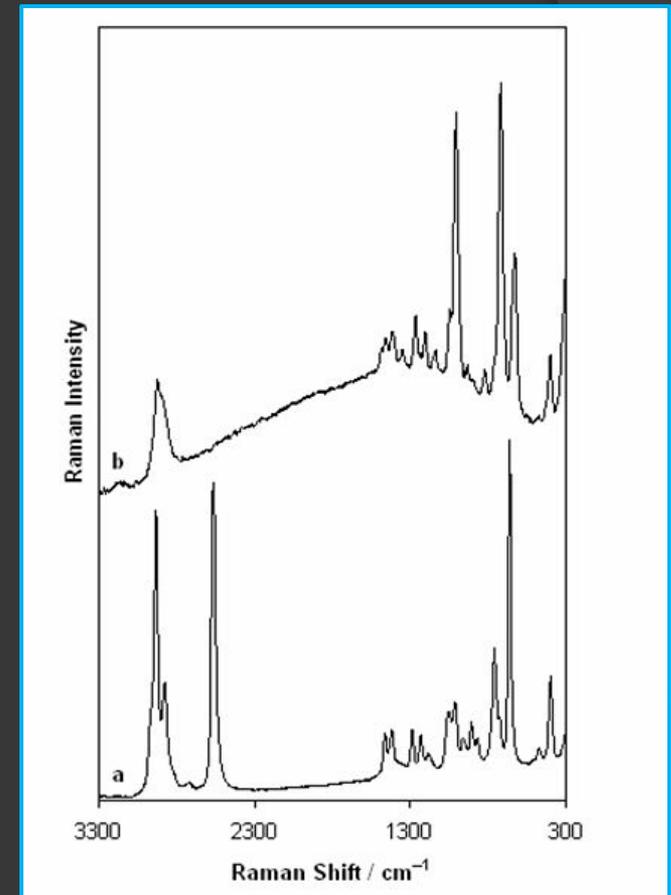
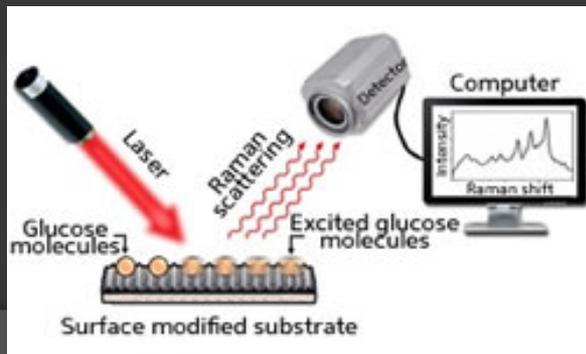
$\lambda_1 =$  Raman spectrum wavelength

# Raman Spectroscopy



# Variations of Raman Spectroscopy

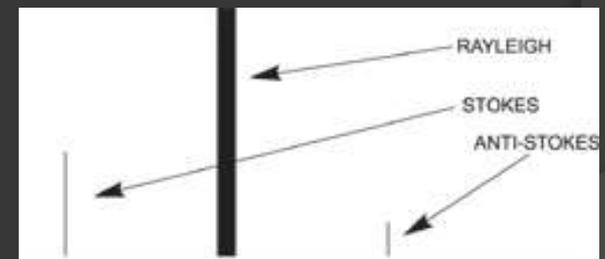
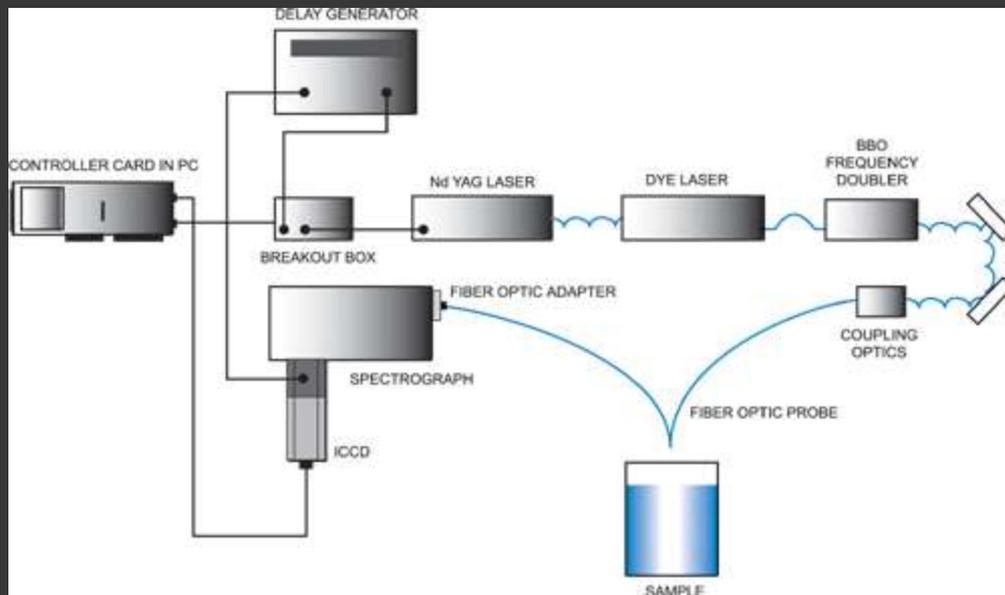
- Surface Enhanced Raman Spectroscopy
  - surface-sensitive technique that enhances Raman scattering by molecules absorbed on rough metal surfaces .



# Variations of Raman Spectroscopy

## ◎ Resonance Raman Spectroscopy

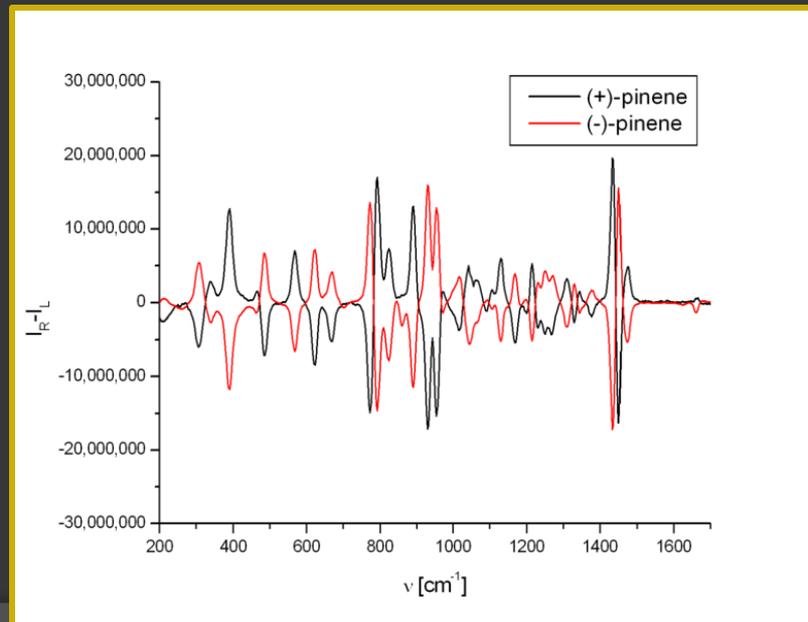
- Uses IR spectrum to identify unknown substances, measure the energy required to change the vibrational state of a chemical compound, and bioinorganic materials.



# Variations of Raman Spectroscopy

## ◎ Raman Optical Activity

- reliant on the difference in intensity of Raman scattered right and left circularly polarised light due to molecular chirality.



# Resources

- [http://www.fdmspectra.com/fdm\\_raman\\_organics.htm](http://www.fdmspectra.com/fdm_raman_organics.htm)
- [http://en.wikipedia.org/wiki/Raman\\_spectroscopy](http://en.wikipedia.org/wiki/Raman_spectroscopy)
- [http://en.wikipedia.org/wiki/Surface\\_Enhanced\\_Raman\\_Spectroscopy](http://en.wikipedia.org/wiki/Surface_Enhanced_Raman_Spectroscopy)
- [http://en.wikipedia.org/wiki/Resonance\\_Raman\\_spectroscopy](http://en.wikipedia.org/wiki/Resonance_Raman_spectroscopy)
- [http://en.wikipedia.org/wiki/Raman\\_optical\\_activity](http://en.wikipedia.org/wiki/Raman_optical_activity)
- [http://en.wikipedia.org/wiki/Raman\\_optical\\_activity](http://en.wikipedia.org/wiki/Raman_optical_activity)
- <http://www.nano.org.uk/news/1368/>
- [http://www.andor.com/learning/applications/Raman\\_Spectroscopy/](http://www.andor.com/learning/applications/Raman_Spectroscopy/)